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The hidden variability of the torus in local Active Galactic Nuclei: 20 years of *Chandra*, *XMM-Newton*, and *NuSTAR* observations

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ABSTRACT

X-ray absorption variability in active galactic nuclei (AGN) provides key constraints on the structure and dynamics of the circumnuclear obscuring medium, the so-called torus. A fraction of nearby AGN, however, have been classified as non-variable in line-of-sight (LoS) column density based on limited temporal coverage. We present the first systematic study of a sample of 11 local ($z \leq 0.1$) obscured ($N_{\text{H}} \geq 10^{22} \text{ cm}^{-2}$) AGN, initially classified as non-variable. The sample is selected from the *Swift*–BAT 100-month catalog, and comprises 60 observations from *Chandra*, *XMM-Newton*, and *NuSTAR*, spanning timescales from days to nearly two decades. We simultaneously model all available spectra for each source adopting physically motivated torus models: X-skirtor, RXTorusD, and UXCLUMPY. This approach allows us to derive the global properties of the obscurer while tracking possible epoch-to-epoch variations in the LoS column density and intrinsic X-ray emission. We find that the original non-variable classification (based on only two X-ray observations) is frequently not robust: clear $N_{\text{H,LoS}}$ variability is detected in half of the sample, whereas 7 out of 10 AGN require intrinsic flux variability, with the rest showing flux– $N_{\text{H,LoS}}$ degeneracies. We also find that the probability of identifying absorption variability increases with the number of observations, and the largest column density changes preferentially occur on long timescales, consistent with absorption by extended, structured clouds on torus scales. These findings support a clumpy and dynamic obscuring medium as a common feature of nearby AGN and highlight the importance of long-term X-ray monitoring for accurately characterizing AGN obscuration.

1. INTRODUCTION

Active Galactic Nuclei (AGN) display a remarkable diversity in luminosity (with bolometric luminosities ranging from 10^{41} to $10^{48} \text{ erg s}^{-1}$), spectral properties, and classification. Despite this apparent variety, they are all powered by the same fundamental mechanism: the accretion of matter onto a supermassive black hole (SMBH; $M_{\text{BH}} \sim 10^6 - 10^{10} M_{\odot}$)

located at the gravitational center of $\sim 10\%$ of known galaxies (A. Soltan 1982; D. Richstone et al. 1998). According to the Unified Model (R. Antonucci 1993; C. M. Urry & P. Padovani 1995), the central engine (i.e., a SMBH surrounded by an accretion disk) emits primarily in the optical and ultraviolet, while a hot corona close to the inner disk up-scatters photons to X-rays via inverse Compton processes (F. Haardt & L. Maraschi 1991, 1993; A. C. Fabian et al. 2015; C. Ricci et al. 2017). Meanwhile, the observed differences among AGN arise mainly from geometrical and orientation effects caused by an optically thick, dusty, molecular torus surround-

ing the nucleus (for a review see [R. C. Hickox & D. M. Alexander 2018](#)). This molecular torus, extending from ~ 1 pc up to few times 100 pc from the SMBH (e.g., [W. Jaffe et al. 2004a](#); [L. Burtscher & K. R. W. Tristram 2013](#)), absorbs ultraviolet and optical radiation from the accretion disk and thermally re-emits it in the infrared, producing a characteristic peak around tens of microns ([J. H. Krolik & T. Di Matteo 2000](#)). Its orientation relative to the observer determines the observed AGN type. When the line-of-sight (LoS) does not intercept the torus, both the broad-line region (BLR) and the narrow-line region (NLR) are visible, yielding a Type 1 optical spectrum; when the LoS intercepts the torus, the BLR is hidden and only narrow lines remain, resulting in a Type 2 AGN. In X-rays, the same geometry leads to different levels of absorption by material characterized by a hydrogen column density ($N_{\text{H,LoS}}$): sources with $N_{\text{H,LoS}} < 10^{22} \text{ cm}^{-2}$ are unobscured, those with $10^{22} \leq N_{\text{H,LoS}} < 1.5 \times 10^{24} \text{ cm}^{-2}$ are Compton-thin (CTH), and those exceeding $N_{\text{H,LoS}} \geq 1.5 \times 10^{24} \text{ cm}^{-2}$ are Compton-thick (CTK) AGN (e.g., [G. Matt 2002](#); [A. Comastri 2004](#); [A. Caccianiga et al. 2007](#); [R. Della Ceca et al. 2008](#)). In the nearby Universe, the majority of AGN are obscured, with approximately 70% exhibiting column densities $\geq 10^{22} \text{ cm}^{-2}$. Of these, ~ 20 –50% are predicted to be CTK-AGN (e.g., [G. Ghisellini et al. 1994](#); [M. Ajello 2009](#); [Y. Ueda et al. 2014](#); [T. T. Ananna et al. 2019](#)), although observations recover them to varying degrees of completeness (e.g., [D. Burlon et al. 2011](#); [C. Ricci et al. 2015](#); [E. S. Kammoun et al. 2020](#); [N. Torres-Albà et al. 2021](#); [D. Sengupta et al. 2023](#); [P. G. Boorman et al. 2024](#)). The optical and X-ray classifications therefore generally represent two complementary manifestations of the same geometry, governed by the viewing angle and the column density of the obscuring material.

The physical nature and geometry of the torus remain one of the most debated aspects of AGN unification. Early radiative-transfer models described it as a smooth, continuous distribution of dust and molecular gas, in which the temperature declines with distance from the SMBH ([E. A. Pier & J. H. Krolik 1992](#)). However, interferometric and spectral studies have shown that this description cannot reproduce the observed infrared emission and variability. Instead, a clumpy torus, composed of discrete, optically thick clouds embedded in a more diffuse medium, provides a better match to both theoretical expectations and observations (e.g., [M. Nenkova et al. 2008a](#); [H. Netzer 2015](#); [C. Ramos Almeida & C. Ricci 2017](#); [S. F. Hönig 2019](#)). In this scenario, the obscuration depends probabilistically on the number and distribution of clumps along the line of sight, while the dust temperature and composition may vary even at fixed radius. Hydrodynamical simulations of chaotic cold accretion (CCA) and radiation-driven turbulence ([K. Wada 2012](#); [M. Gaspari et al. 2020](#)) also produce irregular, dynamic structures consistent with

such clumpiness. In the CCA scenario, cold clouds and filaments condense out of a turbulently stirred hot medium, fragment, and circulate through inflow and fountain-like motions while feedback maintains global quasi-equilibrium. In this framework, LoS column density variability naturally traces both compact inner structures (short timescales) and the evolution or rearrangement of larger cloud complexes at larger radii (long timescales), linking observed absorption changes directly to the granularity and dynamics of the circumnuclear medium (e.g., [M. Gaspari et al. 2013, 2017, 2020](#)).

A major step forward in constraining the geometry of this obscuring medium came from X-ray polarimetry. The launch of the Imaging X-ray Polarimetry Explorer (*IXPE*; [M. C. Weisskopf et al. 2022](#)) in 2021 enabled, for the first time, direct measurements of polarization in heavily obscured AGN. Observations of the Compton-thick sources Circinus galaxy and NGC 1068 revealed polarization degrees and angles consistent with scattering in a geometrically thick equatorial structure with a half-opening angle of about 45° – 55° from the vertical axis of the system, in line with the Unification Model ([F. Ursini et al. 2023](#); [F. Marin et al. 2024a,b](#)). These measurements provided a further direct confirmation of the torus geometry, demonstrating that the equatorial obscurer is indeed extended and likely inhomogeneous. Polarimetry thus complements spectroscopy: while the former reveals the global scattering and orientation of the system, the latter traces its dynamic and inhomogeneous behavior through temporal variations in absorption.

X-ray absorption variability offers one of the most direct probes of the obscuring material clumpiness. Changes in the $N_{\text{H,LoS}}$ over timescales ranging from hours to years are interpreted as the transits of individual clouds across the observer’s line of sight. For example, NGC 1365 presents rapid transitions between Compton-thin and thick states over days, providing the first strong evidence for BLR-scale obscuring clouds (e.g., [G. Risaliti et al. 2002, 2007, 2009b,c](#)); NGC 4151, showing complex, multi-epoch absorption changes (e.g., [S. Puccetti et al. 2007](#); [T. Beuchert et al. 2017](#)); and NGC 7582, where recurrent N_{H} variations revealed complex absorption: short-timescale variability likely arising from BLR clouds, together with longer-term changes driven by a patchy, Compton-thick torus that both obscures the nucleus and contributes significant reflection (e.g., [S. Bianchi et al. 2009](#); [E. Rivers et al. 2015](#)). Long-term variability has also been detected in NGC 4945 ([T. Yaqoob 2012](#)) and NGC 2992 ([X. W. Shu et al. 2010](#)), while even the archetypal Compton-thick AGN NGC 1068 has shown partial-covering changes over multi-year timescales ([A. Marinucci et al. 2016](#)). These represent only a few examples among the many that have established circumnuclear obscuration as a dynamic, multi-phase phenomenon operating

across multiple spatial scales, and that have laid the groundwork for large-scale statistical studies.

Over the past decade, considerable effort has gone into systematically investigating the $N_{\text{H,LoS}}$ variability in nearby AGN using data from *Chandra*, *XMM-Newton*, *Swift-XRT*, and *NuSTAR* (e.g., G. Risaliti et al. 2002; A. G. Markowitz et al. 2014; S. Laha et al. 2020; D. Esparza-Arredondo et al. 2021; X. Zhao et al. 2021; S. Marchesi et al. 2022; A. Tanimoto et al. 2022). The Clemson-INAF Compton thick AGN (CI-CTAGN) project extends this effort by assembling a large, homogeneous sample of obscured AGN to constrain both line of sight and global torus properties through simultaneous, multi-epoch spectral modeling with physically motivated torus models such as MYTorus (K. D. Murphy & T. Yaqoob 2009), borus02 (M. Baloković et al. 2018), UXCLUMPY (J. Buchner et al. 2019), and XCLUMPY (A. Tanimoto et al. 2019). These studies collectively show that approximately one-third to one-half of local CTH-AGN exhibit significant $N_{\text{H,LoS}}$ variability, while the rest appear consistent with being non-variable within observational uncertainties (N. Torres-Albà et al. 2023; A. Pizzetti et al. 2025, see Sect. 2 for more details).

However, AGN with no detected $N_{\text{H,LoS}}$ variability challenge our understanding of AGN obscuration and the clumpy torus paradigm. A true lack of column density variability (or only yearly-scale changes) would require clouds much larger, denser, and more uniform than typically inferred (e.g., M. Nenkova et al. 2008a; S. Laha et al. 2020), suggesting a smoother or more extended torus, possibly dominated by stable circumnuclear dust lanes (consistent with interferometric evidence for extended, stable dust distributions on parsec to hundred-parsec scales in nearby AGN; e.g., W. Jaffe et al. 2004b; C. Packham et al. 2005; S. F. Höning et al. 2010; K. R. W. Tristram et al. 2014; M. Mezcuca et al. 2016) or galactic-scale absorbers (such as misaligned or warped disks and kpc-scale gas concentrations; e.g., M. A. Malkan et al. 1998; A. D. Goulding et al. 2012; J. Buchner & F. E. Bauer 2017). Alternatively, this apparent stability may arise from observational biases, such as limited temporal coverage or sensitivity (S. Bianchi et al. 2012; R. C. Hickox & D. M. Alexander 2018; G. Mazzolari et al. 2024; I. S. Cox et al. 2025). Disentangling these scenarios would require continuous X-ray monitoring over days to years to resolve the full structure of the obscuring medium in individual AGN, an observational effort of considerable scale. However, decades of archival X-ray observations offer a powerful resource for investigating $N_{\text{H,LoS}}$ variability and constraining the geometry and distribution of the absorbing material. Within this framework, this paper inaugurates a series dedicated to the study of Compton-thin and Compton-thick AGN initially classified as non-variable (X. Zhao et al. 2021, see Sect. 2 for the selection criteria). We conduct a systematic study of a sam-

ple of 11 such sources, comprising 60 X-ray observations from *Chandra*, *XMM-Newton*, and *NuSTAR*, with three to nine observations per AGN with separations ranging from 1 day (i.e., consecutive observations) to ~ 20 years. The paper is organized as follows: Sect. 2 details the sample selection and data reduction procedures; Sect. 3 reports the methodology adopted during the analysis; Sect. 4 provides a comparison between the three torus models; Sect. 5 presents the X-ray (CTH- or CTK-AGN) and variability classifications for the sample; Sect. 6 discusses the time evolution of epoch-to-epoch changes in $N_{\text{H,LoS}}$; Sect. 7 reports the statistical analysis of the torus and AGN parameters derived from the best-fit models; Sect. 8 shows the results of the spectral analysis for MCG-03-34-064; and Sect. 9 summarizes the main findings.

In this paper, we use as cosmological constants $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$, $\Omega_{\Lambda_0} = 0.73$, and $\Omega_{\text{M}} = 0.27$. Errors are quoted at the 90% confidence level (c.l.). We consider a probability of 0.01 (roughly corresponding to $\sim 2.6\sigma$ for a Gaussian distribution) as a statistically significant threshold for the null hypothesis probability (NHP; i.e., $\text{Log}(\text{NHP}) < -2.00$).

2. DATA

2.1. Sample selection

The present paper is part of the CI-CTAGN¹⁶ project and within it, of the N_{H} variability project that aims at deriving and studying the torus properties of a well-defined sample of obscured AGN, and their variability (or lack thereof) through multi-epoch X-ray observations. The original sample was selected by X. Zhao et al. (2021), who performed a broadband X-ray spectral analysis of 93 Compton-thin AGN in the nearby Universe ($z \leq 0.1$), all with archival *NuSTAR* coverage. The sources were drawn from the Swift-BAT (Burst Alert Telescope; S. D. Barthelmy et al. 2005) 100-month catalog¹⁷. For each selected AGN, X. Zhao et al. (2021) jointly fitted one *NuSTAR* observation, to account for the hard X-ray (3 – 79 keV) coverage, together with a single soft (0.3 – 12 keV) X-ray observation (from either *XMM-Newton*, *Chandra*, or *Swift-XRT*), to constrain both the torus geometry parameters and the line-of-sight column density. The presence of *NuSTAR* data is critical for obscured AGN, where soft X-rays are attenuated, as it enables disentangling reflection from LoS absorption and provides robust constraints on the properties of the obscuring torus (F. Civano et al. 2015; S. Marchesi et al. 2018). In their preliminary study, X. Zhao et al. (2021) identified 31 AGN as variable in intrinsic flux or $N_{\text{H,LoS}}$ (“variable sample”, hereafter), and 62 as non-variable (“non-variable sample”, hereafter). To be noted that for 22 out of 93 (i.e., 23.7%) AGN, X. Zhao et al. (2021) consid-

¹⁶ <https://science.clemson.edu/ctagn/>

¹⁷ http://bat.ifc.inaf.it/100m_bat_catalog/100m_bat_catalog_v0.0.htm

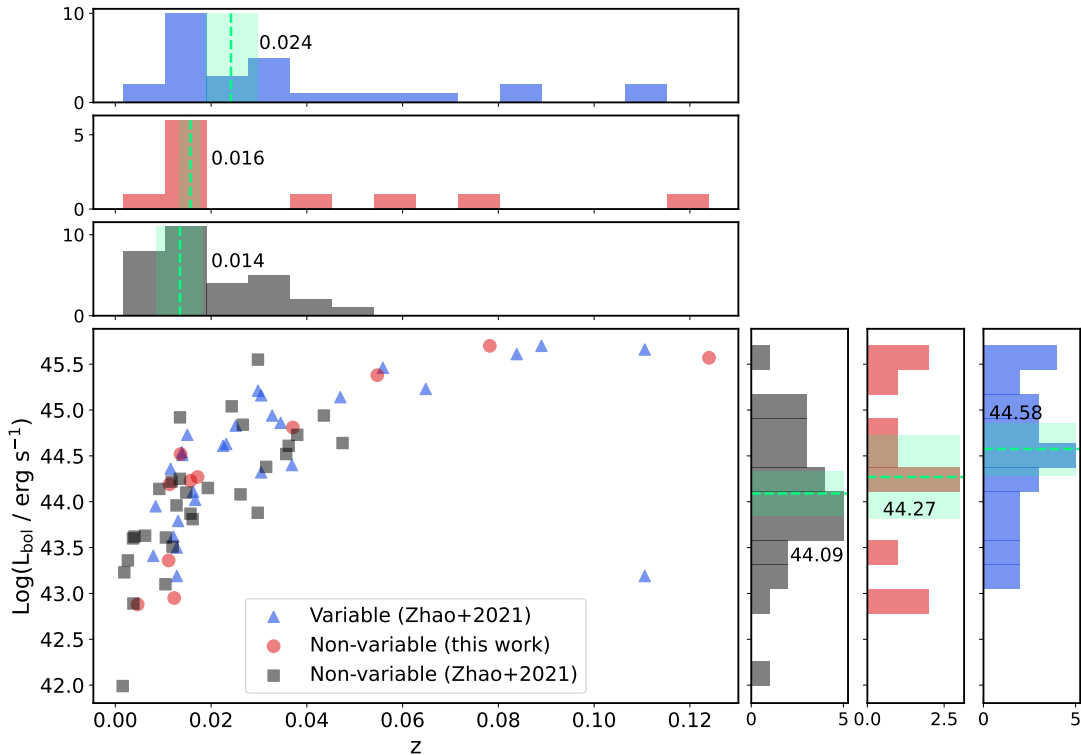


Figure 1. Samples comparison: bolometric luminosity versus redshift. The variable sample (in blue triangles; I–V), the sub-sample of non-variable AGN studied in this paper (in red circles), and the non-variable sources to be analyzed in upcoming papers (in gray squares) are shown. For each sample, the distributions are displayed above the scatter plot, and the green dashed lines with shaded bands indicate the median values and the corresponding median absolute deviations, $MAD = \text{median}(|x_i - \text{median}(x)|)$. The outlier AGN of the variable sample is NGC 6300, analyzed in IV. The KS-tests show no statistically significant differences between the bolometric luminosity or redshift distributions of the sub-samples, supporting a direct comparison between the variable and non-variable sources.

ered *NuSTAR* and soft X-ray simultaneous observations, introducing a possible bias towards a non-variable classification for these sources. In papers I – V (A. Pizzetti et al. 2022; N. Torres-Albà et al. 2023; A. Pizzetti et al. 2025; D. Sengupta et al. 2025; N. Torres-Albà et al. 2025, respectively), 28 out of 31 variable AGN have been the subject of detailed follow-up investigations. Given the large number of available observations, papers I; IV; V were dedicated to single-source studies of the variable AGN NGC 7582, NGC 6300, and Mrk 477, respectively. Meanwhile, in papers II and III, sub-sets of 12 (total of 53 observations) and 13 (total of 52 observations) variable sources have been studied. Across the combined sample of 28 variable AGN, 39% (11/28) shows clear $N_{\text{H,LoS}}$ variability to adequately reproduce the data, and also require flux changes. The remaining 61% (17/28) is consistent with flux variability alone. Considering both geometrical and intrinsic properties, we find no intrinsic differences between the Variable, Non-variable, and Undetermined¹⁸ groups. Nearly half the sources (13/28) require a Compton-thick reflector in UXCLUMPY fits. Importantly, ob-

scuration variability is found to be more common on longer timescales: increasing from $\sim 20\%$ at $\Delta t < 10$ days to 60–70% at $\Delta t > 5$ yr, with Mrk 477 providing a clear example (V).

Here, we study the complementary non-variable sample to i) assess the robustness of this classification in light of the all the available multi-epoch data, and ii) to characterize their torus properties. From the non-variable sample, we selected a sub-set designed to be statistically comparable in size and number of observations to the variable sub-groups studied in II and III. This approach allows us to perform an analysis analogous to that carried out on the variable sample, enabling a direct comparison between the two populations. Specifically, our sub-sample contains 11 sources, for a total of 60 observations. The remaining non-variable sources will be analyzed in future dedicated studies. Table 1 lists names, redshifts, classification in the optical and radio bands, bolometric luminosities (taken from the BASS sample; M. J. Koss et al. 2022), and X-ray (2 - 10 keV) fluxes (derived from our spectral analysis, see Sect 5) of the 11 AGN. In Fig. 1, we show the bolometric luminosities as a function of redshift, as well as the parameters distributions, for the variable and non-variable samples. We show only 42 AGN for the non-variable sample in Fig. 1, given that this is the frac-

¹⁸ We report a complete description of the criteria used to classify a source as “Undetermined” in Sect. 3.5.

tion of sources with more than 2 available X-ray observation and thus, the AGN for which a complete broad-band multi-observations analysis can be carried out. We performed the

two-sample Kolmogorov–Smirnov (KS) test to compare the bolometric luminosity and redshift distributions of the samples, and find no statistically significant differences between any pair of samples in either parameter.

Table 1. AGN properties.

(1)	(2)	(3)	(4)	(5)	(6)	(7)	(8)	(9)
Source	z	Optical	X-ray	Radio	$\log(M_{\text{BH}})$ [M_{\odot}]	$\log(L_{\text{bol}})$ [erg/s]	$\log(\lambda_{\text{Edd}})$	$F_{2-10\text{keV}}$ [erg/s/cm ²]
ESO 464-G016	0.037	Sy2	CTH	RQ	8.40	44.81	-1.76	0.46 ± 0.12
IC 5063	0.011	Sy2	CTH	RL	8.24	44.19	-2.22	$7.27^{+0.10}_{-0.25}$
LEDA 511869	0.078	Sy2	CTH	RQ	8.66	45.70	-1.14	$1.19^{+0.10}_{-0.15}$
MCG-03-34-064	0.017	Sy1.8	CTH	RQ	8.37	44.27	-2.28	$2.27^{+0.18}_{-0.20}$
Mrk 18	0.011	Sy2	CTH	RL	7.72	43.36	-2.53	$0.70^{+0.11}_{-0.14}$
Mrk 1498	0.055	Sy1.9	CTH	RQ	7.19	45.38	0.02	$7.23^{+0.05}_{-0.20}$
NGC 1194	0.014	Sy1.9	CTK	RL	7.83	44.52	-1.49	$1.13^{+0.23}_{-0.11}$
NGC 2655	0.005	Sy2	CTH	RQ	8.34	42.88	-3.63	$0.65^{+0.62}_{-0.19}$
NGC 4785	0.013	Sy2	CTH	RQ	8.00 ¹	42.95	-3.15	$1.15^{+0.11}_{-0.10}$
UGC 03752	0.013	Sy2	CTH/CTK	RQ	7.65	44.23	-1.59	$0.43^{+0.01}_{-0.39}$
WISE J144850	0.124	Sy1.2	CTH	RQ	8.14	45.57	-0.74	$4.48^{+0.11}_{-0.36}$

NOTE— *Columns:* 1) source name; 2) redshift; 3) optical classification; 4) radio classification: radio-quiet (RQ) or radio-loud (RL); 5) X-ray classification: Compton-thin (CTH) or Compton-thick (CTK); 6) black hole mass; 7) bolometric luminosity; 8) logarithm of the Eddington ratio; (9) X-ray flux in the 2–10 keV energy range from the best-fit with the UXCLUMPY in units of 10^{-12} erg/s/cm². The reported mass and bolometric luminosity are taken from the BASS sample (M. J. Koss et al. 2022). In particular, they derive L_{bol} from the intrinsic 14–150 keV luminosity using a bolometric correction of 8, while M_{BH} is derived from broad-line virial estimators when available, or from stellar velocity dispersion measurements for obscured sources. For NGC 4785, we derived L_{bol} from the intrinsic, absorption-corrected 2–10 keV luminosity by applying the bolometric correction of F. Duras et al. (2020) with a bolometric correction of 15.4. We note that these estimates are highly uncertain for Seyfert 2 galaxies and should therefore be taken with caution. The Eddington ratios are taken from (M. J. Koss et al. 2022), except for NGC 4785 for which we derive it. The reported flux refers to the first *Chandra* observation, or XMM observation if no *Chandra* data are available. For the other observations, the flux can be derived by multiplying for the cross-normalization constant registered in the source best-fit Tables B.2–B.11. ¹: see note on the source in Appendix C.

2.2. Data reduction

During the analysis of the sample presented in this paper, we use all the available X-ray observations from *Chandra*¹⁹, XMM-Newton²⁰, and NuSTAR²¹.

For XMM-Newton, we use spectra from the EPIC pn (L. Strüder et al. 2001). Data reduction was performed with SAS v22.1, applying the standard filtering procedure to remove background flares. All NuSTAR (F. A. Harrison et al. 2013) observations include both coaligned X-ray telescopes, Focal Plane Module A (FPMA) and B (FPMB). Cleaned and cali-

brated event files were produced using the Nupipeline task together with the calibration database (CALDB 20250122). For both XMM and NuSTAR, source and background extraction radii were determined iteratively to maximize the signal-to-noise (S/N) ratio in the 2 – 10 keV band, following the procedure described in E. Piconcelli et al. (2004). *Chandra* (M. C. Weisskopf et al. 2000) spectra are reduced with CIAO v4.17 and calibration files (CALDB 4.11.6), following standard procedures. To extract the source (background) data a 5'' circle (annulus with internal radius of 6'' and outer of 15'') was adopted. Each region was visually inspected to avoid contamination from nearby sources. XMM, NuSTAR, and *Chandra* have been rebinned considering J. S. Kaastra & J. A. M. Bleeker (2016) optimal binning scheme. In particular, for NuSTAR spectra, we adopted an iterative procedure to ensure the required S/N and same bin width in both FPMA/B. We adopted the C-statistic as fitting statistic. However, for 5

¹⁹ This paper employs a list of *Chandra* datasets, obtained by the *Chandra* X-ray Observatory, contained in the Chandra Data Collection DOI: 10.25574/cdc.467.

²⁰ <https://www.cosmos.esa.int/web/xmm-newton/xsa>

²¹ https://heasarc.gsfc.nasa.gov/docs/nustar/nustar_archive.html

AGN (LEDA 511869, Mrk 18, NGC 4785, NGC 1194, and MCG-03-34-064), the *Chandra* spectra are rebinned to ≥ 15 photon counts per bin and, in these cases, the χ^2 statistic is used. Tables B.2-B.11 report the statistic adopted for each AGN. Table A.1 lists the observation ID, date, and effective exposure time after the filtering process for each observation.

3. METHODOLOGY

To perform the broad-band X-ray spectral analysis, we follow the methodology described in II and III papers, using XSPEC version 12.14.1 (K. A. Arnaud 1996) to fit simultaneously the 0.5 – 10.0 keV XMM-Newton, 0.5 – 8.0 keV *Chandra*, and 3.0 – 79.0 keV NuSTAR spectra. In the following sections, we describe the different model components adopted during our fit.

3.1. Model components

Galactic neutral absorption: phabs component in XSPEC with column densities appropriate for the sky coordinates of each source from P. M. W. Kalberla et al. (2005), representing absorption due to gas in the Milky Way (order of 10^{20} cm $^{-2}$). The value was fixed during the fit.

Soft X-ray model: below ~ 2 keV, the soft X-ray spectrum is affected by the host galaxy emission and is characterized by emission lines (e.g. N. J. Schurch et al. 2004), likely produced by photoionized gas in the NLR, as commonly found in obscured AGN (S. Bianchi et al. 2006; M. Guainazzi & S. Bianchi 2007; S. Bianchi et al. 2019), or by star-formation processes (e.g., P. Ranalli et al. 2003; S. Mineo et al. 2012). We thus include a collisionally ionized diffuse gas component (apec; R. K. Smith et al. 2001). UGC 3752 requires two apec components to describe the multiphase thermal gas with the hotter component closer to the nucleus and more obscured (see N. Torres-Albà et al. 2018). Furthermore, where significant residuals ($\geq 3\sigma$) remain, at the energies of known emission lines, we model them phenomenologically by adding Gaussian components. In Appendix C, we report the number of added Gaussian components and their energies.

Intrinsic flux variability: to account for differences between observations, we apply a multiplicative factor, C_{AGN} , to the intrinsic power-law emission.

Torus model: it describes the primary and reprocessed AGN emissions, including reflection by obscuring Compton-thick material. The models applied in this paper are described in Sects. 3.2, 3.3, and 3.4. For MCG-03-34-064, Mrk 1498, and NGC 1194, we find that the adopted torus models do not adequately reproduce the iron K band, leaving significant residuals. To account for this, we include a Gaussian line and report its best-fit parameters in Appendix C.

Scattered component: representing the fraction of the intrinsic AGN power-law that passes through the torus without

interacting or interacting elastically, a few percent or less, and primarily arising from non-variable scattered emission and recombination from the NLR, which decreases with increasing column density (e.g., S. Bianchi et al. 2006; J. McKaig et al. 2023; C. Ricci et al. 2017).

In XSPEC, it is parameterized as $F_s * \text{cutoffpl}$, where F_s is a multiplicative constant accounting for the scattered fraction and cutoffpl is the primary power-law component. During the fit, we assume that the photon index (Γ) and torus geometry parameters (see Sects. 3.2, 3.3, and 3.4 for details) do not vary on timescales up to ~ 20 years. Thus, they are linked across epochs to reduce uncertainties (see S. Marchesi et al. 2022). While continuum flux may vary between epochs, the corresponding changes in Eddington ratio (λ_{Edd}) are small enough that they are not expected to significantly affect the intrinsic continuum shape or Γ . This first order approximation is not valid for MCG-03-34-064 and thus, we fit each observation separately (see Sect. 8 for the detailed analysis). In all fits, the high-energy cutoff is fixed to 300 keV.

In summary, the model can be written in XSPEC as:

phabs * (Soft Model + C_{AGN} * (Torus Model + F_s * cutoffpl).

Best-fit results and spectra are presented in Sect. 5 and Appendix B. In Appendix C, we report and discuss whether modifications are applied to the standard fitting methodology.

3.2. Torus model: UXCLUMPY

UXCLUMPY²² (J. Buchner et al. 2019) is a clumpy torus model designed to reproduce the observed distribution of column densities and the frequency of cloud eclipsing events in AGN. Unlike smooth-density torus models, UXCLUMPY accounts for the clumpy nature of the obscurer by assuming clouds distributed on circular Keplerian orbits with random orientations. Their angular dispersion is parameterized by σ_{tor} , which regulates how widely the clouds spread around the equatorial plane.

A key feature of UXCLUMPY is the inclusion of an optional inner Compton-thick reflector, characterized by the parameter CTKcover , which represents the covering factor of this material. Given its nature, in the best-fit tables (Tables B.2 to B.11), this parameter will be presented together with the covering factors as C_f . However, due to its distinct physical origin, it cannot be directly compared with the covering factors derived from the other torus models. This inner component is motivated by the need to reproduce strong reflection features in AGN spectra and can be interpreted as part of the dust-free broad-line region or the inner torus wall. Together, σ_{tor} , CTKcover , and the inclination angle θ allow the model

²² <https://github.com/JohannesBuchner/xars/blob/master/doc/uxclumpy.rst>

to probe a wide range of line-of-sight hydrogen column densities $20 \leq \text{Log}(N_{\text{H,LoS}} / \text{cm}^{-2}) \leq 26$.

The two tables of `UXCLUMPY` treat the direct and torus reflection (first table below), and scattering emissions (second table below) self-consistently. The latter represents emission that escapes the torus after undergoing at least one interaction with the medium. In `XSPEC`, the model can be implemented as:

`Torus Model = {uxclumpy.fits} + F_s * {uxclumpy_scattered.fits}`.

3.3. Torus model: `RXTorusD`

`RXTorusD`²³ (S. Paltani & C. Ricci 2017; C. Ricci & S. Paltani 2023) is the first X-ray spectral model that reproduces the emission of AGN considering a dusty gas. In particular, `RXTorusD` incorporates a wide range of physical processes associated with dust, including scattering, near-edge X-ray absorption fine structure, and self-shielding, as well as additional effects such as Rayleigh scattering and scattering on molecular gas.

`RXTorusD` assumes a toroidal homogeneous geometry, allowing a variable covering factor defined as the ratio of the minor to major axes ($C_f = r/R$) that can vary between 0.01 and 1. Meanwhile, the inclination, i.e., viewing angle of the observer, spans 0° - 90° (with $\theta = 0^\circ$ being a face-on AGN). It distinguishes between line-of-sight ($N_{\text{H,LoS}}$) and equatorial ($N_{\text{H,eq}}$) column densities, where $N_{\text{H,LoS}}$ affects the transmitted continuum and $N_{\text{H,eq}}$ determines the intensity of the reprocessed emission, which self-consistently includes reflection and fluorescence.

In this work, we adopt the tables computed for solar metallicity and a dust fraction of 1, thus assuming that all iron atoms are in dust form. In `XSPEC`, the model can be implemented as follows with the first table accounting for the reprocessed components (i.e., reflection and fluorescence) and the second for absorption:

`Torus Model = {RXTorus_rprc.mod} + {RXTorus_cont.mods}*cutoffpl`.

3.4. Torus model: `X-skirtor`

`X-skirtor`²⁴ (Vander Meulen et al., *subm.*) is the first AGN torus model calculated using the X-ray Monte Carlo radiative transfer code `SKIRT` (B. Vander Meulen et al. 2023). It simulates reflection and obscuration by cold atomic gas in a toroidal geometry, with a uniform wedge shape defined by the covering factor ($C_f = 0.25$ - 0.85) and equatorial hydrogen column density ($22 \leq \text{Log}(N_{\text{H,eq}} / \text{cm}^{-2}) \leq 25$), observed at an inclination θ (between 0° and 90°). What sets `X-skirtor` apart is its advanced treatment of X-ray physics

and high spectral resolution. In particular, it accounts for bound-electron scattering by incorporating the momentum distribution of electrons bound to neutral atoms. Covering a broad energy range (0.2–200 keV) and providing a detailed description of reprocessed emission, `X-skirtor` is among the most advanced AGN torus models currently available. The model treats both transmitted and reprocessed emission using separate tables for the direct continuum (second table below) and the reprocessed component (first table below), in `XSPEC`:

`Torus Model = {xskirtor_smooth_ccd_rpc.mod} + {xskirtor_smooth_ccd_ext.mods}*cutoffpl`.

In Table 2, we report a summary of the parameters fitted during the analysis of the three torus models.

Table 2. Summary of the torus-model parameters.

Geometry	Parameter	Meaning
UXCLUMPY		
Clumpy	Γ	X-ray photon index
	$N_{\text{H,LoS}}$	Line-of-sight column density
	θ	Viewing angle
	σ_{tor}	Angular width of the clouds distribution
	<code>CTKcover</code>	Covering factor inner CTK reflector
RXTorusD		
Smooth toroidal circle	Γ	X-ray photon index
	$N_{\text{H,LoS}}$	Line-of-sight column density
	$N_{\text{H,eq}}$	Equatorial column density
	θ	Viewing angle
	r/R	Inner-to-outer radius ratio
X-skirtor		
Smooth toroidal wedge	Γ	X-ray photon index
	$N_{\text{H,LoS}}$	Line-of-sight column density
	$N_{\text{H,eq}}$	Equatorial column density
	θ	Viewing angle
	C_f	Covering factor

NOTE— For a detailed discussion of the geometries and assumptions of the torus models adopted here, we refer to the corresponding papers.

`UXCLUMPY`: M. Nenkova et al. (2008b); J. Buchner et al. (2019), `RXTorusD`: S. Paltani & C. Ricci (2017); C. Ricci & S. Paltani (2023), and `X-skirtor`: B. Vander Meulen et al. (2023); Vander Meulen et al., *subm.*

3.5. Variability classification

Sources in this work were originally classified as non-variable, based on only two observations. To assess whether incorporating an additional 2 to 7 observations (depending on the AGN) alters this classification, we derive the $N_{\text{H,LoS}}$ for each available observation and assess whether it changes significantly across epochs. As a first step, we check whether

²³ <https://www.astro.unige.ch/reflex/xspec-models>

²⁴ <https://github.com/BertVdM/xskirtor>

the $N_{\text{H,LoS}}$ values from different observations are consistent within their uncertainties. For example, if the value obtained in the first observation lies within the uncertainty range of the second, and both of these are also consistent with the third, then the source is indeed non-variable. If, instead, at least one $N_{\text{H,LoS}}$ measurement falls outside the uncertainties of the others, variability is suggested. Subsequently, to statistically evaluate variability, we apply the two independent methods defined in II.

- **Reduced statistic method**

In this approach, the reduced χ^2 of the best-fit model (which allows $N_{\text{H,LoS}}$ and intrinsic flux variability) is compared to constrained models under three assumptions: 1) no variability at all, 2) only $N_{\text{H,LoS}}$ variability, 3) only intrinsic flux variability. A *tension parameter* (T) is then defined as:

$$T = \frac{|1 - \chi_{\text{red}}^2|}{\sigma},$$

where $\sigma = \frac{1}{\sqrt{N}}$ and N is the number of degrees of freedom. A source is classified as “Variable” if the best-fit model including $N_{\text{H,LoS}}$ variability has $T < 3$, while the fit assuming non-variability yields $T > 5$. If both models yield $T < 3$, the source is considered “Non-variable”, since $N_{\text{H,LoS}}$ variability is not required. When the torus models disagree or classifications are inconsistent, the source is labeled “Undetermined”. In cases where the C-statistic is applied, we consider reduced statistic instead of χ_{red}^2 . We note that the interpretation is less straightforward since the distribution does not strictly follow a Gaussian function. This test therefore provides a way to evaluate whether the best-fit model is statistically satisfactory and whether an equally good fit could be obtained without invoking $N_{\text{H,LoS}}$ variability. In practice, this helps in robustly assessing the number of variable sources.

- **p-value method**

This method tests the null hypothesis that no $N_{\text{H,LoS}}$ variability exists across observations of the same source. By comparing the best-fit $N_{\text{H,LoS}}$ values²⁵ at different epochs with their average, we can define:

$$\chi^2 = \sum_{i=1}^n \frac{(N_{\text{H,LoS},i} - \langle N_{\text{H,LoS}} \rangle)^2}{\delta(N_{\text{H,LoS},i})^2}$$

where $N_{\text{H,LoS},i}$ is the line-of-sight column density at epoch i , $\langle N_{\text{H,LoS}} \rangle$ is the mean value across epochs, and

$\delta(N_{\text{H,LoS},i})$ is the measurement uncertainty (using asymmetric errors when appropriate). The χ^2 is then converted into a *p-value*. If the p-value is ≤ 0.01 for all the three torus models, the AGN is classified as “Variable”. If the p-value is above 0.01 for all models, it is considered “Non-variable”. Disagreement among the models (some above, some below the threshold) leads to an “Undetermined” classification.

In Appendix C, we report the classification of the sources across different wavelength bands (if the information is available in the literature), and we discuss the adopted classification for Mrk 1498 and IC 5063. The *tension* and *p-value* results for each AGN are reported at the end of Tables B.2 – B.11.

4. TORUS MODEL COMPARISON

In this section, we compare the results from the three different models. Since RXTorusD and X-skirtor are newly developed compared to UXCLUMPY, a direct comparison is important to assess their mutual consistency and reliability. To provide a preliminary assessment of how model estimates vary across different observations of the same source and to highlight potential discrepancies between models, Fig. 2 presents a comparison of the $N_{\text{H,LoS}}$ values derived from the three models for each observation in our AGN sample. Each panel compares a pair of models, displaying all sources and epochs together with their corresponding uncertainties. From the scatter plots, the best-fit values show a strong, statistically significant correlation and overall good agreement among the models. From a visual inspection, RXTorusD appears to yield slightly higher $N_{\text{H,LoS}}$ at low column densities, while UXCLUMPY and X-skirtor lie closer to the 1:1 line. This difference could potentially be related to the inclusion of dust in the former torus model, which is not accounted for in the other two. Statistically, however, the differences between all three models are below 1σ , confirming consistency with the 1:1 relation. From the visual inspection of Fig. 2, we find that, for most sources, the different observations cluster within a similar range of $N_{\text{H,LoS}}$ values. The sole exception is UGC 3752, consistent with our classification of this source as a candidate changing-look/obscuration AGN (see Sect. 5.1). We quantified these correlations through the Spearman test, whose rank and p-value evaluate the strength and significance of monotonic trends between parameters. To properly account for asymmetric uncertainties, we adopted the perturbation method described in V. E. Gianoli et al. (2024), which also allows estimating the linear regressions and corresponding uncertainty between model pairs. We report in Fig. 2 the linear regression best-fit parameters, Log(NHP), and intrinsic scatter for each of the model pair.

²⁵ We note that the $N_{\text{H,LoS}}$ values adopted here are taken from the best-fit model accounting for both column density and intrinsic flux variability, and thus are independent of the assumptions made in the tension test.

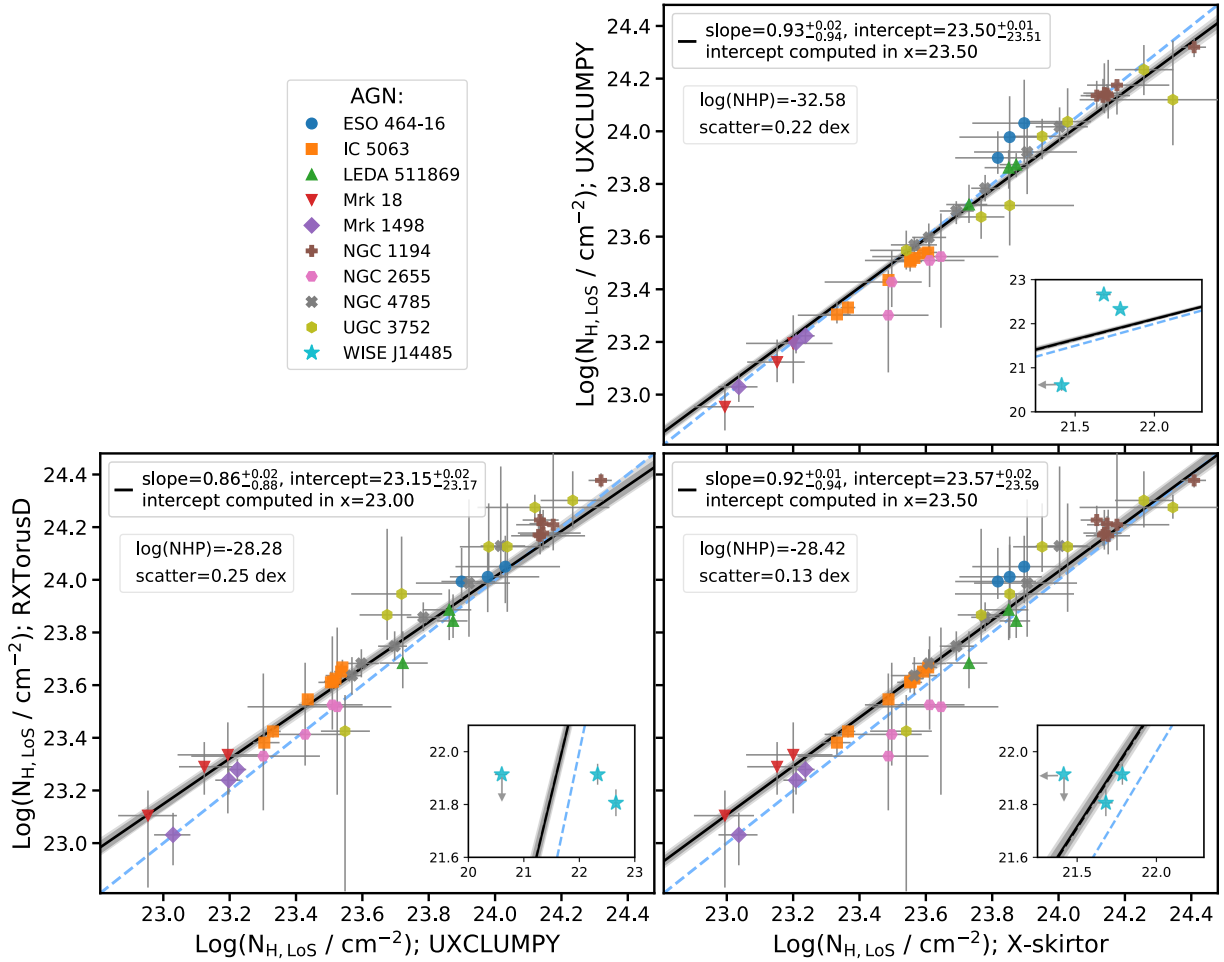


Figure 2. $N_{\text{H,LoS}}$ comparison: $N_{\text{H,LoS}}$ best-fit values derived from RXTorusD, UXCLUMPY, and X-skirtor models for our AGN sub-sample. Insets highlight the low-density regime, populated by WISE J144850, whose *NuSTAR* observation shows upper limits (gray arrows) in the RXTorusD and X-skirtor models. The dashed light blue lines correspond to $y = x$. The solid black lines represent the best-fitting linear correlation and the dark and light gray shadowed areas indicate the 68% and 90% confidence bands, respectively. In the legend, we report the best-fit coefficients, log NHP, and the intrinsic scatters for the correlations. The different models generally provide consistent $N_{\text{H,LoS}}$ estimates for most observations, with the largest deviations occurring in sources with peculiar obscuration behavior (UGC 3752) or in the low-obscuration regime (WISE J144850).

To further assess the consistency of the models within each variability class and to obtain an overall view of their behavior, we compute the pairwise normalized differences:

$$Z = \frac{|m_1 - m_2|}{\sqrt{\sigma_1^2 + \sigma_2^2}},$$

where m_i and σ_i are the median and uncertainty estimated. We define two model estimates as inconsistent when $Z \geq 2.6$, which corresponds approximately to a probability threshold of 0.01 for a Gaussian distribution, consistent with the significance criterion adopted throughout this work. Concerning the median values of the $N_{\text{H,LoS}}$ for each source and model, we find that eight of the ten AGN show mutual agreement among all models, suggesting that the choice of torus model has little impact on the derived obscuration parameters. Only

IC 5063 and WISE J14485 display significant inter-model discrepancies, indicating that their derived $N_{\text{H,LoS}}$ values depend more strongly on the assumed torus geometry. In particular, IC 5063 median column densities differ by up to $\sim 4\sigma$ (maximum $Z = 4.11$). The value derived by adopting RXTorusD is significantly higher than both alternative models, and the strongest discrepancy occurs between UXCLUMPY and RXTorusD, with a median difference of 8.53. Interestingly, if we consider other spectral parameters (i.e., the photon index and normalization, and thus the AGN luminosity), UXCLUMPY appears most discrepant relative to X-skirtor and RXTorusD. This suggests that IC 5063 is a complex source, possibly affected by multiple factors (e.g., spectral degeneracies or partial jet contribution; see A. Travascio et al. 2021, for a discussion on the jet emission), and that different combinations of model parameters can reproduce the ob-

served spectrum, leading to the observed spread in $N_{\text{H,LoS}}$. Interestingly, from Fig. 2, Mrk 18 appears to deviate from the 1:1 line to a similar extent as IC 5063, suggesting a comparable discrepancy. However, the Z-test does not flag Mrk 18 as significantly discrepant. This is likely due to the larger uncertainties in the $N_{\text{H,LoS}}$ measurements for Mrk 18, which effectively encompass the 1:1 relation and reduce the significance of any apparent offset. Even more significant model-to-model discrepancies are present in WISE J14485, with $Z = 14.86$. Here, UXCLUMPY yields a significantly larger median $N_{\text{H,LoS}}$. However, we note that during the fitting process, only UXCLUMPY was able to constrain the $N_{\text{H,LoS}}$ for the third observation (taken with *NuSTAR*), whereas the other two models yielded only upper limits. This AGN was observed in a weakly absorbed state, with inferred obscuration ranging from 0.43 to $5 \times 10^{22} \text{ cm}^{-2}$ (when constrained). Hence, this outcome likely reflects the challenge of modeling sources in a low-obscuration regime with X-skirtor and RXTorusD torus models.

In addition, we applied the same analysis to the other key spectral and geometrical parameters constrained by the three torus models (photon index Γ , fraction of scattered continuum F_s , and torus covering factor C_f (considering only RXTorusD and X-skirtor results, see Sect. 3.2), inclination angle θ , and equatorial column density $N_{\text{H,eq}}$). For Γ , we find overall good agreement among the models for most sources, with significant discrepancies emerging only for IC 5063 for which a higher value is inferred with UXCLUMPY, suggesting that differences in the treatment of the transmitted continuum and scattering components can affect the spectral slope. A stronger inter-model tension appears for the covering factor. Here, half of the sample displays statistically significant discrepancies. The inclination angle is often only weakly constrained. NGC 1194 shows the higher significant difference, with RXTorusD preferring lower inclination angles than the other two models. These mismatches likely reflect the fundamentally different geometric assumptions encoded in each torus framework: UXCLUMPY prescribes a clumpy medium, whereas X-skirtor and RXTorusD impose smooth or quasi-smooth angular density distributions. As a result, the same spectra can be reproduced with very different combinations of covering factor, cloud distribution, and equatorial opacity, leading to large model-dependent shifts.

IC 5063 and WISE J144850 also show strong model-to-model inconsistencies in the scattered-fraction values. Additionally, a significant difference is also present in NGC 4785, for which UXCLUMPY results to be higher than X-skirtor and RXTorusD values, which instead are in agreement. Differences in the equatorial column density are seen in LEDA 511869, Mrk 18, NGC 1194, NGC 2655, and UGC 3752. In the cases of LEDA 511869, NGC 2655, and UGC 3752 the difference is between 0.5 and 1.5. While for

Mrk 18 and NGC 1194, the difference is small, less than 4% and 12%, respectively.

Overall, while the line-of-sight absorption appears robust against torus-model choice for the majority of sources, several secondary parameters are significantly model dependent. This highlights the importance of interpreting such inferred torus properties in the context of the specific geometrical assumptions of each model.

5. X-RAY AND VARIABILITY CLASSIFICATIONS

In the following sections, we discuss the results obtained for 10 of the 11 AGN of the sub-sample. Given that MCG-03-34-064 cannot be fit under our assumptions (constant photon index and torus geometry) and exhibits significant residuals in the soft X-rays and Fe K band, it requires a separate fitting procedure and is thus excluded from the statistical and physical analysis below. A complete discussion of the fitting procedure and results for MCG-03-34-064 is provided separately in Sect. 8.

5.1. Compton-thin and -thick classification

Considering the results of our fitting procedure, reported in Tables B.2-B.11, we classify 9 out of 10 AGN as Compton-thin, while NGC 1194 is confirmed as Compton-thick (in agreement with previous studies; e.g., C. Y. Kuo et al. 2011; P. Severgnini et al. 2012; S. Marchesi et al. 2018; T. J. Turner et al. 2020). We adopt a conservative classification based on overall behavior across epochs and models, rather than on isolated upper limits. In particular, UGC 3752 is identified as a candidate changing-obscuration AGN, with the line-of-sight column density exceeding the Compton-thick threshold ($N_{\text{H,LoS}} > 1.5 \times 10^{24} \text{ cm}^{-2}$) in multiple epochs and models (see Table B.10). ESO 464-G016 and NGC 4785 remain classified as Compton-thin as their $N_{\text{H,LoS}}$ show upper limits in the CTK regime only in a single observation and model (see Tables B.2 and B.9, respectively). NGC 1194 shows evidence for possible transitions between Compton-thin and Compton-thick states on timescales of roughly 1–2 years, although the uncertainties remain consistent with a persistently CTK classification in some models (see Table B.7 and Fig. 12 panel b). NGC 1194 is currently being monitored with *NuSTAR*+XMM (proposal 11159, PI: S. Marchesi) to study weeks-to-months $N_{\text{H,LoS}}$ variability, probing the obscuring medium structure and AGN feeding/feedback processes. We report the X-ray classification in Table 1. Further details on the individual sources of the sample are provided in Appendix C.

5.2. $N_{\text{H,LoS}}$ and intrinsic flux variability classification

To assess the variability classification of each AGN (see Sect. 3.5), we first compare the $N_{\text{H,LoS}}$ values from individual observations to evaluate whether they are consistent within

Table 3. Classification summary.

(1)	(2)	(3)	(4)		(5)		(6)		(7)		(8)
Source	# obs	1st order	X-skirtor	RXTorusD	UXCLUMPY	Comparison	Is $N_{\text{H,LoS}}$ variable?				
			T	p-value	T	p-value	T	p-value	T	p-value	
ESO 464-G016	3	NV	U	NV	U	NV	NV	NV	?		?
LEDA 511869	3	NV	NV	NV	NV	NV	NV	NV			
Mrk 1498	3	V	V	V	V*	V	V*	V			
WISE J144850.99-400845.6	3	U*	U	V	U	V	U	V	?		?
Mrk 18	4	NV	NV	NV	NV	NV	U	NV			
NGC 2655	6	NV	NV	NV	NV	NV	NV	NV			
NGC 4785	7	V	V	V	V	V	V	V			
UGC 3752	7	V	V	V	V	V	V	V			
IC 5063	8	V	V	V	U*	V	U*	V			
NGC 1194	8	V	V	V	V	V	V	V			
MCG-03-34-064 +	9	V	/	/	/	/	/	/	/	/	/

NOTE—*Columns:* 1) Number of observations; 2) First-order variability classification, based on whether $N_{\text{H,LoS}}$ values from different observations overlap within uncertainties; 3–6) classifications from the two statistical tests, reported separately for each of the three adopted models; 7) variability summary across models for each test; 8) final classification combining the results of the two tests (T and p-value) reported in column 7. Gray with a question mark (or “U”), red (or “NV”), and green (or “V”) indicate “Undetermined”, “Non-variable”, and “Variable”, respectively.

* see Appendix C with notes on each AGN.

+ refer to Sect. 8 for the classification of the source.

their uncertainties. The results are reported in Table 3, column 3. For ESO 464-G016, LEDA 511869, Mrk 18, and NGC 2655 (4 out of 10 AGN, $\sim 40\%$) the best-fit $N_{\text{H,LoS}}$ values from different epochs lie within uncertainties, indicating that no significant variability can be inferred. In contrast, for Mrk 1498, NGC 4785, UGC 3752, IC 5063, and NGC 1194 (5 out of 10 AGN, $\sim 50\%$), significant variability in $N_{\text{H,LoS}}$ on timescales of days, months, and/or years is observed. Thus, identifying these AGN as good candidates for variable sources. WISE J144850.99-400845.6 (hereafter “WISE J144850”) shows an intermediate behavior, as only upper limits on $N_{\text{H,LoS}}$ could be derived from the *NuSTAR* observation when adopting X-skirtor and RXTorusD models.

We then statistically classify each AGN as $N_{\text{H,LoS}}$ Variable or Non-variable using the two tests described in Sect. 3.5. For each source, the *T* and *p-value* tests are applied to the best-fit results from the three spectral models, X-skirtor, RXTorusD, and UXCLUMPY, yielding six determinations in total. The results are reported in Table 3, columns 4–6. For each test independently, if at least two of the three model-based determinations agree on Variable or Non-variable (V/NV), that classification is assigned to the corresponding comparison column (column 7); otherwise, the result is marked as Undetermined (U). The final classification com-

binates the two test-comparison results: if both agree on V or NV, the AGN is assigned that class; if they disagree or at least one is U, the final class is Undetermined (column 8). This procedure yields 2 out of 10 Undetermined AGN (ESO 464-G016 and WISE J144850), 3 out of 10 Non-variable AGN in $N_{\text{H,LoS}}$ (LEDA 511869, Mrk 18, and NGC 2655), and 5 out of 10 Variable AGN in $N_{\text{H,LoS}}$ (Mrk 1498, NGC 4785, UGC 3752, IC 5063, and NGC 1194). Overall, for 9/10 sources, the statistical tests confirm the first-order classification. The only discrepancy is ESO 464-G016, classified as NV by the *p-value* test and U by the *tension* test, leading to a final Undetermined classification (see Table 3). Finally, most sources in the sample exhibit intrinsic flux variability. When neither $N_{\text{H,LoS}}$ nor intrinsic flux variability is imposed, 7 out of 10 AGN show significantly worse best-fits (see the “No variability” tests in Appendix B). However, for ESO 464-G016, LEDA 511869, and NGC 4785, the tensions remain comparable across hypotheses or reveal degeneracies between flux and $N_{\text{H,LoS}}$ variability, preventing a firm assessment (see Appendix C for more details).

These results highlight a key aspect of our study: the initial classification, based only on two observations, one in the soft X-ray band and one in the hard X-ray band, is insufficient to properly assess variability. In addition, we note that, out of the 22 AGN for which X. Zhao et al. (2021) consid-

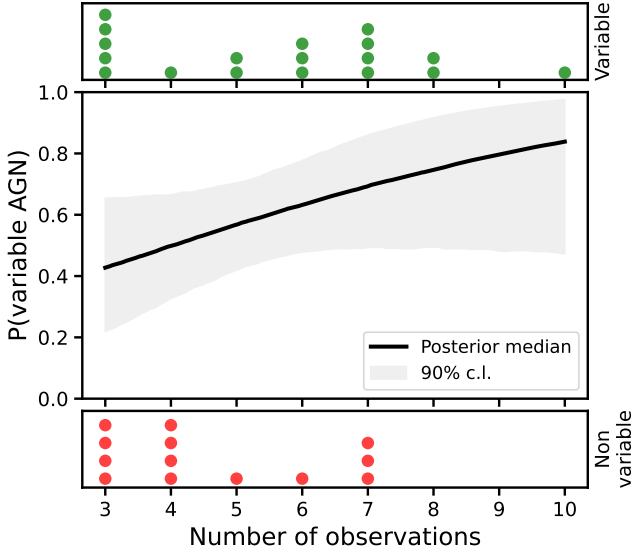


Figure 3. Probability of detecting $N_{\text{H,LoS}}$ variability as a function of the number of available X-ray observations, considering the 10 AGN analyzed here and the sources analyzed by I-V. Green and red points show, respectively, AGN classified as Variable and Non-variable. The black solid line represents the posterior median of a Bayesian logistic regression fitted to the binary variability outcomes, and the gray shaded regions show the corresponding 90% confidence bands. The posterior median probability increases with N_{obs} , with average slopes of 0.06 and 0.05 per observation over the $N_{\text{obs}} = 3-5$ and $N_{\text{obs}} = 5-10$ ranges, respectively. The increase is visually most apparent around $N_{\text{obs}} \sim 5-6$, indicating that denser multi-epoch X-ray coverage improves the detectability of obscuration changes.

ered simultaneous observations (see Sect. 2), our sample includes three: NGC 4785, UGC 3752, and MCG-03-34-064. While we refer to Sect. 8 for MCG-03-34-064, our analysis reclassifies NGC 4785 and UGC 3752 as Variable sources. This reflects the larger multi-epoch dataset analyzed here and highlights the need to account for spectral variability, both in $N_{\text{H,LoS}}$ and intrinsic flux.

Consistent with this interpretation, the detection of $N_{\text{H,LoS}}$ variability appears to depend strongly on observational sampling. In our sample, all targets with at least seven observations are found to be $N_{\text{H,LoS}}$ variable, as shown in Table 3. The only exception is Mrk 1498, which shows $N_{\text{H,LoS}}$ variability despite having only three observations. However, this threshold may differ from source to source and may depend on whether the variability occurs on short or long timescales. To statistically test whether and how the probability of detecting $N_{\text{H,LoS}}$ variability depends on the number of available X-ray observations, we model variability detection as a binary outcome using a Bayesian logistic regression (R. McElreath 2020). For each AGN, variability is therefore treated as a simple yes/no outcome, i.e., either detected or not detected, and we infer the probability of detecting variability

for a given number of observations, $P(\text{variable} | N_{\text{obs}})$. Because this probability must lie between 0 and 1, we describe its dependence on N_{obs} using a logistic function. This provides a continuous empirical description of how the likelihood of detecting variability changes with observational sampling, rather than imposing an arbitrary threshold in N_{obs} . We adopt a Bayesian framework to account for the small sample size and to infer a posterior distribution of plausible probability curves (instead of a single best-fitting curve). We use a prior that does not favor any particular probability, so that the inferred relation is driven primarily by the observed distribution of Variable and Non-variable sources. We emphasize that this analysis probes the detectability of variability given a finite number of observations, rather than the intrinsic fraction of variable AGN. Since variability is encoded as detected (Variable source) or not detected (Non-variable source), Undetermined sources (i.e., sources with ambiguous classifications) are excluded from this analysis. Given the limited size of our sub-sample, we apply the Bayesian analysis to the expanded sample, combining the AGN analyzed in this work with the pre-selected variable sample (I-V). The posterior median relation for the expanded sample is shown in Fig. 3. AGN with more observations are increasingly dominated by Variable sources, whereas sources with fewer observations include a mixed population of Variable and Non-variable AGN. This increase is visually most apparent around $N_{\text{obs}} \sim 5-6$. We note that, although the posterior median trend is positive with the probability for a positive slope of $P(\text{slope} > 0) = 0.91$, the uncertainty on the slope remains large. Therefore, while the data suggest an increasing trend, this result should be regarded as tentative and may change as more AGN are analyzed.

A similar trend is reported by I. S. Cox et al. (2025), who performed a systematic search for $N_{\text{H,LoS}}$ variability in nearby AGN using the *Chandra* archive, further supporting the evidence that expanded multi-epoch coverage enhances our ability to detect obscuration changes. This consistency suggests that the dependence on observational sampling reflects a genuine behavior of multi-epoch X-ray AGN data, rather than a feature specific to our classification method. Quantifying this dependence therefore provides an empirical benchmark for variability studies and clumpy-obscurer models.

6. $\Delta N_{\text{H,LoS}}$ TIME EVOLUTION

In this section, we discuss the derived $N_{\text{H,LoS}}$ and the epoch-to-epoch changes in column density ($\Delta N_{\text{H,LoS}}$) as a function of time. We computed the epoch-to-epoch changes in column density as $\Delta N_{\text{H,LoS}} = N_{\text{H,LoS}}^{i+1} - N_{\text{H,LoS}}^i$, and propagated the asymmetric uncertainties via quadrature of the appropriate adjacent errors. An important aspect of interpreting absorption variability is the characteristic timescale of

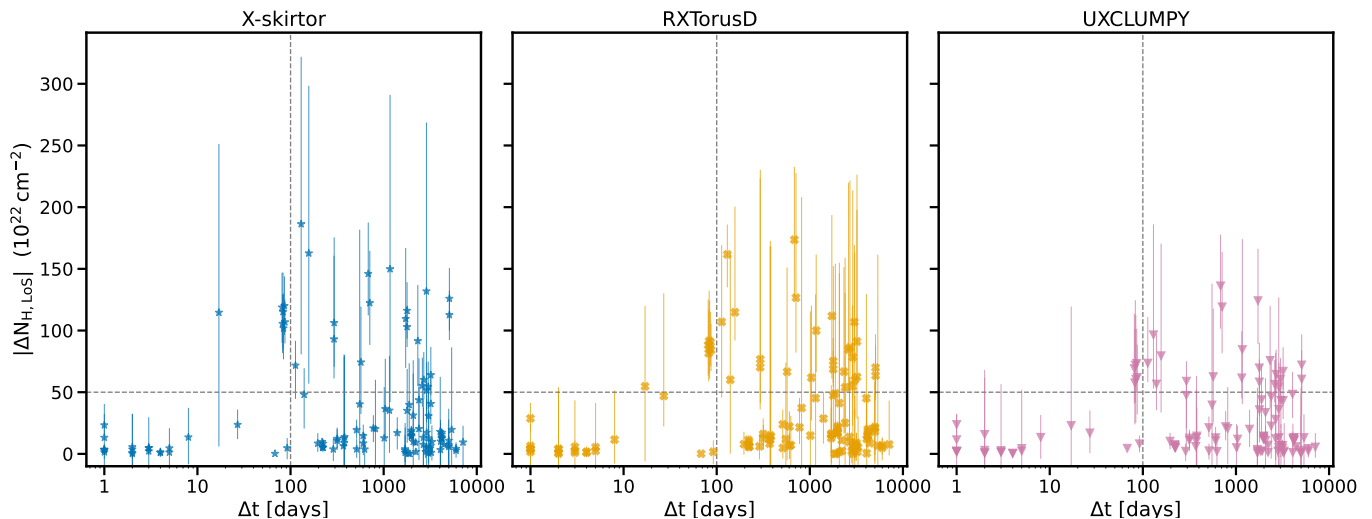


Figure 4. Distribution of $\Delta N_{\text{H,LoS}}$ as a function of time interval (Δt) for the sample. The amplitude of $N_{\text{H,LoS}}$ variability is timescale-dependent: small variations in $\Delta N_{\text{H,LoS}}$ are observed at all timescales, whereas large changes ($\geq 5 \times 10^{23} \text{ cm}^{-2}$), occur predominantly at long Δt (> 100 days). The dashed lines show the thresholds adopted for changes in the column density (horizontal line) and time intervals (vertical line), see II. The blue, yellow, and pink sub-panels correspond to X-skirtor, RXTorusD, and UXCLUMPY, respectively. For all three models, the KS-tests between the short- and long-term distributions confirm a significant difference, with $\text{Log}(\text{NHP}) = -2.97$ for X-skirtor; $\text{Log}(\text{NHP}) = -4.39$ for RXTorusD; and $\text{Log}(\text{NHP}) = -2.06$ for UXCLUMPY.

the change. In a Keplerian potential, short-timescale (i.e., hours to weeks) variations are expected to originate from compact, rapidly moving clouds located at radii comparable to, or smaller than, the BLR, whereas variability on longer timescales (i.e., months to years) is associated with material located at larger radii, such as torus clumps (e.g., G. Risaliti et al. 2002; A. G. Markowitz et al. 2014). In general, large $\Delta N_{\text{H,LoS}}$ events imply denser or more extended structures, while small changes can indicate partially covering clouds or more distant material (see H. Netzer 2015, for a review).

A useful way to visualize this behavior is to plot the variation in column density as a function of the timescale normalized by the black hole mass, $\Delta t/M_{\text{BH}}$. Given that dynamical timescales scale with the mass, this normalization allows different AGN to be compared. For each of the ten AGN in our sample, Appendix B shows the time evolution of $N_{\text{H,LoS}}$ and the plots with $\Delta N_{\text{H,LoS}}$ versus $\Delta t/M_{\text{BH}}$ (middle and lower panels, respectively, of Figs. 7–16). To provide a qualitative check on the possible physical scale of the absorber, we perform a simple cloud-crossing test under the assumptions of Keplerian motion and coherent obscuring structures. For each pair of consecutive epochs, we compared the observed variability timescale with the characteristic timescales expected for BLR- and torus-scale absorbers. The results suggest that the observed variability is not associated with a single characteristic scale (i.e., BLR-scale or torus-scale material). However, this interpretation relies on simplifying assumptions that may not hold in a clumpy, turbulent, or multi-phase circumnuclear medium. In particular, the absorber may not consist of long-lived individual clouds

crossing the line of sight, and non-Keplerian motions such as turbulence, inflows, or outflows may also contribute (e.g., D. Wittor & M. Gaspari 2020). Moreover, given that the AGN are not continuously monitored, our conclusions are necessarily limited by the available sampling. We therefore interpret the inferred locations only as indicative and as a qualitative consistency check indicating that both compact inner absorbers and larger-scale circumnuclear material could contribute to the observed variability.

In II and III, the authors report that large changes in LoS column density (i.e., $\Delta N_{\text{H,LoS}} \geq 5 \times 10^{23} \text{ cm}^{-2}$) are preferentially associated with longer time intervals, while smaller variations occur across all timescales. To investigate this, we consider the computed $\Delta N_{\text{H,LoS}}$ (between all epochs for each source and model) as a function of the difference in time for our sample. The results are shown in Fig. 4 (left panel for X-skirtor, middle panel for RXTorusD, and right panel for UXCLUMPY), where the time intervals are divided into short ($\Delta t < 100$ days) and long ($\Delta t > 100$ days) epochs. We observe that small changes in $N_{\text{H,LoS}}$ are present at all timescales, whereas large variations occur only over longer time separations also for our sample. We run KS tests between the short- and long-term distributions, confirming significant differences between them (X-skirtor: $\text{Log}(\text{NHP}) = -2.97$; RXTorusD: $\text{Log}(\text{NHP}) = -4.39$; UXCLUMPY: $\text{Log}(\text{NHP}) = -2.06$). Depending on the size and distance of the absorbing clouds, this result could have different interpretations. For extended clouds, it may reflect a density profile, with density increasing toward the cloud centers, as also inferred by II. Alternatively, if the clouds are roughly uniform, short-term

observations would sample the same cloud, while longer intervals between observations could map a different cloud, resulting in a markedly different column density and, consequently, a larger $\Delta N_{\text{H,LoS}}$. A third interpretation, motivated by hydrodynamical simulations, suggests that the dominant structures are extended cloud or filament bundles shaped by turbulence, collisions, and shear (e.g., [M. Gaspari et al. 2017, 2020](#)). A further possibility is that the line of sight intersects multiple clouds spanning a range of scales and velocities. In this picture, slow column density variations from a large-scale structure (e.g., the torus) are modulated by rapid fluctuations from smaller, faster inner clouds. Alignment of several components would temporarily increase the $N_{\text{H,LoS}}$, producing short-timescale variability superimposed on longer-term changes. We note, however, that our sample is biased towards longer timescales as those in [II](#) and [III](#). In particular, although short intervals ($\Delta t < 100$ days) are present in several sources (NGC 4785, UGC 3752, IC 5063, NGC 1194, Mrk 18, NGC 2655, ESO 464-G016, and WISE J144850), the majority of intervals (77%) are long ($\Delta t > 100$ days). Adopting a different methodology, i.e., a population-based approach to identify $N_{\text{H,LoS}}$ variability, [I. S. Cox et al. \(2025\)](#) independently reinforce our results and those of [II](#); [III](#). In particular, the authors assess variability through a χ^2 statistic computed between spectral pairs as a function of time separation, rather than by directly measuring $\Delta N_{\text{H,LoS}}$. By dividing the sample into short and long timescales (adopting the same Δt threshold as used here), they find that the fraction of pairs flagged as variable increases from $\sim 10\%$ at short timescales to $\sim 24\%$ at long timescales. Although this method does not allow the variability amplitude to be directly quantified, since the χ^2 statistic depends on both data quality and intrinsic variability, the conclusion is consistent: large $N_{\text{H,LoS}}$ variability is more prevalent over longer timescales.

6.1. Torus model comparison: $\Delta N_{\text{H,LoS}}$ values

In this section, we expand the torus model comparison by focusing on temporal consistency within each model and agreement across models. To assess the former, we consider the interval $[\Delta N_{\text{H,LoS}}^i - \sigma_{\Delta_i}^-, \Delta N_{\text{H,LoS}}^i + \sigma_{\Delta_i}^+]$. If consecutive $\Delta N_{\text{H,LoS}}$ intervals do not overlap, this indicates a significant change in column density within a single model. To test agreement between models, we computed the difference $\delta_i = \Delta N_{\text{H,LoS}}^{\text{Mod A}} - \Delta N_{\text{H,LoS}}^{\text{Mod B}}$, propagating the associated asymmetric uncertainty. If the resulting interval contains zero, the two models are considered consistent, meaning that any observed difference could plausibly be explained by measurement uncertainties.

We find that all the Non-variable AGN (i.e., LEDA 511869, Mrk 18, and NGC 2655) along with the Undetermined ESO 464-G016, show no between-model discrepancies, although LEDA 511869 exhibits consecutive-

delta non-overlaps with `X-skirtor`. We refrain from discussing WISE J144850, as only `UXCLUMPY` provides well-constrained $N_{\text{H,LoS}}$ values; thus, any observed discrepancy found would reflect differences in constraining power rather than genuine model conflict. By applying the same criteria to the Variable sub-sample, we instead obtain the following results:

- IC 5063, the within-model comparisons reveal that the first two intervals (obs 1-2 vs 2-3, and 2-3 vs 3-4) as well as the last (obs 6-7 vs 7-8) do not overlap for all three models. The remaining consecutive intervals do. Between-model comparisons confirm agreement across nearly all intervals, except for the final interval when comparing `RXTorusD` and `UXCLUMPY` which shows a disagreement;
- Mrk 1498 shows clear non-overlap between individual observations within the same model. However, when considering the full $N_{\text{H,LoS}}$ ranges (including uncertainties) across all models, the $\Delta N_{\text{H,LoS}}$ values remain consistent;
- NGC 1194 exhibits the clearest model-dependent tension. In particular, `X-skirtor` predicts a substantially larger $\Delta N_{\text{H,LoS}}$ for obs 3-4 compared to those derived from `RXTorusD` and `UXCLUMPY`. Overall, this source exhibits the largest number of non-overlapping consecutive intervals among all sources, highlighting strong short-term variability. Between-model comparisons indicate agreement for most intervals; however, clear disagreements appear also for obs 4-5 when comparing `X-skirtor` with `UXCLUMPY`;
- In NGC 4785, the first interval (obs 1–2) does not overlap in any model, indicating a significant change. In contrast, subsequent intervals mostly overlap within each model, except for `UXCLUMPY` where obs 3–4 vs 4–5 show no overlap, suggesting that variations in column density between later observations are generally consistent within the uncertainties of each model;
- UGC 3752 fifth interval (obs 5-6) shows no overlap for any of the three models, while the other intervals overlap within their respective uncertainties.

Regarding the temporal evolution of $\Delta N_{\text{H,LoS}}$ between models, we find that although the absolute values may differ, the overall trend is largely consistent. This evolution as a function of $\Delta t/M_{\text{BH}}$ is shown in the lower panels of [Figs. 7–15](#).

Our analysis shows that between-model differences are rare, occurring in only $\sim 4\%$ of all intervals, and primarily involving `X-skirtor` and `UXCLUMPY`. Discrepancies are

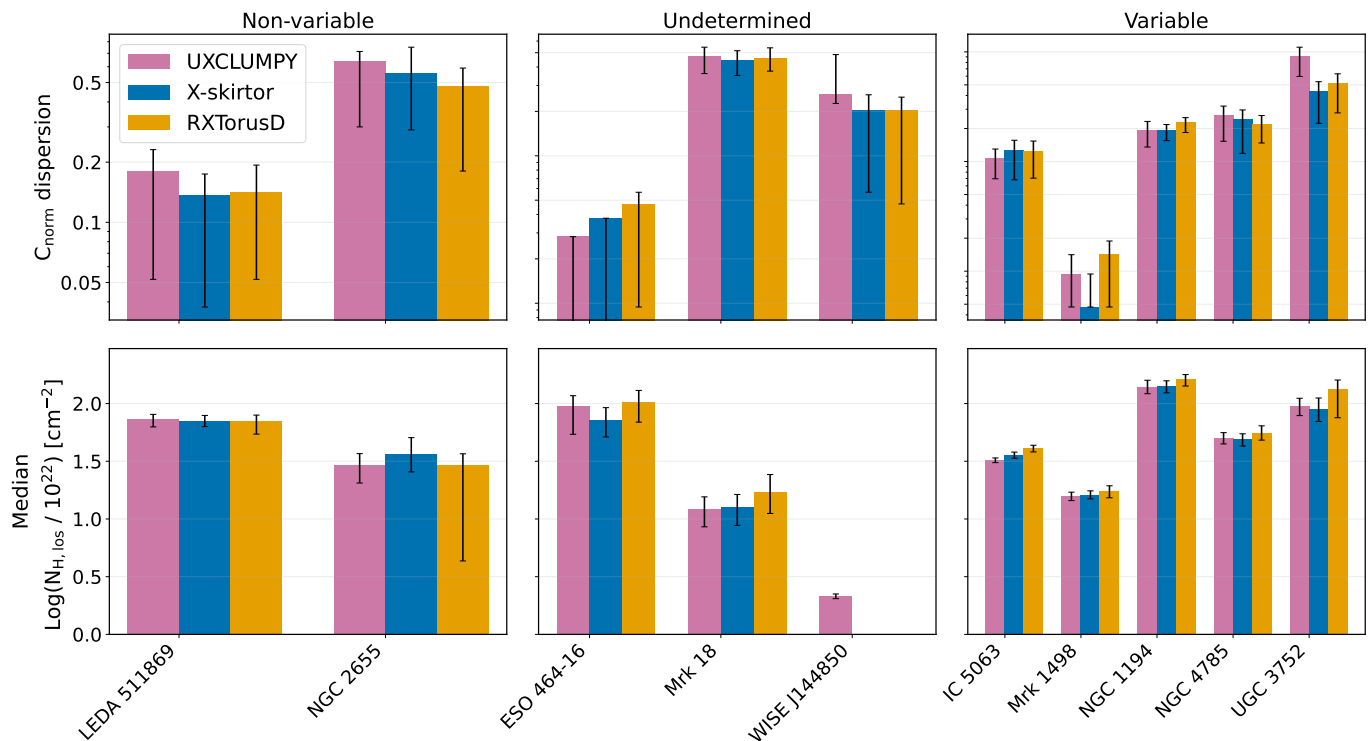


Figure 5. Distributions of the dispersion for the cross-normalization constants and the logarithm of the median $N_{\text{H,LoS}}$ values, grouped by variability class. Results for the three adopted torus models are shown as: UXCLUMPY in pink, X-skirtor in blue, and RXTorusD in yellow, including asymmetric uncertainties at 90% c.l.. *Left panels* present the non-variable, *middle panels* the undetermined, and *right panels* the variable AGN samples. The middle panel of the lower row show only the best-fit result for UXCLUMPY for WISE J14485, as the other two models provide only upper limits. Within the limitations of the current small and heterogeneous sample, the two distributions do not exhibit significant differences among variability classes.

most evident in AGN with strong short-term variability (e.g., NGC 1194), while Non-variable and Undetermined sources generally show agreement across all models. We note, however, that systematic shifts between models could introduce shifts in the $N_{\text{H,LoS}}$ values, so overlapping ranges across all models do not necessarily imply true non-variability. In summary, while the choice of model affects the amplitude of inferred column density variations, the classification of AGN as Variable or Non-variable remains robust, indicating that the observed trends largely reflect intrinsic source behavior rather than systematic biases.

7. STATISTICAL PROPERTIES

Considering the best-fit results of the 10 AGN in our sample, we analyze the statistical properties of the model parameters by examining their distributions and potential correlations.

7.1. Parameter distributions

In the following, we investigate whether the torus (covering factor C_f for RXTorusD and X-skirtor, inclination angle θ , equatorial column density $N_{\text{H,eq}}$, vertical extent of the cloud population σ_{tor} , and line-of-sight column density $N_{\text{H,LoS}}$) and AGN continuum properties (photon index Γ ,

fraction of scattered continuum F_s , and cross-normalization constant) differ among AGN with different variability classifications (i.e., Variable, Non-variable, and Undetermined). The distributions of the parameters are shown in Figs. 5 and 17. For each source and model, we consider the median value across observations for $N_{\text{H,LoS}}$ to provide a robust estimate. Group medians are then computed separately for the three classification sub-samples. Given that the cross-normalization constant represents a relative scaling with respect to the first *Chandra* observation of each AGN, its median value depends on the arbitrary choice of reference epoch. We therefore characterize the cross-normalization using its dispersion, which is independent of the normalization choice and captures the relative spread of the constants across observations. We stress that the present sample is small and heterogeneous, and therefore any comparison among variability classes should be interpreted with caution. Moreover, as discussed above, the probability of identifying variability depends on the number and temporal sampling of the available observations. Consequently, some sources currently classified as Non-variable may be reclassified once additional observations become available.

To test for possible differences among the three variability classes, we adopt the Kruskal-Wallis statistical test (W. H.

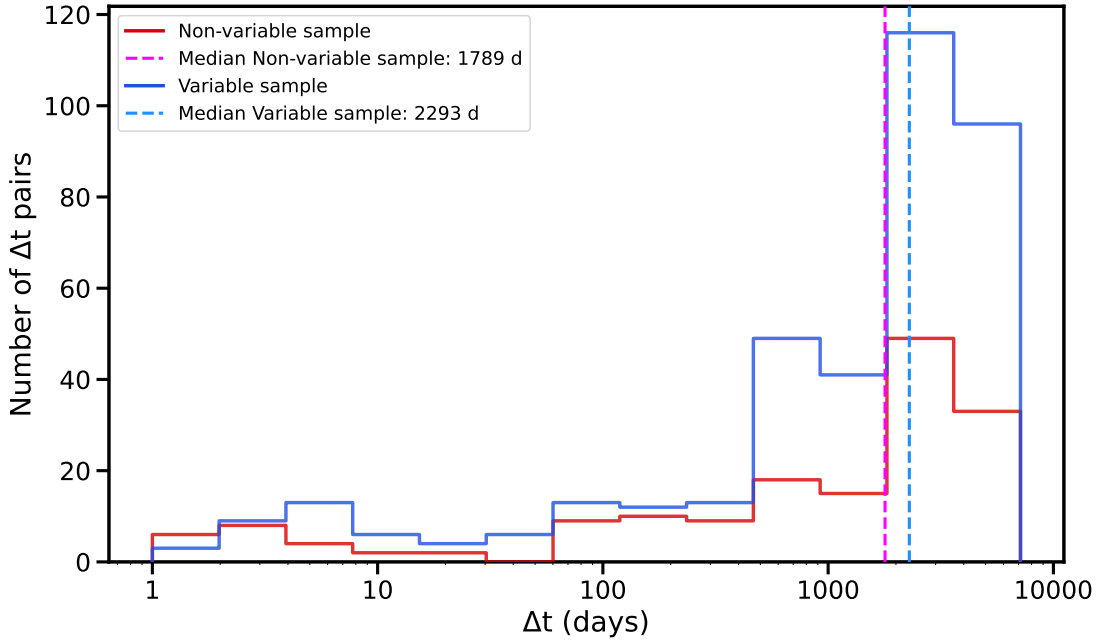


Figure 6. Comparison of Δt distributions between pre-selected non-variable and variable samples. Histograms show the number of Δt pairs in log-scaled bins for the Non-variable sample in red, and the variable sample in blue. The dashed vertical lines indicate the median Δt for each sample (magenta for non-variable, light blue for variable). The KS test performed to quantify whether the two distributions are statistically different yields to a KS statistic of 0.12 and $\text{Log}(\text{NHP}) = -1.22$, indicating no statistically significant difference between the samples, suggesting that differences in variability classification are not primarily driven by different time-interval coverage.

Kruskal & W. A. Wallis 1952), a non-parametric method suitable for small samples that may not follow a Gaussian distributions. To further explore pairwise differences, we apply the KS-test to evaluate whether the two distributions differ in shape. We report the derived medians and p-values for the two tests in Appendix D. Across all parameters, Kruskal-Wallis tests yield non-significant differences ($p > 0.2$, i.e., $\text{Log}(\text{NHP}) = -0.7$, in all cases, the values are reported in Table D.12). The KS tests generally present non-significant p-values (see Table D.12), indicating no statistically significant differences in the distributions of the parameters between the variability classes across the models. These findings suggest that in the current sample and for the majority of parameters, the distributions of torus and continuum properties do not strongly depend on AGN variability classification.

Although no significant differences are found, we note that the photon index shows a decrease from Non-variable to Variable sources across all models, implying marginally harder spectra in the latter class of AGN. In the literature, a well-established trend exists between the X-ray photon index and the Eddington ratio, with higher values typically associated with softer spectra (larger Γ) and lower λ_{Edd} corresponding to harder spectra (smaller Γ ; e.g., N. Brandt & T. Boller 1998; A. Laor 2000; O. Shemmer et al. 2008; G. Risaliti et al. 2009a; M. Brightman et al. 2013). Considering the Edding-

ton ratios of the sources in our sample²⁶, we find that Non-variable AGN have a higher median λ_{Edd} (0.036) than Variable AGN (0.026). This is consistent with the literature trend, suggesting that the harder spectra observed in Variable AGN can be interpreted as a consequence of their lower accretion rates and, correspondingly, reduced radiative cooling of the X-ray emitting corona. A more robust statistical assessment will be possible once the full sample of the project has been analyzed.

In Fig. 6, we show the distribution of the pre-selected non-variable and variable samples in terms of the number of Δt pairs. The pre-selected non-variable sample exhibits a larger number of observations at short time intervals compared to the variable sample. This trend is observed in the sub-sample analyzed in this work (see Sect. 6). However, the KS-test performed on the two distributions confirms that no statistically significant difference is present, $\text{Log}(\text{NHP}) = -1.22$.

7.2. Parameter correlations

We performed a Spearman test (accounting for asymmetric errors) to investigate possible correlation between torus and AGN parameters derived from the best-fit results of each of the three models independently (see Appendixes B.2-B.11

²⁶ The Eddington ratios are reported in Table 1. Values are taken from the BASS sample (M. J. Koss et al. 2022), except for NGC 4785, for which we derive λ_{Edd} using the bolometric luminosity we estimated.

for the best-fits). For $N_{\text{H,LoS}}$ and the cross-normalization constants, we adopt the median value across observations. No significant correlations emerged. However, we note a marginally significant negative correlation between C_f and θ best-fits from *X-skirtor* ($\text{Log}(\text{NHP}) = -1.89^{27}$). A complete correlation analysis including all sources (both initially classified as variable and non-variable) will be presented in a forthcoming paper, once the non-variable sub-sample has been fully analyzed. This will ensure a comprehensive sample with sufficient AGN in each variability class, allowing us to investigate not only correlations across different models but also within variability classes themselves.

8. MCG-03-34-064

In the following sections, we present the X-ray spectral analysis of MCG-03-34-064, a Compton-thin Seyfert 1.8 (M. P. Véron-Cetty & P. Véron 2006) AGN, candidate to host a dual system (A. Trindade Falcão et al. 2024).

8.1. Spectral modeling

To optimize the signal-to-noise ratio and minimize the impact of the instrumental background at high energies, different energy bands are selected for each instrument: 0.5-10 keV for the *XMM-Newton*, 0.8-8 keV for *Chandra*, and 3.5-28 keV for *NuSTAR* data. For this AGN, our first-order approximation (i.e., photon index and torus geometry parameters do not vary over the timescales of the available observations, see Sect. 3.1) is not valid. Indeed, for all three models applied, we obtain poor fits, with $\chi^2/\text{d.o.f.} \sim 3$, and clear residuals in the soft band (<2 keV) and around the iron K band (6-8 keV). Even after introducing Gaussian lines to account for significant emission and absorption features, the fits remain statistically unacceptable, with $\chi^2/\text{d.o.f.} \sim 1.7$. We note that the complexities in the iron K band have been previously reported, including evidence for line broadening and a strong reflection component (G. Miniutti et al. 2007). This suggests that additional physical processes may be at play and thus motivates our modeling approach.

To carry out a more detailed analysis, we focus on the computationally fastest of the three models, *X-skirtor*. As a first test, we allow the photon index Γ to vary freely for each observation. This results in an improvement of $\Delta\chi^2 = 40$ for eight additional free parameters. Γ is generally clustered around ~ 2.3 – 2.4 for most XMM and *Chandra* spectra, indicating a broadly consistent intrinsic continuum. We report the contour plot of the photon index versus the normalization of the primary continuum in Fig. 18, upper panel. We note that while the photon indices of the XMM spectra are well constrained at 3σ (i.e., 99.87%), those of the *Chan-*

dra observations are less constrained. In particular, *Chandra_2* (2021-03-29) and *Chandra_3* (2023-04-19) observations present only a lower limit on Γ , whereas *Chandra_4* (2023-04-20) and *Chandra_5* (2023-04-21) are constrained only at the 90% c.l., and 2σ (95.45%) c.l., respectively. Overall, most observations favor a soft spectral shape; however, a significantly harder slope, with $\Gamma = 1.78 \pm 0.11$, is observed in *Chandra_1* (2006-07-31). This hard spectrum suggests either a variation in the intrinsic continuum or the effect of increased parameter degeneracy with absorption, coupled with reduced signal-to-noise ratio. In heavily absorbed spectra, a degeneracy between Γ and $N_{\text{H,LoS}}$ is expected: increasing column densities suppress soft photons, which can be compensated in the fit by a flatter Γ , and vice versa. In *Chandra_1*, the combination of a moderately high $N_{\text{H,LoS}}$ and relatively large uncertainties allows the fit to prefer a flatter continuum. We note that other spectra have similar column densities, but do not require such a hard photon index when the data quality is higher or the constraints are tighter.

As a second step, we analyze each spectrum individually. The XMM_3 and *NuSTAR* observations are simultaneous and are therefore fitted jointly. We also note that the reduced chi-squared values for the *Chandra_2*, 3, 4, and 5 observations are the closest to unity in the combined fit. In addition, the photon index is poorly constrained, the remaining parameters from the individual fits are consistent within uncertainties, and the *Chandra_3*, 4, and 5 observations are separated by only one day. For these reasons, we link these observations, allowing only the cross-calibration constant and $N_{\text{H,LoS}}$ to vary, and refer to this combined dataset as “Ch_(2+3+4+5)”. The results of the spectral fitting are presented in Table E.13 and the spectra are shown in Fig. 19.

8.2. Variability across epochs

The thermal plasma temperature remains consistent across all observations, with $kT \sim 0.85$ - 0.90 keV. No evidence for variability is found, suggesting an extended and stable plasma component, likely associated with circumnuclear or host-galaxy-scale emission rather than the central engine (see contour plot in Fig. 18, middle panel). In contrast, the photon index shows significant changes, with soft Γ during the XMM_1, XMM_2, and *Chandra* observations and a harder continuum during the simultaneous XMM_3+*NuSTAR* epoch, indicating intrinsic spectral variability. The covering factor of the neutral reflector is well constrained only for the XMM_3+*NuSTAR* observation, and lower limits are found for the remaining observations. Both the scattered fraction and continuum normalization vary between epochs. The XMM_3+*NuSTAR* observation shows an enhanced scattered component and a lower normalization, consistent with the observed flux decrease. The equatorial column density is generally poorly constrained, par-

²⁷ The derived probability is above our adopted significance threshold, but it is below the conventional $p = 0.05$ ($\text{Log}(\text{NHP}) = -1.30$) level.

ticularly in the *Chandra* observations, preventing firm conclusions regarding its variability. The line-of-sight column density exhibits clear variability, both among XMM observations and among the closely spaced *Chandra* epochs, indicating changes in the absorbing material on timescales as short as one day. We report the contour plot between the X-ray photon index and the $N_{\text{H,LoS}}$ in Fig. 18, lower panel. The time evolution of $N_{\text{H,LoS}}$ and $\Delta N_{\text{H,LoS}}$ versus $\Delta t/M_{\text{BH}}$ for MCG-03-34-064 are shown in Fig. 20. Applying the *p-value* method (see Sect. 3.5) to the best-fit $N_{\text{H,LoS}}$ values yields $p\text{-value} = 1.49 \times 10^{-3}$, confirming the variability classification for this AGN. Finally, the observed 2–10 keV flux varies reaching a factor of ~ 1.6 between the brightest (XMM_2) and faintest (XMM_3+*NuSTAR*) epochs, consistent with the combined effects of intrinsic continuum variability and variable absorption.

8.3. Physical interpretation

We note that the obtained results are potentially influenced by the nature of MCG-03-34-064 as a candidate dual AGN with a projected separation of ~ 100 pc ($\sim 0.3''$; A. Trindade Falcão et al. 2024), corresponding to a system in the transition between the dual and binary phases. At this separation, the angular resolution of XMM-*Newton* and *NuSTAR* is insufficient to disentangle the two nuclei, and the *Chandra* data reduction adopted here was not specifically optimized to isolate their individual contributions, as such an analysis is beyond the scope of this work, which may affect the modeling of the Fe K band. Within this context, the observed variability of the line-of-sight column density on timescales as short as one day suggests that at least part of the absorbing material is located at relatively small radii, possibly within the broad-line region or in clumpy structures at the inner edge of the dusty torus. In a dual AGN system transitioning towards a bound binary, the circumnuclear gas distribution is expected to be dynamically complex, and rapid changes in $N_{\text{H,LoS}}$ could arise from multiple absorbing structures at different distances, whose relative contribution along the LoS varies with time. However, we stress that comparable levels of rapid absorption variability are also commonly observed in isolated AGN, where clumpy absorbers alone can reproduce similar phenomenology. Therefore, while the dual AGN nature of MCG-03-34-064 provides a plausible framework for interpreting part of the observed spectral complexity, it is not required by the present data, and further investigation of this scenario is beyond the scope of this work. We thus conservatively classify the source as X-ray variable, with the caveat that the observed variability may be driven either by changes in the absorbing material along the LoS or by the unresolved dual nature of the system.

9. CONCLUSIONS

In this work, we carried out the first systematic multi-epoch X-ray study of a sub-sample of AGN previously classified as non-variable (in both line-of-sight column density and intrinsic flux) by X. Zhao et al. (2021) based on the analysis of only two X-ray observations per source. Our primary goals are to reassess the robustness of this classification by adopting the full archival X-ray coverage available to date, and to characterize the geometry and physical properties of the obscuring material using physically motivated torus models. We select and analyze a sample of 11 local ($z \leq 0.1$) AGN selected from the *Swift*-BAT 100-month catalog, with a total of 60 observations from *Chandra*, XMM-*Newton*, and *NuSTAR*, spanning timescales from days to nearly two decades (see Sect. 2). The AGN properties and information on the available observations are reported in Tables 1 and A.1. By simultaneously fitting all available spectra for each source with three torus models (X-skirtor, RXTorusD, and UXCLUMPY, see Sect. 3.1 for details), we constrained global torus parameters while allowing the line-of-sight column density, $N_{\text{H,LoS}}$, and the cross-normalization constant, $C_{\text{inst.,num}}$ accounting for the intrinsic flux variability, to vary between epochs. In Appendix C, we provide a description of each source, including its multiwavelength classifications and any modifications adopted to the standard fitting procedure. The LoS column density variability was assessed through both direct comparison of $N_{\text{H,LoS}}$ measurements and two complementary statistical tests (Sect. 3.5).

Our main results can be summarized as follows:

1. **Comparison of torus models.** Even though the three adopted torus models (UXCLUMPY, RXTorusD, and X-skirtor) rely on different geometrical and physical assumptions, they provide consistent estimates of $N_{\text{H,LoS}}$ (see Fig. 2) and lead to robust variability classifications (Sect. 4). Eight out of ten sources show mutual agreement in their median values (Fig. 5; Appendix B). Significant discrepancies are limited to IC 5063 and WISE J14485, likely reflecting increased model sensitivity to complex geometries or low-obscuration regimes. For example, both RXTorusD and X-skirtor are unable to constrain the column density in the low-obscuration states of WISE J14485. UXCLUMPY can provide constrained values even for $N_{\text{H,LoS}} < 10^{21} \text{ cm}^{-2}$. The constants accounting for intrinsic flux variability, are also generally in agreement between the models (Sect. 4). Concerning the remaining AGN and torus parameters (i.e., photon index, scattered fraction, covering factor for RXTorusD and X-skirtor, equatorial column density, and inclination angle) exhibit stronger inter-model discrepancies, reflecting the intrinsic differences in the

torus geometry and cloud distributions assumed by each model (Sect. 4). Moreover, we note that the $\Delta N_{\text{H,LoS}}$ derived for each pair of observations differs in absolute values across the three models (see Sect. 6.1), but the evolution is consistent as seen from the $\Delta N_{\text{H,LoS}}$ versus $\Delta t / M_{\text{BH}}$ plots in the lower panels of Figs. 7-15.

2. Compton-thin and Compton-thick classification.

The analysis confirms that the majority of our sample (9 out of 11) are Compton-thin AGN (see Table 1). We identify UGC 3752 as a candidate transitioning source and confirm the Compton-thick nature of NGC 1194 (Sect. 6). The latter shows possible transitions between CTH and CTK states on timescales of ~ 1 -2 years (see Table B.7 and Fig. 12), providing strong evidence for a clumpy and dynamic obscuring medium.

3. Reassessment of the non-variable classification.

When fitting more than two observations, we find that the original “non-variable” classification is often not robust. Out of the ten AGN for which a homogeneous analysis was possible (excluding MCG-03-34-064; Sect. 8), five sources (50%) show clear $N_{\text{H,LoS}}$ variability, three (30%) remain consistent with being non-variable, and two (20%) are classified as undetermined due to model-dependent results (see Sect. 5.2 and Tables B.2-B.11 for the best-fit results). A classification summary for all the analyzed AGN is reported in Table 3. For comparison, follow-up studies of the pre-selected variable sample find clear $N_{\text{H,LoS}}$ variability in 39% (11/28) of AGN, while the rest show either no column-density changes or Undetermined behavior (see I-V papers).

We note that 7 out of 10 AGN in our sample require intrinsic flux variability to reproduce the data (see Sect. 5.2 and Tables B.2-B.11). In the remaining three cases, the tensions are comparable across hypotheses or reveal degeneracies between intrinsic flux and $N_{\text{H,LoS}}$ variability, preventing a firm determination of the physical driver.

4. Dependence of variability detection on observational cadence.

By applying a Bayesian logistic regression to the combined sample, which includes the AGN analyzed in this work together with the previously studied variable sources from the CI-CTAGN project, we find tentative evidence for a positive relation between the number of observations N_{obs} and the probability of detecting Variable AGN (see Sect. 5.2). In particular, sources with fewer observations show a mixed population of Variable and Non-variable AGN, whereas sources with larger numbers of epochs ($N_{\text{obs}} \gtrsim 5$ -6) are increasingly dominated by Variable AGN

(Fig. 3). This result highlights the importance of both large samples and adequate temporal sampling for identifying $N_{\text{H,LoS}}$ variability.

5. Timescales and physical origin of the absorbing material.

In Sect. 6, we examine the epoch-to-epoch changes in column density as a function of time separation, $\Delta N_{\text{H,LoS}}$ versus Δt . We find that small $\Delta N_{\text{H,LoS}}$ variations occur on all timescales, whereas large changes ($\Delta N_{\text{H,LoS}} \gtrsim 5 \times 10^{23} \text{ cm}^{-2}$) are preferentially associated with long time intervals ($\Delta t \gtrsim 100$ days; see Fig. 4). This behavior, also observed by II, III, and I. S. Cox et al. (2025), supports a scenario in which both BLR-scale and torus-scale absorbers contribute to the observed variability.

6. Parameter distributions and correlations.

The distributions of torus and continuum parameters (Figs. 5 and 17) do not show statistically significant differences across AGN variability classes (see Sect. 7.1 and Table D.12). No statistically significant difference is present between the pre-selected non-variable and variable samples distributions in terms of number of Δt pairs (see Fig. 6). We also investigate possible correlations between torus and AGN parameters. However, no statistically significant correlations are detected in the current sample (see Sect. 7.2 for more details).

7. The case of MCG-03-34-064.

MCG-03-34-064 represents a special case in our sample and was therefore analyzed separately (Sect. 8). Unlike the other AGN, the assumption of constant spectral shape across epochs is not valid for this source, preventing a simultaneous multi-epoch fit. When observations are fitted independently (see Sect. 8 for the details on the analysis, Table E.13 for the best-fit results and Figs. 19 and 18 for the spectra and contours plots), MCG-03-34-064 exhibits clear variability in $N_{\text{H,LoS}}$ on timescales ranging from days to years (see Table E.13 and Fig. 20). This variability may be due to changes in the line-of-sight absorbing column density, to the dual-AGN nature of the system, or to a combination of both effects.

In conclusion, our analysis reveals that a substantial fraction of AGN previously classified as non-variable do, in fact, exhibit significant line-of-sight column density variability when sufficient temporal coverage is available. This result strengthens the case for a clumpy, inhomogeneous, and dynamic torus as a common feature of nearby AGN. More generally, it highlights the critical importance of long-term, multi-epoch X-ray monitoring for properly characterizing AGN obscuration. The extension of this analysis to the remaining (pre-selected) non-variable sources in the CI-CTAGN sample will allow these findings to be placed on

firmer statistical grounds and will further constrain the physical structure of the AGN torus.

ACKNOWLEDGMENTS

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APPENDIX

A. SAMPLE

In Table A.1, we report the information on the X-ray observations of the sub-sample of 11 non-variable AGN analyzed in this paper.

Table A.1. X-ray observation details.

(1)	(2)	(3)	(4)	(5)	(6)
Source	Telescope	Obs. ID	Obs. date	Exp. time [ks]	Tot. counts
ESO 464-G016	<i>XMM-Newton</i>	0762920401	2016-04-11	16.2	713
	<i>NuSTAR</i>	60101013002	2016-04-13	22.1 (0.3%)	774 (4.5%)
	<i>Chandra</i>	27972	2023-08-04	9.9	71
IC 5063	<i>NuSTAR</i>	60061302002	2013-07-08	18.4 (0.1%)	7550 (8.2%)
	<i>Chandra</i> 1	7878	2007-06-15	34.1	4810
	<i>Chandra</i> 2	21467	2018-12-11	26.9	3086
	<i>Chandra</i> 3	21999	2018-12-12	34.1	3612
	<i>Chandra</i> 4	22000	2018-12-13	15.6	1610
	<i>Chandra</i> 5	22001	2018-12-15	29.3	3325
	<i>Chandra</i> 6	22002	2018-12-16	43.9	4443
LEDA 511869	<i>XMM-Newton</i>	0802450401	2018-02-09	17.3	1176
	<i>NuSTAR</i> 1	60201033002	2016-05-25	21.5 (0.1%)	774 (0.9%)
	<i>NuSTAR</i> 2	60061252002	2020-03-25	23.5 (0.9%)	1470 (8.7%)

Table A.1 *continued*

Table A.1 (continued)

(1)	(2)	(3)	(4)	(5)	(6)
Source	Telescope	Obs. ID	Obs. date	Exp. time [ks]	Tot. counts
MCG-03-34-064	XMM-Newton 1	0206580101	2005-01-24	38.3	21394
	XMM-Newton 2	0506340101	2008-01-24	76.5	41441
	XMM-Newton 3	0763220201	2016-01-17	123.3	62583
	NuSTAR	60101020002	2016-01-17	78.4 (0.3%)	11038 (2.6%)
	Chandra 1	7373	2006-07-31	7.1	992
	Chandra 2	23690	2021-03-29	3.1	225
	Chandra 3	25253	2023-04-19	15.6	926
	Chandra 4	27802	2023-04-20	17.9	1150
Mrk 18	Chandra 5	27803	2023-04-21	16.9	1003
	XMM-Newton	0312191001	2006-03-23	9.8	1547
	NuSTAR 1	60061088002	2013-12-15	20.2 (0.2%)	832 (15.4%)
	NuSTAR 2 †	60760004001	2022-08-15	30.7 (1.0%)	801 (13.2%)
Mrk 1498	Chandra †	23813	2022-08-15	19.2	375
	XMM-Newton	0500850501	2007-06-23	7.6	4771
	NuSTAR	60160640002	2015-05-11	23.7 (0.3%)	8458 (0.3%)
NGC 1194	Chandra	17085	2016-05-15	19.5	3172
	XMM-Newton 1	0307000701	2006-02-19	12.5	1303
	XMM-Newton 2 †	0852200101	2020-01-16	52.9	5294
	NuSTAR 1	60061035002	2015-02-28	31.5 (0.2%)	2639 (1.8%)
	NuSTAR 2 †	60501011002	2020-01-17	58.1 (0.3%)	5160 (3.2%)
	Chandra 1	22552	2019-10-22	39.5	1056
	Chandra 2	22880	2019-10-25	20.0	482
	Chandra 3	22881	2019-10-27	20.3	541
NGC 2655	Chandra 4	23688	2020-11-05	7.6	216
	XMM-Newton	0301650301	2005-09-04	8.8	2704
	NuSTAR 1	60160341002	2016-11-02	5.1 (0.2%)	203 (6.4%)
	NuSTAR 2 *	60160341003	2016-11-10	0.2 (0.3%)	15 (20.7%)
	NuSTAR 2 *	60160341004	2016-11-10	15.9 (0.3%)	705 (1.4%)
	Chandra 1 *	28152	2025-03-03	12.1	205
NGC 4785	Chandra 1 *	30827	2025-03-03	11.9	216
	XMM-Newton 1 †	0743010101	2014-08-20	22.9	2066
	XMM-Newton 2	0762920701	2015-07-03	16.1	1500
	XMM-Newton 3	0762920801	2016-01-15	16.9	1796
	NuSTAR 1 †	60001143002	2014-08-20	48.8 (0.1%)	2764 (12.4%)
	NuSTAR 2	60161523002	2021-03-10	18.3 (0.6%)	147 (20.4%)
	NuSTAR 3	60161523004	2023-06-04	21.5 (0.5%)	675 (27.3%)
	Chandra	18074	2016-04-16	9.8	245

Table A.1 continued

Table A.1 (continued)

(1)	(2)	(3)	(4)	(5)	(6)
Source	Telescope	Obs. ID	Obs. date	Exp. time [ks]	Tot. counts
UGC 03752	XMM-Newton	0883210701	2022-03-28	18.3	2147
	NuSTAR 1	60061072002	2013-12-03	23.6 (0.2%)	871 (4.1%)
	NuSTAR 2	60061072004	2020-04-17	31.3 (0.5%)	788 (3.9%)
	NuSTAR 3	60702053002	2021-10-22	23.8 (0.4%)	535 (16.3%)
	NuSTAR 4	60702053004	2021-11-08	29.7 (0.5%)	1038 (9.8%)
	NuSTAR 5	60702053006	2022-03-01	26.7 (0.6%)	2239 (8.6%)
	Chandra	30709	2025-01-05	9.9	93
WISE J144850	XMM-Newton	0720280101	2014-02-16	22.4	21038
	NuSTAR	60463049002	2019-03-12	20.2 (0.7%)	3471 (18.8%)
	Chandra	22226	2019-05-19	10.0	1705

NOTE— Columns: 1) source name; 2) telescope used in the analysis; 3) observation ID; 4) observation date; 5) effective exposure time after reduction in ks; 6) total source counts after reduction. We note that the exposure times for XMM refer to the EPIC-pn spectra. Meanwhile, the reported exposure times and total counts for NuSTAR are averaged between FPMA and FPMB, with the range of percentage variance between the two in parentheses.

†: the marked observations are simultaneous and will be fitted accordingly, i.e., assuming no variability in flux and line-of-sight column density.

*: the NuSTAR observations 60160341003 and 60160341004, as well as the Chandra observations 28152 and 30827, are consecutive in time; therefore, each pair is treated as a single NuSTAR and a single Chandra observation, respectively, during the spectral analysis.

B. X-RAY FITTING RESULTS

In this work, we present the best-fit results for 11 Compton-thin, local AGN with multi-epoch observations selected from the 100-month BAT catalog. We analyze 60 X-ray observations from *Chandra*, *XMM-Newton*, and *NuSTAR*, using physical torus models (*xskirtor*, *RxTorusD*, and *UXCLUMPY*) and constraining the torus parameters and the line-of-sight column density for each observation. In Tables B.2-B.11, we report the best-fit values obtained from the simultaneous multi-epoch spectral analysis. Particularly, for each Table the following parameters are shown. We report the physical and geometrical properties of the torus are described by the following parameters: C_f is the covering factor of the torus; θ is the inclination angle, where $\theta = 0^\circ$ is the face-on scenario; F_s is the fraction of scattered continuum; and Norm is the normalization of the AGN emission. We note that, if the inclination results to be completely unconstrained during the fit, we fix it to $\theta = 60^\circ$. In the following tables, we report the parameter *CTKcover* of the *UXCLUMPY* model as C_f . However, the reader should be aware that this quantity represents the covering factor of the inner Compton-thick ring of clouds (see Sect. 3.2), and therefore it does not physically correspond to the global torus covering factor defined in the other models. Consequently, these parameters cannot be directly compared. For what concern *RxTorusD* and *xskirtor* models, $N_{H,eq}$ is the equatorial column den-

sity of the torus. The vertical extent of the cloud population is reported as σ_{tor} for the *UXCLUMPY* model. $N_{H,inst,num}$ shows the LoS hydrogen column density for a given observation. $C_{inst,num}$ represents the cross-normalization constant for each observation, with respect to the intrinsic flux of the first *Chandra* observation. The last part of each Table presents the χ^2 of the best-fit when considering: a) no variability between observations; b) no intrinsic flux variability; c) no $N_{H,LoS}$ variability. In Fig. 17, we show the distributions of the best-fit parameters for each AGN and each adopted model.

Table B.2. ESO 464-G016: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	$0.26^{+0.06}_{-0.04}$	$0.28^{+0.09}_{-0.06}$	$0.27^{+0.06}_{-0.04}$
Comptonized primary continuum			
Γ	$1.62^{+0.32}_{-0.39}$	$1.63^{+0.33}_{-0.39}$	$1.71^{+0.19}_{-0.28}$
Neutral reflector			
C_f^+	$0.45_{-0.13}$	$0.81^{+0.17}_{-0.26}$	0^f
θ / deg	67^{+7}_{-6}	54^{+20}_{-16}	60^f
σ_{tor} / deg	/	/	$26.49^{+36.78}_{-11.97}$
$F_s / 10^{-2}$	$0.61^{+1.11}_{-0.37}$	$0.14^{+0.48}_{-0.11}$	$1.24^{+1.68}_{-0.71}$
norm / 10^{-3}	$1.23^{+2.28}_{-0.88}$	$5.55^{+1.55}_{-4.28}$	$2.11^{+1.33}_{-1.14}$
$N_{\text{H,eq}} / 10^{22} \text{ cm}^{-2}$	$79.43^{+110.27}_{-47.81}$	$304.72^{+170.28}_{-143.72}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{Ch} / 10^{22} \text{ cm}^{-2}$	$78.79^{+24.09}_{-23.84}$	$112.21^{+34.82}_{-30.68}$	$107.36^{+49.60}_{-31.40}$
$N_{\text{H}}^{XMM} / 10^{22} \text{ cm}^{-2}$	$71.21^{+17.83}_{-20.97}$	$102.66^{+33.23}_{-27.28}$	$95.02^{+40.88}_{-21.95}$
$N_{\text{H}}^{NuS} / 10^{22} \text{ cm}^{-2}$	$65.60^{+19.85}_{-16.80}$	$98.52^{+33.69}_{-13.93}$	$79.27^{+20.74}_{-10.37}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1^f	1^f	1^f
C_{XMM}	$0.92^{+0.49}_{-0.31}$	$0.90^{+0.48}_{-0.30}$	$0.94^{+0.48}_{-0.35}$
C_{NuS}	$1.00^{+0.74}_{-0.41}$	$1.02^{+0.83}_{-0.42}$	$0.94^{+0.50}_{-0.28}$
Statistic			
C-stat/d.o.f.	268/215	259/215	239/217
T	3.61σ	3.00σ	1.49σ
p-value	0.91	0.95	0.71
Statistic (No variability)			
C-stat/d.o.f.	278/219	278/219	249/221
T	3.99σ	3.99σ	1.88σ
Statistic (No flux variability)			
C-stat/d.o.f.	269/217	270/217	240/219
T	3.53σ	3.60σ	1.42σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	269/217	268/217	241/219
T	3.53σ	3.46σ	1.49σ

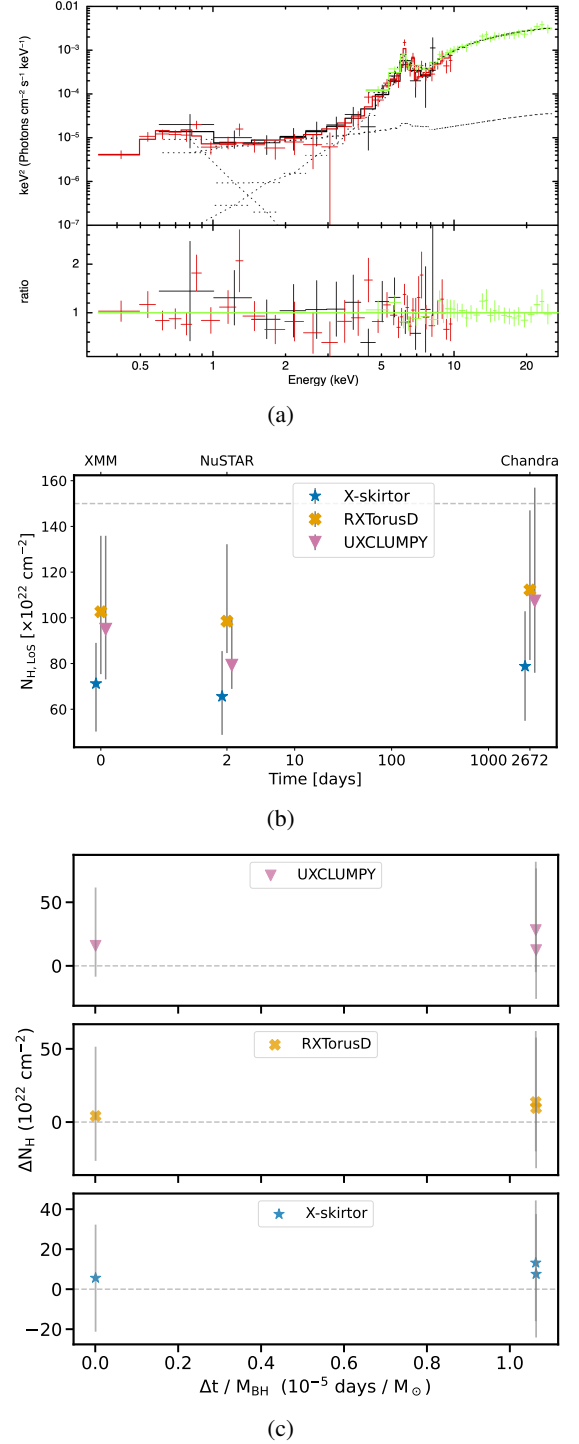
NOTE—⁺: For UXCLUMPY, C_f represents the inner Compton-thick ring covering factor and it cannot be directly compared with the covering factors of X-skirtor and RXTorusD, see Sect. 3.2.**Figure 7.** ESO 464-G016. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), *XMM-Newton* (in red), and *NuSTAR* (FPMA and FPMB spectra are grouped together in green) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$ derived from the different torus models (X-skirtor in yellow stars, RXTorusD in green crosses, and UXCLUMPY in purple triangles). The x-axis is in logarithmic scale to clearly present the timescale between observations. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass, for three adopted torus models (UXCLUMPY in pink, RXTorusD in yellow, and X-skirtor in light blue).

Table B.3. IC 5063: spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	0.74 ^{+0.07} _{-0.08}	0.75 ^{+0.07} _{-0.08}	0.71 ^{+0.12} _{-0.15}
Comptonized primary continuum			
Γ	1.49 \pm 0.05	1.49 \pm 0.05	1.73 ^{+0.03} _{-0.07}
Neutral reflector			
C_f^+	0.59 ^{+0.11} _{-0.10}	0.66 ^{+0.07} _{-0.05}	0.60 _{-0.05}
θ / deg	52 ⁺⁶ ₋₄	39 ⁺⁷ ₋₁₃	60 ^f
σ_{tor} / deg	/	/	6.50 ^{+1.00} _{-2.78}
$F_s / \times 10^{-2}$	0.59 ^{+0.01} _{-0.9}	5.59 ^{+0.63} _{-0.73}	2.25 ^{+0.28} _{-0.26}
norm / $\times 10^{-3}$	3.47 ^{+0.46} _{-0.41}	3.44 ^{+0.43} _{-0.38}	7.10 ^{+1.07} _{-1.24}
$N_{\text{H,eq}} / 10^{22} \text{ cm}^{-2}$	15.55 ^{+4.25} _{-2.43}	22.99 ^{+5.15} _{-3.93}	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{Ch,1}} / 10^{22} \text{ cm}^{-2}$	23.19 ^{+1.21} _{-1.17}	26.56 ^{+1.45} _{-1.37}	21.41 ^{+1.18} _{-1.14}
$N_{\text{H}}^{\text{Ch,2}} / 10^{22} \text{ cm}^{-2}$	35.83 ^{+2.15} _{-2.18}	41.07 ^{+2.81} _{-2.55}	32.44 ^{+1.59} _{-1.94}
$N_{\text{H}}^{\text{Ch,3}} / 10^{22} \text{ cm}^{-2}$	39.04 ^{+2.47} _{-2.46}	44.82 ^{+3.10} _{-2.92}	34.36 ^{+1.37} _{-1.60}
$N_{\text{H}}^{\text{Ch,4}} / 10^{22} \text{ cm}^{-2}$	35.69 ^{+3.10} _{-3.06}	40.79 ^{+4.01} _{-3.48}	32.00 ^{+2.20} _{-2.66}
$N_{\text{H}}^{\text{Ch,5}} / 10^{22} \text{ cm}^{-2}$	36.78 ^{+2.20} _{-2.23}	42.16 ^{+2.85} _{-2.61}	33.04 ^{+1.51} _{-1.82}
$N_{\text{H}}^{\text{Ch,6}} / 10^{22} \text{ cm}^{-2}$	40.46 ^{+2.61} _{-2.65}	46.48 ^{+3.23} _{-3.10}	34.66 ^{+1.27} _{-1.41}
$N_{\text{H}}^{\text{Ch,7}} / 10^{22} \text{ cm}^{-2}$	30.72 ^{+1.20} _{-1.22}	35.16 ^{+1.51} _{-1.41}	27.25 ^{+0.51} _{-0.64}
$N_{\text{H}}^{\text{NuS}} / 10^{22} \text{ cm}^{-2}$	21.48 ^{+2.14} _{-2.18}	24.08 ^{+2.35} _{-2.39}	20.16 ^{+2.25} _{-1.53}
$C_{\text{inst,num}}$ (Cross-normalization constant)			
$C_{\text{Ch,1}}$	1 ^f	1 ^f	1 ^f
$C_{\text{Ch,2}}$	1.34 ^{+0.12} _{-0.11}	1.34 ^{+0.12} _{-0.11}	1.28 ^{+0.14} _{-0.12}
$C_{\text{Ch,3}}$	1.35 \pm 0.12	1.34 ^{+0.12} _{-0.11}	1.26 ^{+0.13} _{-0.10}
$C_{\text{Ch,4}}$	1.19 ^{+0.14} _{-0.13}	1.18 ^{+0.14} _{-0.13}	1.12 ^{+0.15} _{-0.13}
$C_{\text{Ch,5}}$	1.36 \pm 0.12	1.36 \pm 0.11	1.29 ^{+0.14} _{-0.11}
$C_{\text{Ch,6}}$	1.34 ^{+0.12} _{-0.11}	1.33 ^{+0.12} _{-0.11}	1.22 ^{+0.13} _{-0.09}
$C_{\text{Ch,7}}$	1.45 \pm 0.09	1.45 ^{+0.10} _{-0.09}	1.34 ^{+0.11} _{-0.08}
C_{NuS}	1.28 ^{+0.11} _{-0.10}	1.25 \pm 0.10	1.36 ^{+0.10} _{-0.19}
Statistic			
C-stat/d.o.f.	753/681	762/681	770/682
T	2.76 σ	3.10 σ	3.47 σ
p-value	0	0	0
Statistic (No variability)			
C-stat/d.o.f.	2283/695	2261/695	2487/696
T	60.24 σ	59.40 σ	67.89 σ
Statistic (No flux variability)			
C-stat/d.o.f.	845/688	868/688	981/689
T	5.99 σ	6.86 σ	11.12 σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	1055/688	1069/688	1249/689
T	13.99 σ	14.53 σ	21.33 σ

NOTE—Refer to note in Table B.2.

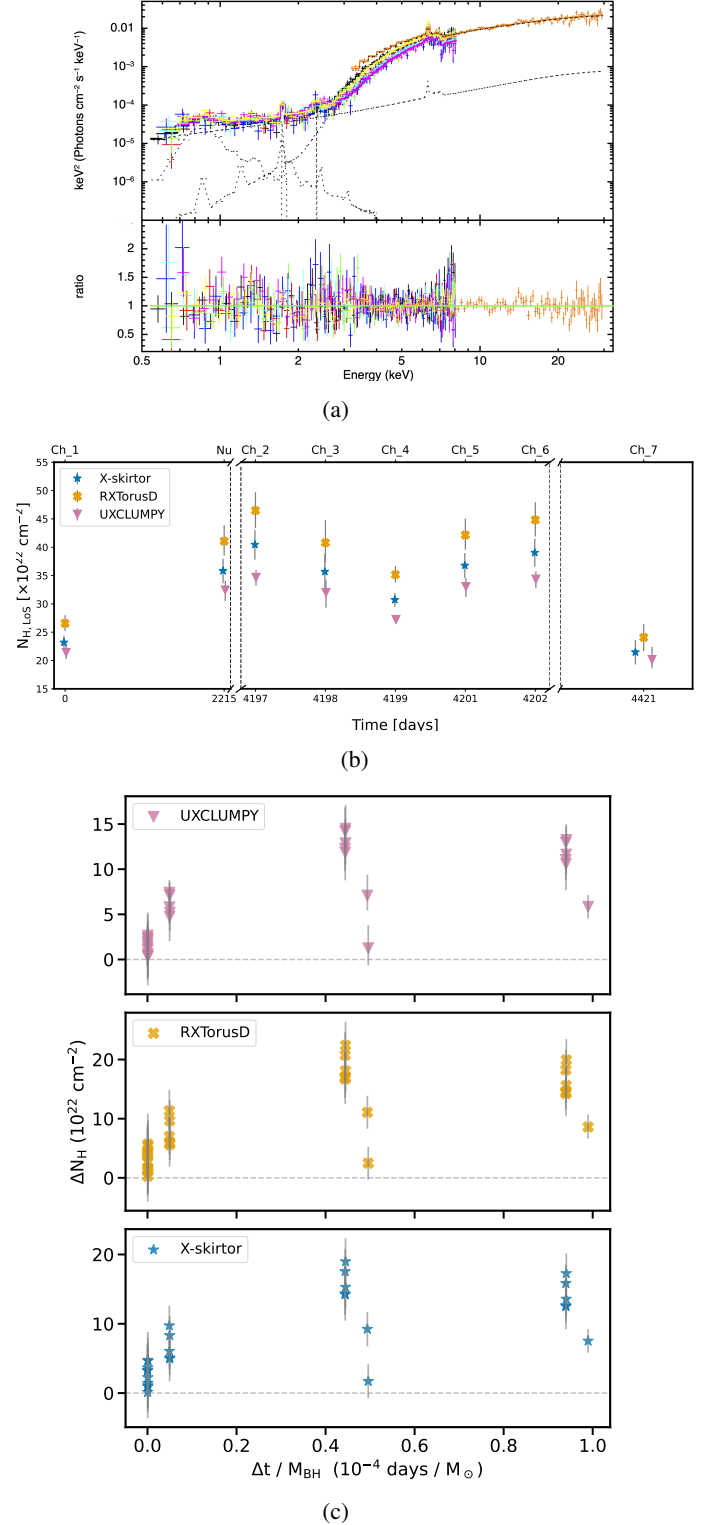
**Figure 8.** IC 5063. *Panel a:* best-fit with the UXCLUMPY torus model. The *Chandra* (in black, red, blue, cyan, pink, and yellow) and *NuSTAR* (FPMA and FPMB spectra are grouped together in orange) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in logarithmic scale for the left and right panel, linear for the middle panel, with a visual break to compress the long timescale between observations. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.4. LEDA 511869: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	$0.63^{+0.51}_{-0.31}$	$0.69^{+0.38}_{-0.64}$	$0.55^{+0.32}_{-0.43}$
Comptonized primary continuum			
Γ	$1.57^{+0.13}_{-0.15}$	$1.47^{+0.15}_{-0.30}$	$1.58^{+0.16}_{-0.14}$
Neutral reflector			
C_f +	$0.42^{+0.18}_{-0.11}$	$0.79^{+0.13}_{-0.09}$	$0.30^{+0.12}_{-0.17}$
θ / deg	70^{+2}_{-6}	78_{-30}	90_{-29}
σ_{tor} / deg	/	/	$17.33^{+6.65}_{-6.53}$
F_s / 10^{-3}	$2.19^{+1.48}_{-1.46}$	3.02 ± 1.11	$2.29^{+2.56}_{-1.16}$
norm / 10^{-3}	$2.72^{+0.99}_{-0.91}$	$1.19^{+0.55}_{-0.61}$	$3.64^{+1.53}_{-1.16}$
$N_{\text{H,eq}}$ / 10^{22} cm^{-2}	1000_{-76}	$80.94^{+237.17}_{-18.27}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{XMM}}$ / 10^{22} cm^{-2}	$74.54^{+7.59}_{-8.14}$	$69.79^{+18.24}_{-9.64}$	$74.71^{+7.90}_{-7.81}$
$N_{\text{H}}^{\text{NuS,1}}$ / 10^{22} cm^{-2}	$70.76^{+10.33}_{-10.92}$	$76.91^{+15.09}_{-17.88}$	$72.74^{+12.04}_{-12.23}$
$N_{\text{H}}^{\text{NuS,2}}$ / 10^{22} cm^{-2}	$53.71^{+7.27}_{-7.85}$	$48.28^{+15.45}_{-9.55}$	$52.70^{+9.97}_{-7.85}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{XMM}	1^f	1^f	1^f
$C_{\text{NuS,1}}$	$0.71^{+0.18}_{-0.14}$	$0.59^{+0.37}_{-0.15}$	$0.51^{+0.16}_{-0.13}$
$C_{\text{NuS,2}}$	$0.63^{+0.16}_{-0.20}$	$0.70^{+0.15}_{-0.14}$	$0.62^{+0.17}_{-0.13}$
Statistic			
$\chi^2/\text{d.o.f.}$	186/212	186/212	187/212
T	1.79σ	1.79σ	1.72σ
p-value	0.12	0.39	0.20
Statistic (No variability)			
$\chi^2/\text{d.o.f.}$	422/216	423/216	424/217
T	14.02σ	14.08σ	14.05σ
Statistic (No flux variability)			
$\chi^2/\text{d.o.f.}$	197/214	199/214	197/214
T	1.16σ	1.03σ	1.16σ
Statistic (No N_{H} variability)			
$\chi^2/\text{d.o.f.}$	206/214	204/214	205/214
T	0.55σ	0.68σ	0.62σ

NOTE—Refer to note in Table B.2.

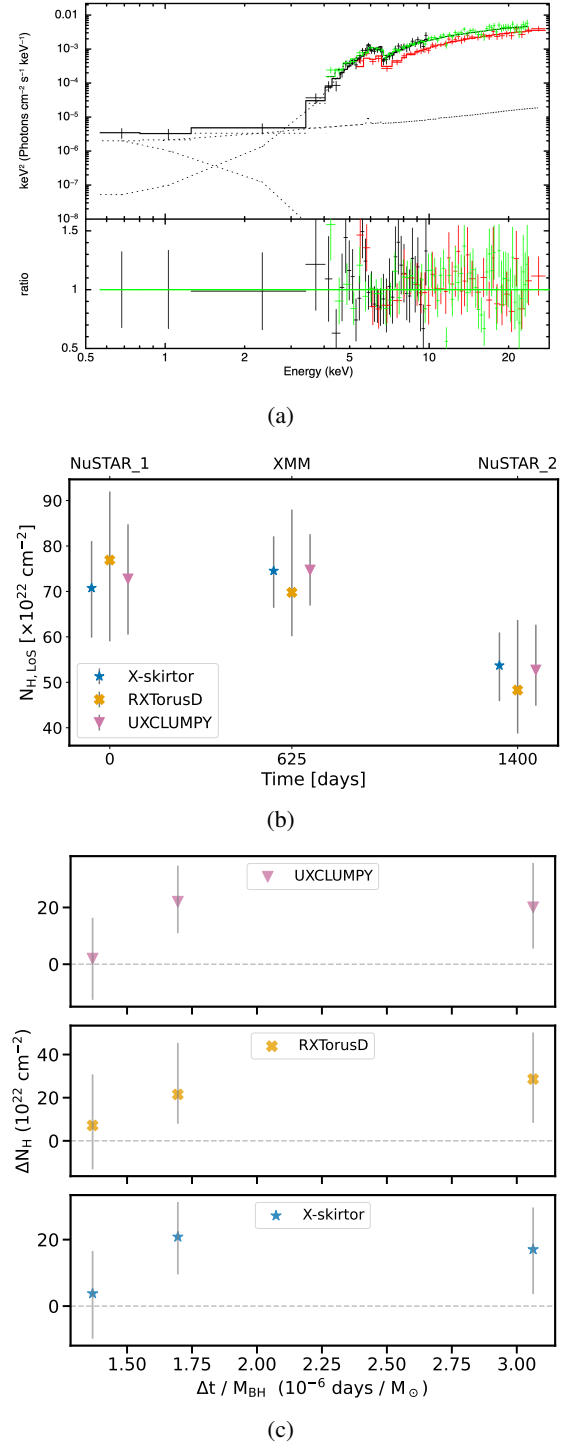
**Figure 9.** LEDA 511869. *Panel a:* Best-fit with the UXCLUMPY torus model. The XMM-Newton (in black), NuSTAR 1 (in red) and NuSTAR 2 (in green) spectra are shown. FPMA and FPMB spectra are grouped together for each NuSTAR observation. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in linear scale. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.5. Mrk 18: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
KT / keV	$0.74^{+0.28}_{-0.31}$	$0.74^{+0.18}_{-0.22}$	$0.74^{+0.19}_{-0.22}$
Comptonized primary continuum			
Γ	$1.94^{+0.18}_{-0.24}$	$1.93^{+0.22}_{-0.40}$	$1.95^{+0.13}_{-0.17}$
Neutral reflector			
C_f^+	$0.59^{+0.04}_{-0.19}$	$0.95_{-0.03}$	$0.30^{+0.26}_{-0.22}$
θ / deg	20^f	18^{+2}_{-3}	20^f
σ_{tor} / deg	/	/	$24.03^{+22.98}_{-11.09}$
$F_s / 10^{-2}$	$1.06^{+0.94}_{-0.54}$	$0.50^{+2.33}_{-0.35}$	$0.11^{+0.31}_{-0.09}$
norm / 10^{-3}	0.47 ± 0.18	$0.44^{+0.20}_{-0.24}$	$0.62^{+0.21}_{-0.18}$
$N_{\text{H,eq}} / 10^{22} \text{ cm}^{-2}$	$246.94^{+123.93}_{-103.35}$	$85.21^{+53.24}_{-56.87}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{Ch}} / 10^{22} \text{ cm}^{-2}$	$9.87^{+2.21}_{-1.91}$	$12.72^{+3.12}_{-5.94}$	$8.99^{+2.00}_{-1.68}$
$N_{\text{H}}^{\text{XMM}} / 10^{22} \text{ cm}^{-2}$	$14.18^{+3.00}_{-2.66}$	$19.50^{+4.70}_{-4.23}$	$13.29^{+2.89}_{-2.14}$
$N_{\text{H}}^{\text{NuS,1}} / 10^{22} \text{ cm}^{-2}$	$15.86^{+4.97}_{-4.43}$	$21.64^{+7.11}_{-8.67}$	$15.65^{+4.36}_{-4.61}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1^f	1^f	1^f
C_{XMM}	$2.25^{+0.55}_{-0.42}$	$2.31^{+0.56}_{-0.50}$	$2.30^{+0.57}_{-0.41}$
$C_{\text{NuS,1}}$	$2.01^{+0.58}_{-0.39}$	$2.04^{+0.55}_{-0.47}$	$2.09^{+0.59}_{-0.43}$
Statistic			
$\chi^2/\text{d.o.f.}$	222/193	227/192	231/193
T	2.08σ	2.52σ	2.74σ
p-value	0.05	0.04	0.03
Statistic (No variability)			
$\chi^2/\text{d.o.f.}$	356/199	364/198	367/199
T	11.12σ	11.80σ	11.91σ
Statistic (No flux variability)			
$\chi^2/\text{d.o.f.}$	294/196	225/195	302/196
T	7.00σ	2.15σ	7.57σ
Statistic (No N_{H} variability)			
$\chi^2/\text{d.o.f.}$	234/196	235/195	242/196
T	2.71σ	2.86σ	3.29σ

NOTE—Refer to note in Table B.2.

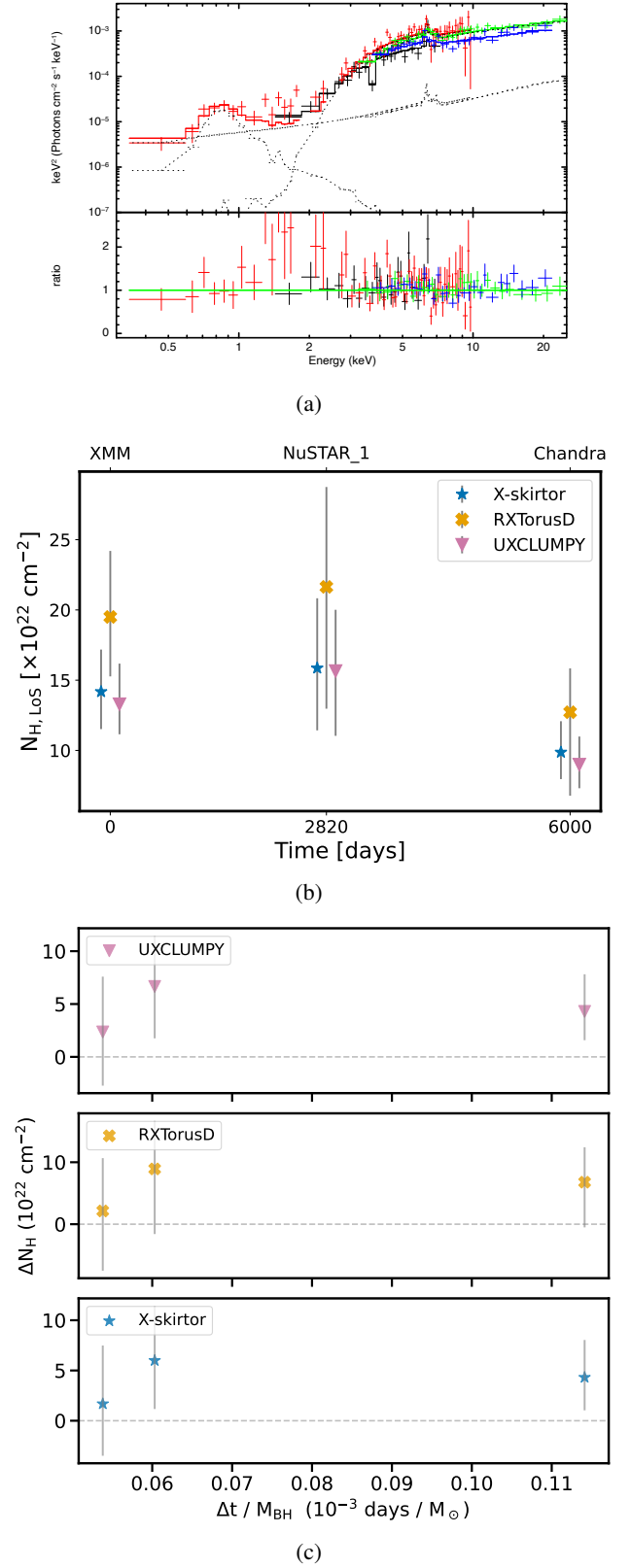
**Figure 10.** Mrk 18. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), *XMM* (in red) and *NuSTAR* (FPMA and FPMB spectra grouped together in green and blue) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The left part of the x-axis is in linear scale with a visual break, the right part is not in scale to clearly visualize the *Chandra* and *NuSTAR 2* observations, which are only few hours apart. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.6. Mrk 1498: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	$0.10^{+0.03}_{-0.02}$	0.11 ± 0.02	$0.10^{+0.03}_{-0.02}$
Comptonized primary continuum			
Γ	$1.53^{+0.08}_{-0.06}$	$1.55^{+0.10}_{-0.06}$	1.57 ± 0.04
Neutral reflector			
C_r^+	$0.50^{+0.12}$	$0.58^{+0.30}_{-0.35}$	0^f
θ / deg	78^{+16}	87_{-21}	87^{+4}_{-16}
$\sigma_{\text{tor}} / \text{deg}$	/	/	$5.97^{+3.04}_{-0.61}$
$F_s / 10^{-2}$	$1.44^{+0.21}_{-0.24}$	$1.48^{+0.55}_{-0.32}$	1.55 ± 0.01
$\text{norm} / 10^{-3}$	$2.98^{+0.61}_{-0.37}$	$2.87^{+0.81}_{-0.79}$	4.79 ± 0.88
$N_{\text{H,eq}}$	$41.77^{+43.95}_{-19.11}$	$82.58^{+177.25}_{-26.42}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{Ch}} / 10^{22} \text{ cm}^{-2}$	$17.26^{+1.14}_{-1.03}$	$19.04^{+1.81}_{-1.77}$	$16.72^{+1.06}_{-1.15}$
$N_{\text{H}}^{\text{XMM}} / 10^{22} \text{ cm}^{-2}$	$16.17^{+1.24}_{-1.36}$	$17.34^{+2.08}_{-2.05}$	$15.75^{+1.32}_{-1.41}$
$N_{\text{H}}^{\text{NuS}} / 10^{22} \text{ cm}^{-2}$	$10.87^{+1.51}_{-1.43}$	$10.75^{+2.28}_{-2.51}$	$10.70^{+1.37}_{-1.32}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1^f	1^f	1^f
C_{XMM}	1.01 ± 0.08	$0.99^{+0.08}_{-0.07}$	1.02 ± 0.08
C_{NuS}	$0.99^{+0.08}_{-0.07}$	0.96 ± 0.07	$1.03^{+0.09}_{-0.26}$
Statistic			
C-stat/d.o.f.	346/297	321/297	334/298
T	2.84σ	1.39σ	2.09σ
p-value	$1.12\text{e-}03$	0.01	$2.14\text{e-}03$
Statistic (No variability)			
C-stat/d.o.f.	536/301	522/301	527/302
T	12.95σ	12.74σ	13.55σ
Statistic (No flux variability)			
C-stat/d.o.f.	346/299	322/299	334/300
T	2.72σ	1.33σ	1.96σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	393/299	378/299	379/300
T	5.44σ	4.57σ	4.56σ

NOTE—Refer to note in Table B.2.

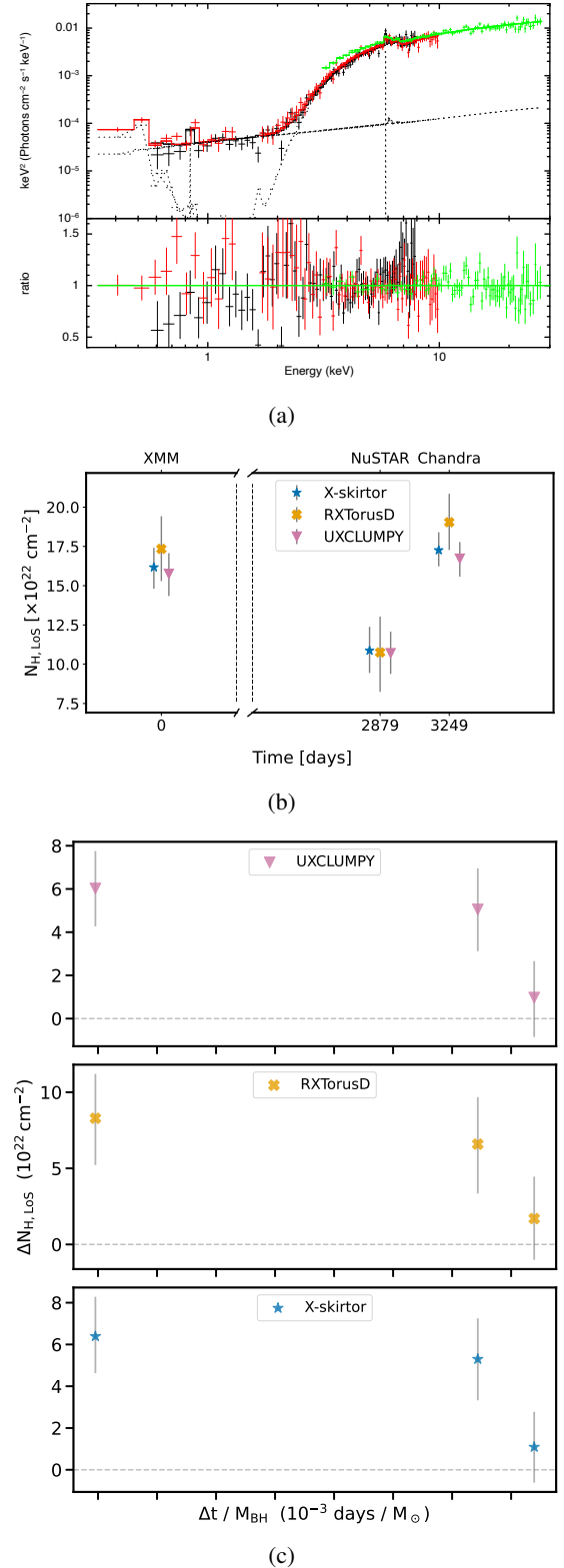


Figure 11. Mrk 1498. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), *XMM-Newton* (in red), and *NuSTAR* (FPMA and FPMB spectra are grouped together in green) spectra are shown. *Panel b:* evolution of $N_{\text{H,LoS}}$ with time. The x-axis is in logarithmic scale with a visual break to compress the long timescale between observations. *Panel c:* variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.7. NGC 1194: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	$1.18^{+0.10}_{-0.09}$	$1.18^{+0.09}_{-0.08}$	$1.22^{+0.09}_{-0.07}$
Comptonized primary continuum			
Γ	$1.54^{+0.05}_{-0.06}$	$1.49^{+0.04}_{-0.04}$	$1.56^{+0.04}_{-0.16}$
Neutral reflector			
C_f	$0.25^{+0.04}$	$0.40^{+0.01}_{-0.04}$	$0.30^{+0.06}_{-0.04}$
θ / deg	76^{+3}_{-1}	51 ± 1	60^f
σ_{tor} / deg	/	/	$7.00^{+4.07}_{-2.31}$
F_s / 10^{-2}	$0.33^{+0.11}_{-0.05}$	$0.24^{+0.54}_{-0.53}$	$0.60^{+0.18}_{-0.30}$
norm / 10^{-3}	$4.94^{+1.03}_{-1.26}$	$4.92^{+0.99}_{-0.65}$	2.17 ± 0.01
$N_{\text{H,eq}}$ / 10^{22} cm^{-2}	$43.51^{+9.75}_{-9.69}$	$63.58^{+10.51}_{-4.20}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{Ch,1}}$ / 10^{22} cm^{-2}	$135.24^{+22.96}_{-16.34}$	$148.04^{+19.25}_{-13.21}$	$136.17^{+9.08}_{-8.57}$
$N_{\text{H}}^{\text{Ch,2}}$ / 10^{22} cm^{-2}	$136.68^{+50.08}_{-24.88}$	$146.94^{+37.68}_{-22.02}$	$141.12^{+23.06}_{-20.25}$
$N_{\text{H}}^{\text{Ch,3}}$ / 10^{22} cm^{-2}	$139.59^{+41.65}_{-22.47}$	$150.48^{+33.78}_{-20.26}$	$137.41^{+17.44}_{-18.63}$
$N_{\text{H}}^{\text{Ch,4}}$ / 10^{22} cm^{-2}	$149.71^{+33.97}$	$161.87^{+153.00}_{-32.50}$	$149.99^{+65.69}_{-28.12}$
$N_{\text{H}}^{\text{XMM,1}}$ / 10^{22} cm^{-2}	$136.55^{+18.91}_{-15.49}$	$168.64^{+22.42}_{-16.98}$	$130.33^{+11.59}_{-13.77}$
$N_{\text{H}}^{\text{XMM,2}}$ / 10^{22} cm^{-2}	$138.90^{+12.19}_{-11.91}$	$163.38^{+11.17}_{-9.84}$	$140.08^{+6.62}_{-6.23}$
$N_{\text{H}}^{\text{NuS,1}}$ / 10^{22} cm^{-2}	$208.60^{+16.21}_{-17.31}$	$238.54^{+15.21}_{-14.33}$	$256.22^{+22.06}_{-21.96}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
$C_{\text{Ch,1}}$	1^f	1^f	1^f
$C_{\text{Ch,2}}$	0.94 ± 0.15	$0.94^{+0.14}_{-0.15}$	$0.87^{+0.13}_{-0.12}$
$C_{\text{Ch,3}}$	$1.04^{+0.16}_{-0.15}$	$1.04^{+0.14}_{-0.15}$	$1.04^{+0.14}_{-0.12}$
$C_{\text{Ch,4}}$	$1.29^{+0.25}_{-0.24}$	$1.30^{+0.23}_{-0.25}$	$1.27^{+0.23}_{-0.21}$
$C_{\text{XMM,1}}$	$0.76^{+0.12}_{-0.10}$	$0.92^{+0.10}_{-0.11}$	$0.62^{+0.09}_{-0.08}$
$C_{\text{XMM,2}}$	$0.83^{+0.10}_{-0.08}$	$0.94^{+0.08}_{-0.09}$	$0.65^{+0.06}_{-0.03}$
$C_{\text{NuS,1}}$	$1.29^{+0.18}_{-0.16}$	$1.49^{+0.13}_{-0.16}$	$0.77^{+0.14}_{-0.11}$
Statistic			
$\chi^2/\text{d.o.f.}$	653/594	653/594	660/595
T	2.42σ	2.42σ	2.66σ
p-value	$2.11\text{e-}15$	$6.67\text{e-}9$	0
Statistic (No variability)			
$\chi^2/\text{d.o.f.}$	785/608	771/608	846/609
T	7.18σ	6.61σ	9.30σ
Statistic (No flux variability)			
$\chi^2/\text{d.o.f.}$	766/601	758/601	831/602
T	6.73σ	6.40σ	9.33σ
Statistic (No N_{H} variability)			
$\chi^2/\text{d.o.f.}$	747/601	790/601	919/602
T	5.95σ	7.71σ	12.92σ

NOTE—Refer to note in Table B.2.

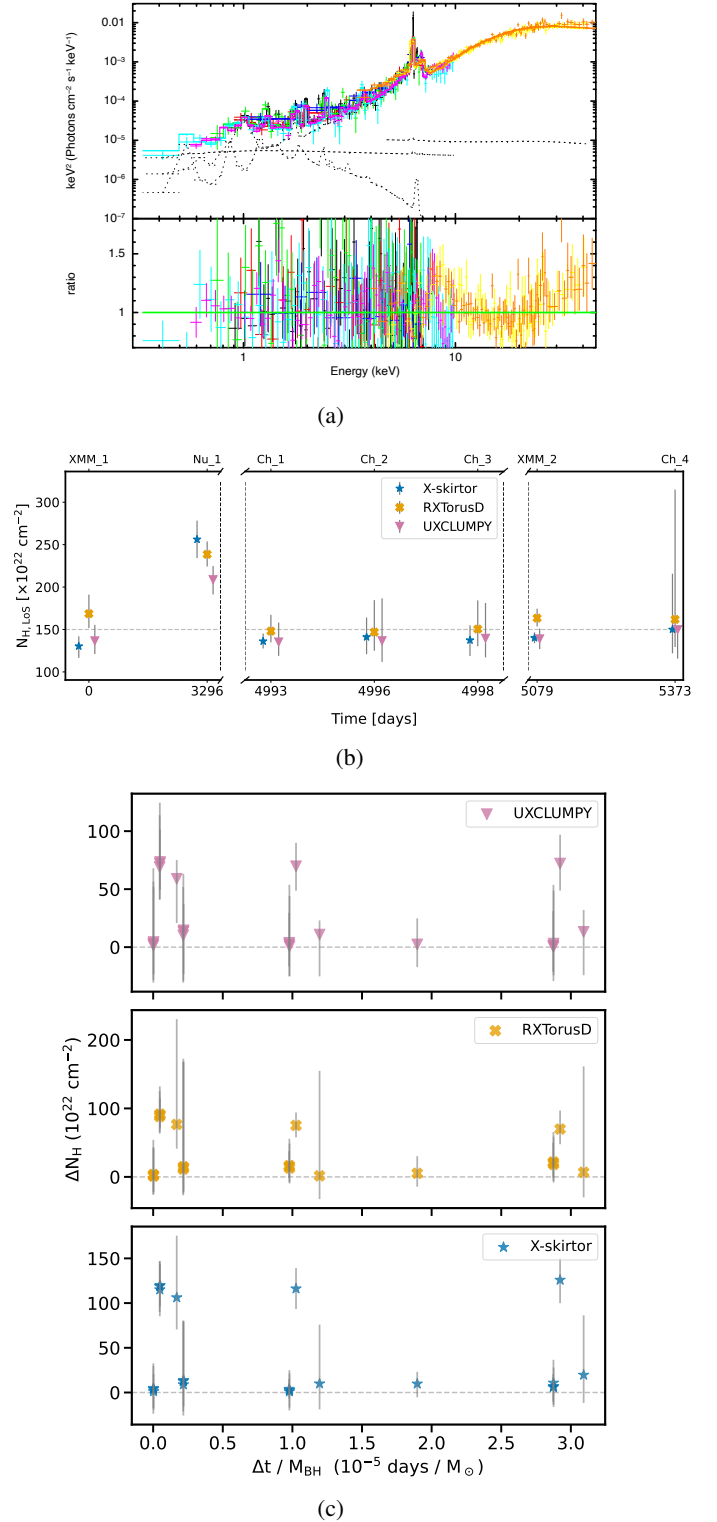
**Figure 12.** NGC 1194. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black, red, green, and blue), *XMM-Newton* (in cyan and pink), and *NuSTAR* (FPMA and FPMB spectra are grouped together in yellow and orange) spectra are shown. See Appendix C for more information on the residuals in the fit of the *NuSTAR* data. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in logarithmic scale for the left and right panel, linear for the middle panel, with a visual break to compress the long timescale between observations. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.8. NGC 2655: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	0.74 ± 0.05	$0.74^{+0.05}_{-0.05}$	0.82 ± 0.17
Comptonized primary continuum			
Γ	$2.06^{+0.19}_{-0.17}$	$2.08^{+0.19}_{-0.14}$	$2.02^{+0.13}_{-0.11}$
Neutral reflector			
C_f^+	$0.45^{+0.20}_{-0.12}$	$0.61^{+0.11}_{-0.21}$	$0.006^{+0.004}_{-0.007}$
θ / deg	61_{-11}	54^{+17}_{-14}	60^f
σ_{tor} / deg	/	/	0^f
F_s / 10^{-2}	$1.95^{+2.04}_{-0.91}$	$3.05^{+2.46}_{-1.55}$	$0.08^{+2.26}_{-0.78}$
norm / 10^{-3}	$1.06^{+0.93}_{-0.54}$	$0.71^{+0.94}_{-0.33}$	$4.16^{+3.34}_{-0.03}$
$N_{\text{H,eq}}$ / 10^{22} cm^{-2}	$10.00^{+12.39}_{-6.24}$	$100.02^{+368.63}_{-62.20}$	/
$N_{\text{H,inst,num}}$ (LoS hydrogen column density)			
N_{H}^{Ch} / 10^{22} cm^{-2}	$31.42^{+7.27}_{-11.70}$	$25.88^{+22.55}_{-6.18}$	$26.76^{+8.47}_{-5.26}$
$N_{\text{H}}^{\text{XMM}}$ / 10^{22} cm^{-2}	$40.86^{+11.21}_{-14.78}$	$33.51^{+27.48}_{-6.52}$	$32.32^{+7.56}_{-6.71}$
$N_{\text{H}}^{\text{NuS,1}}$ / 10^{22} cm^{-2}	$44.20^{+21.66}_{-16.76}$	$32.94^{+32.94}_{-17.67}$	$33.43^{+15.30}_{-15.49}$
$N_{\text{H}}^{\text{NuS,2}}$ / 10^{22} cm^{-2}	$30.68^{+9.88}_{-14.31}$	$21.40^{+22.68}_{-8.08}$	$20.02^{+9.64}_{-7.88}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1^f	1^f	1^f
C_{XMM}	$2.28^{+0.67}_{-0.51}$	$2.16^{+0.64}_{-0.42}$	$1.96^{+0.41}_{-0.34}$
$C_{\text{NuS,1}}$	$2.83^{+1.73}_{-1.06}$	$2.43^{+5.09}_{-0.77}$	$2.69^{+1.28}_{-0.97}$
$C_{\text{NuS,2}}$	$2.04^{+0.85}_{-0.69}$	$1.92^{+0.75}_{-0.48}$	$2.56^{+0.82}_{-0.88}$
Statistic			
C-stat/d.o.f.	260/242	264/242	245/244
T	1.16σ	1.41σ	0.02σ
p-value	0.75	0.85	0.74
Statistic (No variability)			
C-stat/d.o.f.	375/248	374/248	362/250
T	8.06σ	8.00σ	7.08σ
Statistic (No flux variability)			
C-stat/d.o.f.	349/245	303/245	317/247
T	6.64σ	3.71σ	4.45σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	269/245	270/245	259/247
T	0.76σ	1.60σ	1.53σ

NOTE—Refer to note in Table B.2.

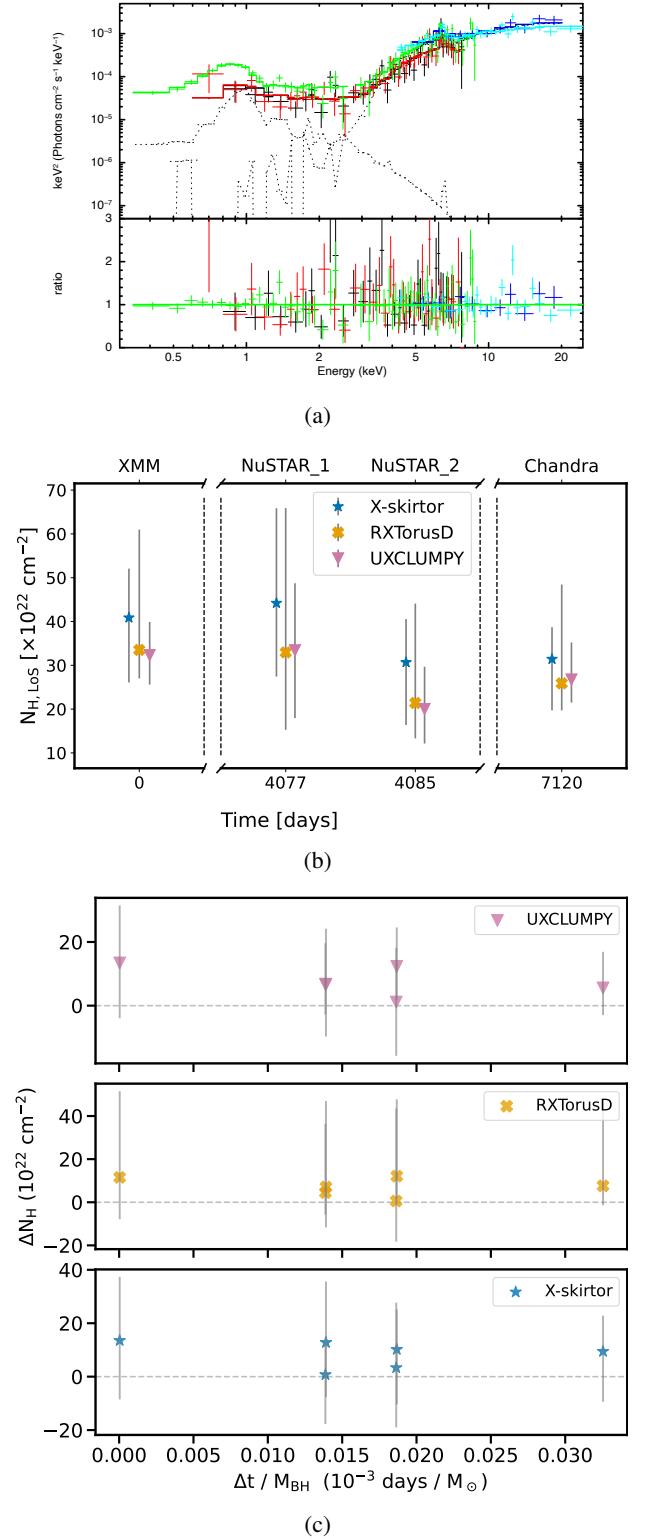
**Figure 13.** NGC 2655. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black and red), *XMM* (in green) and *NuSTAR* (FPMA and FPMB grouped together in cyan and blue) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in linear scale with a visual break to compress the long timescale between observations. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.9. NGC 4785: spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	0.31 ^{+0.04} _{-0.03}	0.30 ^{+0.03} _{-0.02}	0.31 ^{+0.04} _{-0.03}
Comptonized primary continuum			
Γ	1.88 ^{+0.10} _{-0.17}	1.97 ^{+0.10} _{-0.20}	1.95 ^{+0.07} _{-0.10}
Neutral reflector			
C_f +	0.55 ^{+0.05} _{-0.07}	0.52 ^{+0.26} _{-0.12}	0.40 ^{+0.12} _{-0.05}
θ / deg	60 ^f	60 ^f	60 ^f
σ_{tor} / deg	/	/	0 ^f
F_s / 10 ⁻²	0.61 ^{+0.27} _{-0.14}	0.49 ^{+0.29} _{-0.12}	2.03 ^{+0.53} _{-0.73}
norm / 10 ⁻³	2.11 ^{+0.84} _{-0.77}	2.76 \pm 0.11	3.12 ^{+0.11} _{-0.89}
$N_{\text{H,eq}}$ / 10 ²² cm ⁻²	323.59 ^{+434.92} _{-133.05}	242.33 ^{+100.58} _{-69.99}	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
N_{H}^{Ch} / 10 ²² cm ⁻²	36.75 ^{+6.25} _{-5.52}	43.28 ^{+7.58} _{-6.63}	37.03 ^{+2.67} _{-6.20}
$N_{\text{H}}^{\text{XMM,1}}$ / 10 ²² cm ⁻²	60.07 ^{+6.57} _{-5.53}	72.05 ^{+10.07} _{-8.17}	60.76 ^{+7.51} _{-6.60}
$N_{\text{H}}^{\text{XMM,2}}$ / 10 ²² cm ⁻²	49.18 ^{+6.35} _{-5.35}	55.97 ^{+7.76} _{-6.42}	49.81 ^{+4.46} _{-5.41}
$N_{\text{H}}^{\text{XMM,3}}$ / 10 ²² cm ⁻²	40.63 ^{+5.20} _{-4.43}	48.14 ^{+6.35} _{-5.52}	39.53 ^{+5.12} _{-3.54}
$N_{\text{H}}^{\text{NuS,2}}$ / 10 ²² cm ⁻²	80.42 ^{+33.26} _{-24.79}	97.17 ^{+104.86} _{-36.39}	83.43 ^{+27.43} _{-25.71}
$N_{\text{H}}^{\text{NuS,3}}$ / 10 ²² cm ⁻²	100.72 ^{+21.82} _{-15.36}	134.40 ^{+135.03} _{-32.70}	104.02 ^{+19.24} _{-13.58}
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1 ^f	1 ^f	1 ^f
$C_{\text{XMM,1}}$	1.16 ^{+0.35} _{-0.25}	1.09 ^{+0.32} _{-0.23}	1.19 ^{+0.38} _{-0.25}
$C_{\text{XMM,2}}$	0.96 ^{+0.30} _{-0.22}	0.88 ^{+0.27} _{-0.19}	0.97 ^{+0.33} _{-0.22}
$C_{\text{XMM,3}}$	0.83 ^{+0.26} _{-0.19}	0.64 ^{+0.25} _{-0.18}	0.79 ^{+0.27} _{-0.17}
$C_{\text{NuS,2}}$	0.39 ^{+0.22} _{-0.14}	0.34 ^{+0.36} _{-0.11}	0.39 ^{+0.24} _{-0.14}
$C_{\text{NuS,3}}$	1.24 ^{+0.50} _{-0.33}	0.76 ^{+0.50} _{-0.29}	1.33 ^{+0.51} _{-0.37}
Statistic			
$\chi^2/\text{d.o.f.}$	414/372	430/372	431/373
T	2.18 σ	3.00 σ	3.00 σ
p-value	3.35e-07	2.91e-08	0
Statistic (No variability)			
$\chi^2/\text{d.o.f.}$	1839/385	1558/385	1608/386
T	74.10 σ	59.78 σ	62.20 σ
Statistic (No flux variability)			
$\chi^2/\text{d.o.f.}$	448/378	468/378	467/379
T	3.60 σ	4.63 σ	4.52 σ
Statistic (No N_{H} variability)			
$\chi^2/\text{d.o.f.}$	515/378	523/378	505/379
T	7.05 σ	7.46 σ	6.47 σ

NOTE—Refer to note in Table B.2.

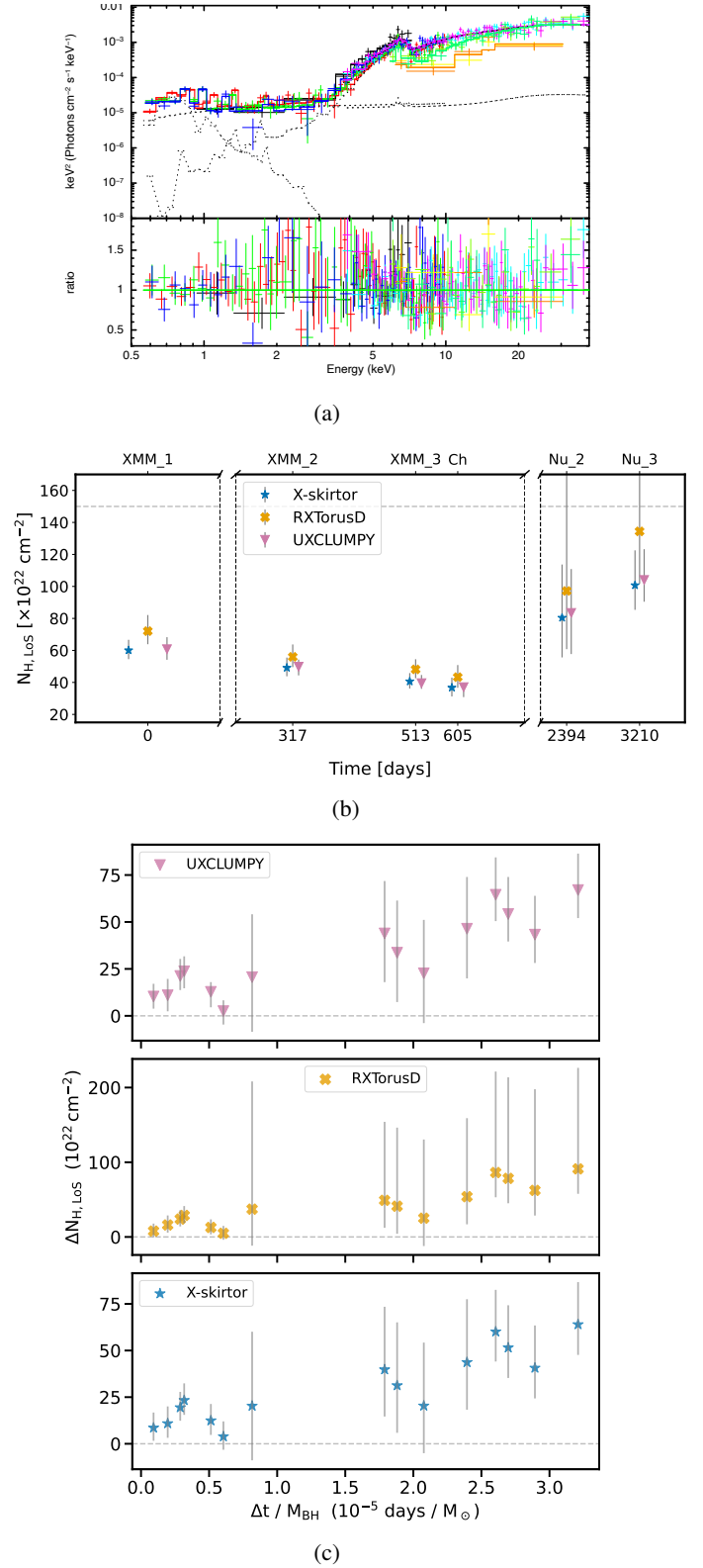
**Figure 14.** NGC 4785. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), XMM (in red, green, and blue) and *NuSTAR* (FPMA and FPMB grouped together in cyan, blue, pink, yellow, and orange) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in logarithmic scale with a visual break to compress the long timescale between observations. The gray dashed line shows the CTK threshold. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.10. UGC 3752: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT_1 / keV	$0.13^{+0.03}_{-0.08}$	$0.13^{+0.04}_{-0.09}$	$0.13^{+0.03}_{-0.07}$
kT_2 / keV	0.69 ± 0.06	$0.62^{+0.06}_{-0.06}$	0.70 ± 0.06
Comptonized primary continuum			
Γ	$1.49^{+0.12}_{-0.17}$	$1.65^{+0.20}_{-0.36}$	$1.54^{+0.12}_{-0.11}$
Neutral reflector			
C_f^+	$0.45^{+0.12}_{-0.11}$	$0.53^{+0.09}_{-0.07}$	$0.46^{+0.17}_{-0.12}$
θ / deg	60^f	60^f	60^f
σ_{tor} / deg	/	/	$28.16^{+34.07}_{-5.53}$
$F_s / 10^{-2}$	$2.14^{+1.08}_{-0.69}$	$1.30^{+0.65}_{-0.43}$	$1.17^{+0.12}_{-0.34}$
norm / 10^{-3}	$0.52^{+0.37}_{-0.24}$	$0.88^{+0.61}_{-0.38}$	$0.46^{+0.33}_{-0.20}$
$N_{\text{H,eq}} / 10^{22} \text{ cm}^{-2}$	$14.79^{+60.26}_{-2.88}$	$412.13^{+131.87}_{-273.79}$	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
$N_{\text{H}}^{\text{Ch}} / 10^{22} \text{ cm}^{-2}$	$71.24^{+40.08}_{-22.51}$	$88.39^{+57.57}_{-28.43}$	$52.27^{+17.01}_{-15.43}$
$N_{\text{H}}^{\text{XMM}} / 10^{22} \text{ cm}^{-2}$	$58.43^{+10.26}_{-8.77}$	$73.57^{+82.64}_{-14.43}$	$47.29^{+8.65}_{-8.23}$
$N_{\text{H}}^{\text{NuS,1}} / 10^{22} \text{ cm}^{-2}$	$89.22^{+19.31}_{-16.26}$	$133.52^{+61.60}_{-26.35}$	$95.67^{+15.88}_{-17.37}$
$N_{\text{H}}^{\text{NuS,2}} / 10^{22} \text{ cm}^{-2}$	$180.79^{+41.00}_{-32.89}$	$200.20^{+58.12}_{-42.16}$	$171.42^{+41.17}_{-34.22}$
$N_{\text{H}}^{\text{NuS,3}} / 10^{22} \text{ cm}^{-2}$	$221.09^{+135.36}_{-105.38}$	$188.33^{+22.15}_{-17.71}$	$131.77^{+89.28}_{-43.28}$
$N_{\text{H}}^{\text{NuS,4}} / 10^{22} \text{ cm}^{-2}$	$106.50^{+18.74}_{-26.05}$	$133.61^{+61.36}_{-58.03}$	$108.85^{+36.85}_{-14.43}$
$N_{\text{H}}^{\text{NuS,5}} / 10^{22} \text{ cm}^{-2}$	$34.75^{+6.75}_{-7.71}$	$26.62^{+9.89}_{-20.06}$	$35.30^{+6.65}_{-5.45}$
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1^f	1^f	1^f
C_{XMM}	$1.66^{+0.86}_{-0.54}$	$1.62^{+0.71}_{-0.46}$	$1.94^{+1.14}_{-0.61}$
$C_{\text{NuS,1}}$	$2.00^{+1.74}_{-1.06}$	$2.32^{+1.80}_{-0.99}$	$3.42^{+2.52}_{-1.44}$
$C_{\text{NuS,2}}$	$2.34^{+1.11}_{-0.71}$	$0.68^{+1.86}_{-1.72}$	$3.98^{+2.45}_{-1.55}$
$C_{\text{NuS,3}}$	$2.36^{+1.16}_{-0.75}$	$0.99^{+1.62}_{-0.98}$	$2.85^{+1.77}_{-1.47}$
$C_{\text{NuS,4}}$	$2.12^{+1.43}_{-0.94}$	$1.12^{+1.86}_{-1.70}$	$3.58^{+2.26}_{-1.50}$
$C_{\text{NuS,5}}$	$2.17^{+3.19}_{-3.04}$	$0.80^{+1.30}_{-1.32}$	$3.42^{+2.20}_{-1.26}$
Statistic			
C-stat/d.o.f.	422/423	453/423	431/423
T	0.05σ	1.46σ	0.39σ
p-value	0	0	0
Statistic (No variability)			
C-stat/d.o.f.	2647/435	2598/435	2630/435
T	106.06σ	98.92σ	105.24σ
Statistic (No flux variability)			
C-stat/d.o.f.	474/429	470/429	462/429
T	2.17σ	1.98σ	1.59σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	711/429	656/429	721/429
T	13.62σ	10.96σ	14.10σ

NOTE—Refer to note in Table B.2.

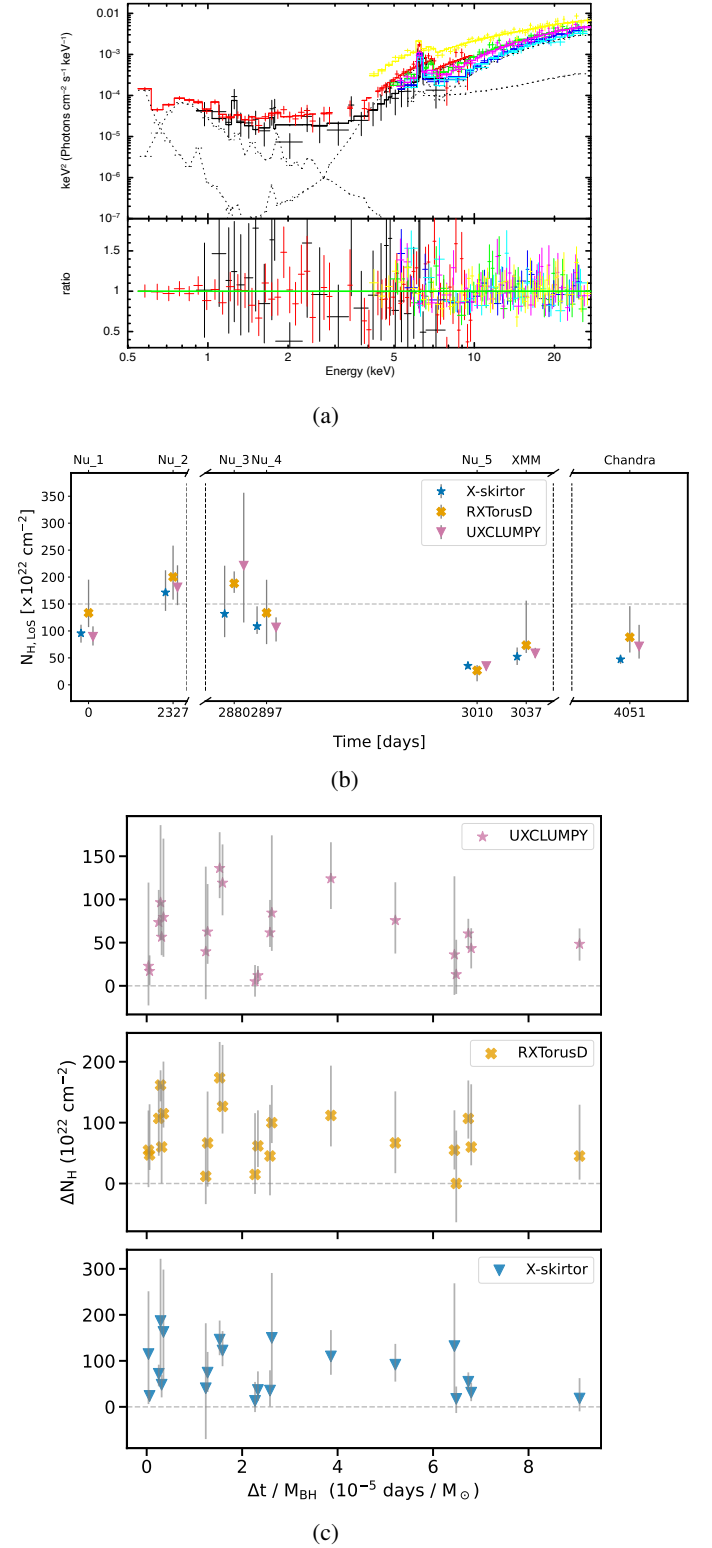
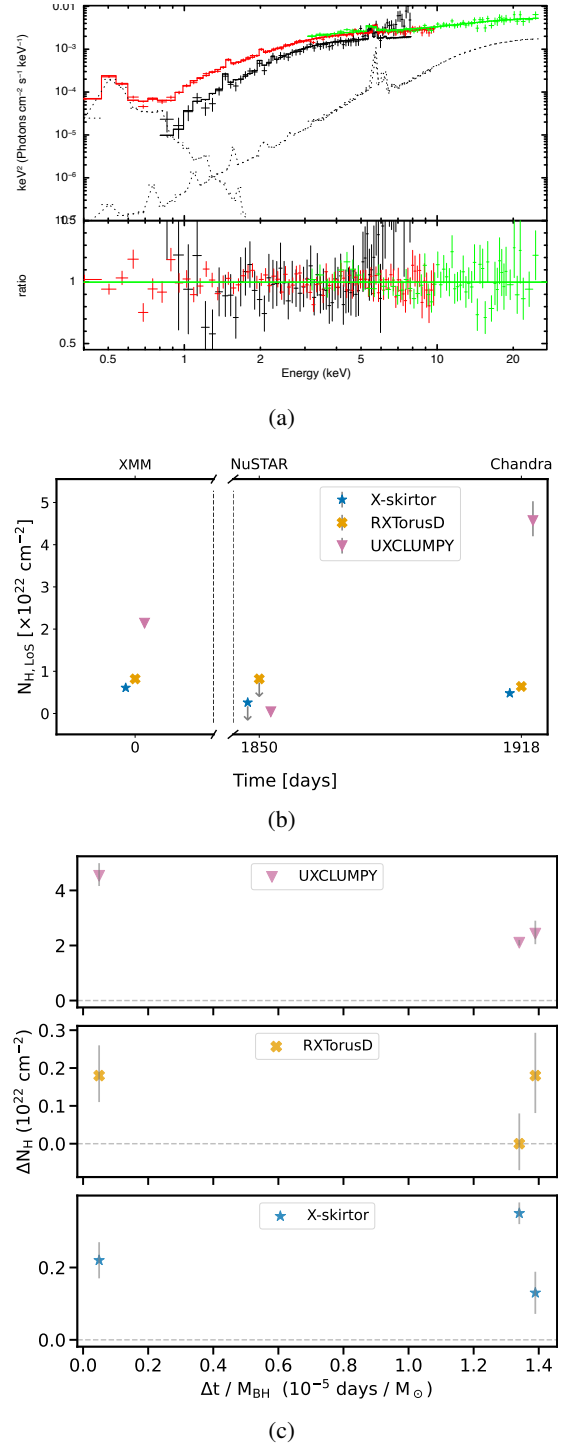
**Figure 15.** UGC 3752. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), *XMM* (in red) and *NuSTAR* (FPMA and FPMB grouped together in green, blue cyan, pink, and yellow) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in logarithmic scale for the left and middle panels, linear for the right panel, with visual breaks to compress the long timescale between observations. The gray dashed line shows the CTK threshold. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

Table B.11. WISE J144850.99-400845.6: best-fit spectral analyses for each torus model.

Parameter	xskirtor	RXTorusD	UXCLUMPY
apec (Thermal emission)			
kT / keV	0.20±0.01	0.19±0.01	0.21±0.01
Comptonized primary continuum			
Γ	1.70 ^{+0.04} _{-0.05}	1.73 ^{+0.05} _{-0.03}	1.66±0.04
Neutral reflector			
C_f^+	0.65 _{-0.32}	0.69 _{-0.18}	0.34 ^{+0.02} _{-0.03}
θ / deg	60 ^f	60 ^f	60 ^f
σ_{tor} / deg	/	/	0.91 ^{+0.42} _{-0.30}
F_s / 10 ⁻²	22.37 ^{+1.37} _{-1.31}	0.21 ^{+0.03} _{-0.03}	7.80 ^{+0.02} _{-0.01}
norm / 10 ⁻³	0.84 ^{+0.09} _{-0.08}	0.90 ^{+0.06} _{-0.05}	2.47 ^{+0.38} _{-0.40}
$N_{\text{H,eq}}$ / 10 ²² cm ⁻²	126.60 ^{+561.41} _{-53.02}	197.92 ^{+207.99} _{-86.57}	/
$N_{\text{H,inst,num.}}$ (LoS hydrogen column density)			
N_{H}^{Ch} / 10 ²² cm ⁻²	0.48±0.05	0.64 ^{+0.08} _{-0.07}	4.57 ^{+0.46} _{-0.37}
$N_{\text{H}}^{\text{XMM}}$ / 10 ²² cm ⁻²	0.61±0.03	0.82 ^{+0.08} _{-0.07}	2.14±0.10
$N_{\text{H}}^{\text{NuS}}$ / 10 ²² cm ⁻²	0.001 ^{+0.26}	0.001 ^{+0.82}	0.04±0.01
$C_{\text{inst,num}}$ (Cross-normalization constant)			
C_{Ch}	1 ^f	1 ^f	1 ^f
C_{XMM}	1.43±0.05	1.43 ^{+0.05} _{-0.04}	2.03 ^{+0.27} _{-0.24}
C_{NuS}	1.55±0.07	1.53±0.07	1.55 ^f
Statistic			
C-stat/d.o.f.	329/259	336/259	318/259
T	4.33 σ	4.78 σ	3.66 σ
p-value	1.11e-16	9.38e-7	0
Statistic (No variability)			
C-stat/d.o.f.	1313/263	957/263	1350/263
T	64.77 σ	42.94 σ	67.01 σ
Statistic (No flux variability)			
C-stat/d.o.f.	667/261	624/261	401/261
T	25.14 σ	22.47 σ	8.69 σ
Statistic (No N_{H} variability)			
C-stat/d.o.f.	353/261	414/261	530/261
T	5.68 σ	9.47 σ	16.68 σ

NOTE—Refer to note in Table B.2.

**Figure 16.** WISE J144850.99-400845.6. *Panel a:* Best-fit with the UXCLUMPY torus model. The *Chandra* (in black), *XMM-Newton* (in red), and *NuSTAR* (FPMA and FPMB spectra are grouped together in green) spectra are shown. *Panel b:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in linear scale with a visual break to compress the long timescale between observations. The gray arrows show the upper limits obtained for the *NuSTAR* observation during the fit with X-skirtor and RXTorusD models. *Panel c:* Variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass. Panels b and c adopt the same color code as Fig. 7.

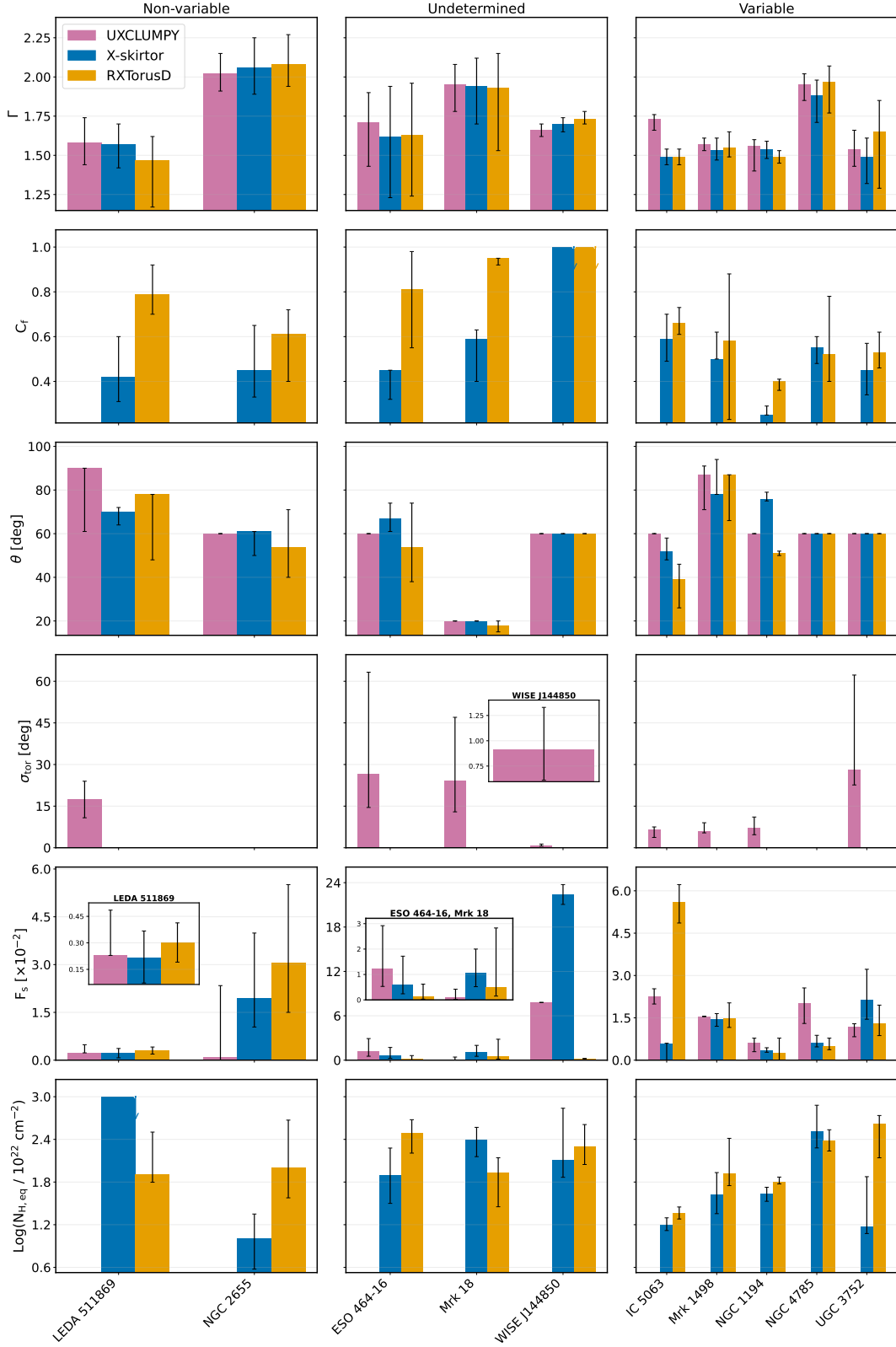


Figure 17. Distributions of the torus parameters grouped by variability class. *Rows:* 1) photon index Γ ; 2) covering factor C_f ; 3) inclination angle θ ; 4) vertical extent of the cloud population σ_{tor} ; 5) scattering fraction of the primary continuum F_s ; 6) equatorial column density $N_{\text{H,eq}}$. Each bar shows the best-fit value of each torus models (UXCLUMPY in pink, X-skirtor in blue, and RXTorusD in yellow) with asymmetric uncertainties at 90% c.l.. *Left panels* present the Non-variable, *middle panels* the Undetermined, and *right panels* the Variable AGN samples. Insets are included to improve the visualization of AGN with low best-fit values. Within the current sample, no statistically significant differences are present among variability classes for the torus and continuum parameters.

C. NOTES AND GENERAL DETAILS ON SINGLE SOURCES

ESO 464-G016 is a Seyfert 2 galaxy (Y.-P. Chen et al. 2022) and a candidate Compton-thick (S. Marchesi et al. 2019) AGN. However, our multi-epoch analysis shows that, for only one observation of a specific model (UXCLUMPY), the line-of-sight column density ($N_{\text{H,LoS}}$) reaches an upper limit exceeding the CTK threshold ($> 1.5 \times 10^{24} \text{ cm}^{-2}$). Based on this, we adopt a conservative approach and classify ESO 464-G016 as Compton-thin (see Sect. 5.1). For the variability classification, the $N_{\text{H,LoS}}$ values derived across different epochs are consistent within their uncertainties, suggesting no variability. The statistical tests yield mixed indications: the p-value test favors no variability, whereas the tension test is inconclusive, resulting in a final classification of Undetermined AGN (see Sect. 5.2 and Table 3). The intrinsic flux variability tests under the no-variability hypothesis return tensions below 5, comparable to those obtained for the best-fit and the other hypotheses (see Table B.2). This indicates that allowing for variability does not significantly improve the fit.

IC 5063 is a radio-loud (R. Morganti et al. 2013) Seyfert 2 (M. P. Véron-Cetty & P. Véron 2006) AGN. Our multi-epoch analysis classify this AGN as Compton-thin (see Sect. 5.1). During the fit, the residuals in the *Chandra* spectra are modeled with a Gaussian component at $E = 1.33^{+0.02}_{-0.05}$ keV. The tension derived from the best-fit obtained with RXTorusD and UXCLUMPY models is above 3, which is due to residuals present in *NuSTAR*/FPMB instrument. We tested the inclusion of Gaussian components that could reduce the tension below 3; however, these additional Gaussians lack any clear physical interpretation. Therefore, we chose not to include them in the best-fit and retained the value of $T > 3$. Despite this, when testing the no $N_{\text{H,LoS}}$ variability hypothesis, the resulting tensions for the two models are 14.53 and 21.33 (respectively), both significantly higher than the T values obtained in the best-fit. Consequently, we classify the source as $N_{\text{H,LoS}}$ Variable (see Sect. 5.2 and Table 3). Moreover, the tensions associated with the no-variability and no-flux variability tests are all well above 5, indicating that flux variability is also required to adequately reproduce the spectral properties of this source (see Table B.3).

LEDA 511869 is a Seyfert 2 galaxy (R. Landi et al. 2007). Our multi-epoch analysis classify this AGN as Compton-thin (see Sect. 5.1). Regarding the variability classification, the best-fit $N_{\text{H,LoS}}$ values across different epochs are within uncertainties, indicating no significant absorption variability. This result is confirmed by both statistical tests, which classify the source as Non-Variable (see Sect. 5.2 and Table 3). However, the no-variability tests show that the source cannot be reproduced under the hypothesis of constant spectral pa-

rameters (i.e., the tensions are higher than 5, see Table B.4). Both intrinsic flux variability and $N_{\text{H,LoS}}$ variability, when allowed independently, are capable of compensating for the other and provide acceptable fits. Therefore, while variability is required to explain the data, the current analysis does not allow us to determine its physical origin.

MCG-03-34-064 is a Seyfert 1.8 (M. P. Véron-Cetty & P. Véron 2006) AGN, candidate to host a dual system (A. Trindade Falcão et al. 2024). As discussed in Sec. 8, the X-ray spectrum of MCG-03-34-064 presents several significant ($>3\sigma$) emission and absorption lines. In the soft band, we identify (and model with Gaussian lines) prominent emission lines at 0.54 ± 0.01 keV, 1.07 ± 0.01 keV, and at 1.80 ± 0.02 keV. The Fe K band is known to be complex (G. Miniutti et al. 2007), and we detect both emission and absorption features. The Fe $K\alpha$ emission line is detected at 6.39 ± 0.01 keV and is intrinsically broadened ($\sigma = 100^{+12}_{-11}$ eV), with a large equivalent width ~ 200 eV. These properties indicate a possible origin in BLR-scale material or the inner regions of the obscuring torus. In addition, we detect an unresolved absorption feature at $7.23^{+0.10}_{-0.04}$ keV, consistent with blueshifted Fe XXVI $\text{Ly}\alpha$ absorption and suggestive of highly ionized outflowing gas. A detailed characterization of this absorber is beyond the scope of this work. According to the p-value test applied to the best-fit $N_{\text{H,LoS}}$ values (see Sect. 8), $N_{\text{H,LoS}}$ variability is detected in MCG-03-34-064. However, this result should be treated cautiously, as the fit is not robust and fails to reproduce the iron band.

Mrk 18. This galaxy is identified as a Seyfert 2 AGN. Our multi-epoch analysis classify this AGN as Compton-thin (see Sect. 5.1). During the fitting procedure, we found that the inclination angle was unconstrained for both X-skirtor and UXCLUMPY while it was well constrained for RXTorusD. Therefore, instead of adopting 60° (as per methodology), we fixed the inclination to 20° for X-skirtor and UXCLUMPY consistent with the value obtained for RXTorusD. Moreover, we allowed the normalization of the apec component to vary independently between the *Chandra* ($2.14^{+4.11}_{-1.96} \times 10^{-5}$), *NuSTAR* (fixed to 0), and XMM observation ($3.47 \pm 0.25 \times 10^{-5}$). This choice is motivated by the different extraction radii used for the two instruments: the larger XMM extraction region may include part of the star-forming region (SFR) emission, whereas this contribution is likely absent in the *Chandra* data due to its smaller extraction radius. Regarding the $N_{\text{H,LoS}}$ variability, the first-order analysis shows that the best-fit values for different epochs are consistent within uncertainties, indicating no significant variability. This result is supported by both statistical tests, which classify the AGN as Non-variable (see Sect. 5.2 and Table 3). In contrast, the no-variability tests yield tensions above 5, indicating the presence of intrinsic flux variability (see Table B.5).

Mrk 1498 is a Compton-thin (e.g., S. Eguchi et al. 2009; F. Ursini et al. 2018) Seyfert 1.9 (M. P. Véron-Cetty & P. Véron 2006) AGN. Our multi-epoch analysis confirms the Compton-thin nature of this AGN (see Sect. 5.1). We note that the adopted models are not able to properly model the iron K band and residuals are present. We thus add an unresolved Gaussian (width fixed to 0 keV, significance $\sim 4\sigma$) at energy 6.21 ± 0.05 keV, which is likely associated with low-ionization states of the Fe K α emission line.

For this source, the tension values for the no $N_{\text{H,LoS}}$ variability hypothesis are close to 5 for both *RXTorusD* and *UXCLUMPY* and exceed 5 for *X-skirtor*. Therefore, we classify the source as Variable, even though the tension test alone would render the classification formally Undetermined. We note, however, that the T values obtained under the no intrinsic flux variability hypothesis are quite low, comparable to those derived from the best-fit. Hence, we are unable to distinguish whether the observed variability arises from changes in the neutral column density or in the intrinsic flux (see Sect. 5.2 and Tables 3 and B.6).

NGC 1194 has been classified as a Compton-thick (C. Y. Kuo et al. 2011; P. Severgnini et al. 2012; S. Marchesi et al. 2018) radio-loud Seyfert 1.9 (M. P. Véron-Cetty & P. Véron 2006) galaxy with megamaser emission (C. Y. Kuo et al. 2011; E. Fedorova et al. 2016). Our results, considering all three models, confirm the Compton-thick nature of the source, with two observations (*Chandra_2* taken on 2019-10-27, and *Chandra_4* on 2020-11-05) showing column densities above the CTK threshold (i.e., $N_{\text{H,LoS}} > 1.5 \times 10^{24} \text{ cm}^{-2}$) even when accounting for the lower uncertainties (see Sect. 5.1). To model the significant emission features in the soft X-ray band and Fe K complex, we use three Gaussian components. Concerning the soft spectrum, emission lines at $E = 1.33_{-0.02}^{+0.01}$ keV and at $E = 1.80 \pm 0.02$ are observed. Meanwhile, a moderately broad emission line is detected at $E = 6.64_{-0.02}^{+0.01}$ with width $\sigma = 80 \pm 50$ eV and equivalent width $EW = 500 \pm 100$ eV. Its energy is consistent with He-like Fe XXV K α emission, likely originating from hot, ionized gas in the inner regions of the AGN, such as the broad-line region or circumnuclear photoionized material. We note that some residuals are present in the *NuSTAR* fit with the *UXCLUMPY* model (see Fig. 12). These residuals are not seen with *X-skirtor* and *RXTorusD*, and the best-fit parameters are consistent across models, indicating that the *UXCLUMPY* fit remains reliable.

Regarding variability, the first-order analysis reveals significant $N_{\text{H,LoS}}$ variations across different epochs. This result is confirmed by both statistical tests, which consistently classify *NGC 1194* as Variable (see Sect. 5.2 and Table 3). In addition, the no-flux variability tests yield tensions above 5, indicating also the presence of intrinsic flux variability (see Table B.7).

NGC 2655 is a Seyfert 2 (M. P. Véron-Cetty & P. Véron 2006) galaxy and low-luminosity AGN (N. M. Nagar et al. 2002). Our multi-epoch analysis classify this AGN as Compton-thin (see Sect. 5.1). All tests indicate no variability in $N_{\text{H,LoS}}$, while the AGN results variable in intrinsic flux (see Sect. 5.2 and Tables 3 and B.8).

NGC 4785 is a Seyfert 2 (M. P. Véron-Cetty & P. Véron 2006) previously classified as Compton-thick (P. Gandhi et al. 2015) AGN. However, our multi-epoch analysis shows that, for only one observation of a specific model (*RXTorusD*), the line-of-sight column density ($N_{\text{H,LoS}}$) reaches an upper limit exceeding the CTK threshold ($> 1.5 \times 10^{24} \text{ cm}^{-2}$). Based on this, we adopt a conservative approach and classify *NGC 4785* as a Compton-thin AGN (see Sect. 5.1). Given that no direct BH mass measurement is present in the literature for *NGC 4785*, we adopt a value of $\log(M_{\text{BH}}/M_{\odot}) \simeq 8.0$. This estimate is inferred from the stellar velocity dispersion of the host galaxy ($\sigma_{\star} \approx 187 \text{ km s}^{-1}$; E. Oliva et al. 1999) via the M - σ relation (e.g., K. Gültekin et al. 2009) and lies within the ~ 0.4 dex intrinsic scatter of the relation. Residuals are present in the *XMM* and *Chandra* spectra. We find two significant features, which are modeled with Gaussian components, at $E = 1.33_{-0.06}^{+0.05}$ keV and at $E = 0.98 \pm 0.03$ keV. Similarly to *Mrk 18*, during the fitting procedure we disentangled the normalization of the *apec* component between the *XMM* and *Chandra-NuSTAR* spectra for all three models. We subsequently fixed the latter normalization to zero, as it was unconstrained, while the normalization for the *XMM-Newton* spectra was found to be $(1.61_{-0.30}^{+0.31}) \times 10^{-5}$. All tests consistently indicate the presence of variability in $N_{\text{H,LoS}}$. However, intrinsic flux variability cannot be firmly established, as the tension does not exceed the adopted threshold of 5 (see Sect. 5.2 and Tables 3 and B.9).

UGC 3752 is a Seyfert 2 (M. P. Véron-Cetty & P. Véron 2006) AGN. During the analysis, two *apec* components are used to model the soft X-ray spectrum. Following our spectral fitting, we find that the inferred line-of-sight column density shows significant variability across epochs and models. In particular, the *RXTorusD* model yields column densities whose upper limits exceed the Compton-thick threshold for the *XMM-Newton* observation and for several *NuSTAR* pointings, including the observation obtained on 2021-10-22, for which the best-fit value itself lies in the Compton-thick regime. In contrast, the *X-skirtor* and *UXCLUMPY* models generally favor Compton-thin solutions, with Compton-thick values reached only at the upper end of the uncertainty range in a subset of *NuSTAR* observations, while other epochs remain fully consistent with a Compton-thin absorber. Overall, these results support the classification of *UGC 3752* as a candidate changing-obscuraton AGN, possibly undergoing tran-

sitions between Compton-thin and Compton-thick state (see Sect. 5.1). From the first order and statistical tests, $N_{\text{H,LoS}}$ variability is clearly detected in UGC 3752 (see Sect. 5.2 and Tables 3). The tension associated with the no-variability test is above $T = 5$, indicating that variability is indeed required by the data. However, the no-flux variability test yields tensions well below 5, suggesting that absorption variability is predominantly driving the observed spectral variability (see Table B.10).

WISE J144850.99-400845.6 is a Seyfert 1.2 galaxy (A. Malizia et al. 2016). Our multi-epoch analysis classify this AGN as Compton-thin (see Sect. 5.1). During the fitting process for this source, the cross-normalization constant of the *NuSTAR* data in the UXCLUMPY model, when left free to vary, tends to a nonphysical value of ~ 17 . When fixed to 1.55 (value consistent with the best-fit obtained for the other two models), the resulting fit is very similar in terms of C-stat/d.o.f. to those models. Therefore, we decided to fix the cross-normalization constant to 1.55 in the final best-fit. *WISE J144850* is listed in Table 3 as first-order undetermined, i.e., based on whether $N_{\text{H,LoS}}$ values from different observations fall within each other's uncertainties, due to the upper limits derived during *RXTorusD* and *X-skirtor* fits, which prevent a definitive classification. The statistical tests also yield mixed indications: the p-value test favors variability, while the tension test is inconclusive, resulting in a final classification of an Undetermined AGN (see Sect. 5.2 and Tables 3). The intrinsic flux variability tests under the no-variability hypothesis yield tensions > 5 , suggesting the presence of flux variability (see Table B.11).

D. STATISTICAL COMPARISON OF THE PARAMETER DISTRIBUTIONS

Table D.12. Statistical comparison of parameter distributions for the three adopted models across variability classes.

(1) Parameter	(2) NV Median	(3) U Median	(4) V Median	(5) KW p-value	(6) KS p-value
UXCLUMPY					
$N_{H,LoS}$	51.14	12.18	49.81	0.42	NV vs U: 0.60 NV vs V: 0.95 U vs V: 0.28
$\sigma(C_{inst.})$	0.41	0.26	0.19	0.87	NV vs U: 0.90 NV vs V: 0.57 U vs V: 0.96
Γ	1.80	1.71	1.57	0.45	NV vs U: 0.91 NV vs V: 0.57 U vs V: 0.47
C_f	0.15	0.30	0.30	0.79	NV vs U: 1.00 NV vs V: 0.95 U vs V: 0.86
θ	75.00	60.00	60.00	0.22	NV vs U: 0.69 NV vs V: 0.29 U vs V: 0.64
σ_{tor}	8.66	24.03	5.97	0.45	NV vs U: 0.60 NV vs V: 0.71 U vs V: 0.29
F_s	0.15	1.24	2.03	0.17	NV vs U: 0.61 NV vs V: 0.10 U vs V: 0.67
RXTorusD					
$N_{H,LoS}$	49.60	16.96	55.97	0.41	NV vs U: 0.60 NV vs V: 0.96 U vs V: 0.29
$\sigma(C_{inst.})$	0.31	0.20	0.22	0.86	NV vs U: 0.60 NV vs V: 0.58 U vs V: 0.96
Γ	1.77	1.73	1.55	0.70	NV vs U: 0.90 NV vs V: 0.81 U vs V: 0.46
C_f	0.70	0.81	0.53	0.04	NV vs U: 0.59 NV vs V: 0.28 U vs V: 0.04
θ	66.00	54.00	60.00	0.61	NV vs U: 0.80 NV vs V: 0.95 U vs V: 0.90
F_s	1.68	0.21	1.30	0.23	NV vs U: 0.60 NV vs V: 1.00 U vs V: 0.29
$N_{H,eq}$	90.48	197.92	82.58	0.58	NV vs U: 0.60 NV vs V: 0.96 U vs V: 0.46

(1) Parameter	(2) NV Median	(3) U Median	(4) V Median	(5) KW p-value	(6) KS p-value
X-skirtor					
$N_{H,LoS}$	53.45	12.77	49.18	0.45	NV vs U: 0.61 NV vs V: 0.95 U vs V: 0.29
$\sigma(C_{inst.})$	0.36	0.20	0.19	0.68	NV vs U: 0.60 NV vs V: 0.57 U vs V: 0.96
Γ	1.81	1.70	1.53	0.14	NV vs U: 0.89 NV vs V: 0.29 U vs V: 0.14
C_f	0.43	0.59	0.50	0.30	NV vs U: 0.40 NV vs V: 0.43 U vs V: 0.68
θ	65.50	60.00	60.00	0.52	NV vs U: 0.60 NV vs V: 0.57 U vs V: 0.79
F_s	1.08	1.06	0.61	0.64	NV vs U: 0.90 NV vs V: 0.80 U vs V: 0.79
$N_{H,eq}$	505.00	126.60	41.77	0.56	NV vs U: 0.90 NV vs V: 0.80 U vs V: 0.14

Note— We applied the Kruskal-Wallis (KW) and pairwise Kolmogorov-Smirnov (KS) tests to examine statistical differences in the fitting values across the three variability classes and models. No significant differences are found. The small sample sizes, however, limit the test sensitivity. *Columns:* 1) considered parameter; 2–4) medians, where NV = non-variable, U = undetermined, and V = variable; 5) KW-test p-value; 6) KS-test p-value.

E. MCG-03-34-064 FITTING RESULTS

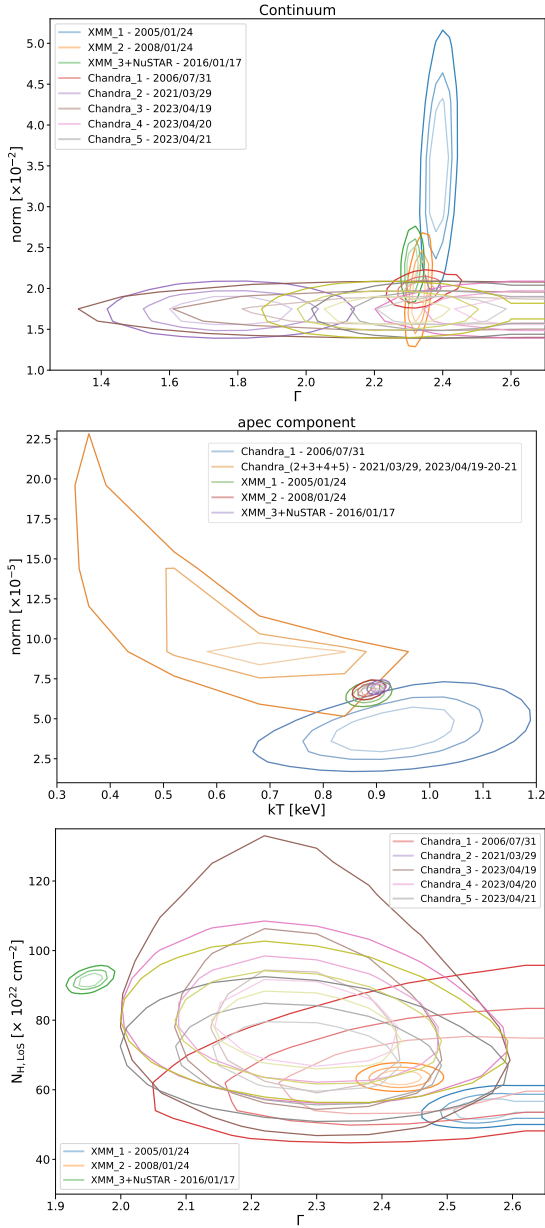


Figure 18. MCG-03-34-064 contour plots considering the best-fit obtained with *X-skirtor*, showing that the assumption of a constant spectral shape across epochs is not valid for this AGN. *Upper panel:* photon index Γ versus normalization of the primary continuum. *Middle panel:* plasma temperature versus normalization of the apec component. *Lower panel:* X-ray photon index versus $N_{\text{H,LoS}}$. The plot in the *upper panel* is obtained considering our first step best-fit with all observation linked together and with Γ free to vary for each; the plots in the *middle* and *lower panels* considers the second step best-fit, where the available observations are fit independently (see Sect. 8 for more details).

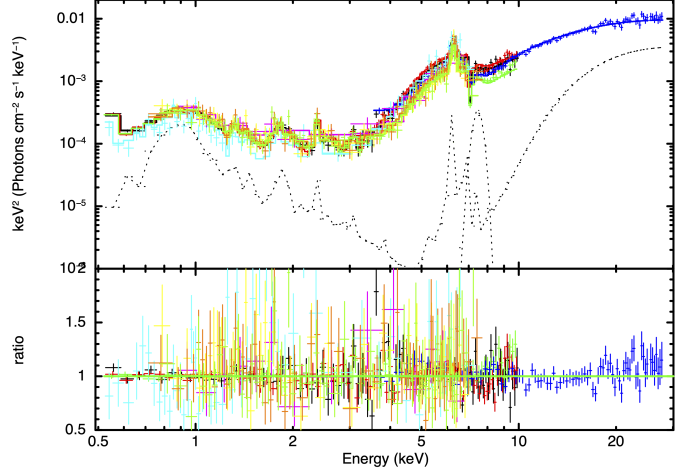


Figure 19. MCG-03-34-064. Second step best-fit with the *X-skirtor* torus model, refer to the results reported in Table E.13. The *Chandra* (in pink, yellow, orange, light green, and lime), *XMM-Newton* (in black, red, and green), and *NuSTAR* (FPMA and FPMB spectra are grouped together in blue) spectra are shown.

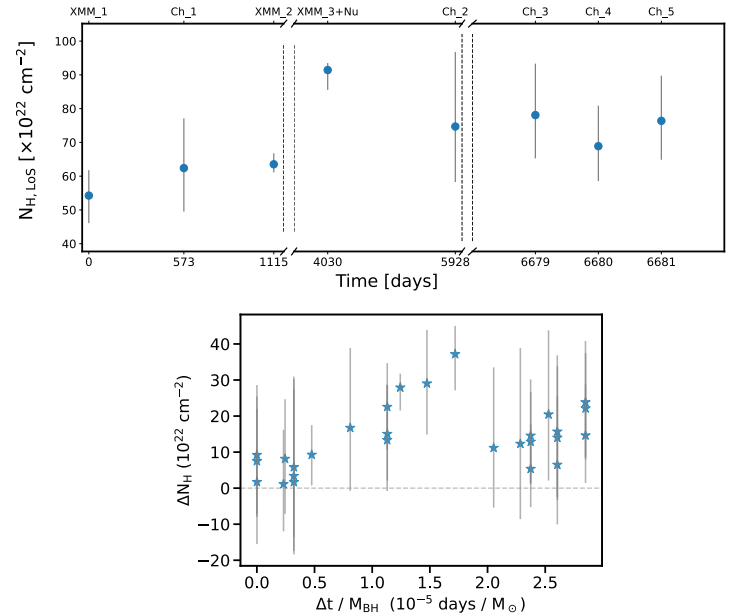


Figure 20. MCG-03-34-064. *Upper panel:* evolution of the $N_{\text{H,LoS}}$. The x-axis is in linear scale with visual breaks to better visualize the observations. *Lower panel:* variations of $N_{\text{H,LoS}}$ as a function of the time separation between observations, normalized by the black-hole mass, considering *X-skirtor*.

Table E.13. MCG-03-34-064: second step best-fit spectral analysis for X-skirtor.

Parameter	XMM.1	XMM.2	XMM.3+NuSTAR	Ch.1	Ch. (2+3+4+5)
apec (Thermal emission)					
kT / keV	0.88±0.02	0.89±0.02	0.87±0.01	0.93±0.13	0.75 ^{+0.14} _{-0.29}
Comptonized primary continuum					
Γ	2.56 _{-0.05}	2.42 ^{+0.05} _{-0.04}	1.95 ^{+0.03} _{-0.01}	2.44 _{-0.22}	2.28 ^{+0.22} _{-0.21}
Neutral reflector					
C _f	0.65 _{-0.14}	0.64 _{-0.02}	0.65 _{-0.07}	0.59 ^{+0.19} _{-0.11}	0.65 _{-0.04}
θ / deg	73 ⁺¹⁷ ₋₁₃	60 ^f	56±2	60 ^f	60 ^f
F _s / 10 ⁻³	7.96 ^{+2.15} _{-1.91}	7.47 ^{+1.02} _{-1.19}	24.35 ^{+3.25} _{-3.84}	5.82 ^{+7.42} _{-3.52}	11.56 ^{+5.91} _{-4.03}
norm / 10 ⁻²	1.91 ^{+0.86} _{-0.41}	2.12 ^{+0.39} _{-0.27}	0.78 ^{+0.15} _{-0.10}	2.27 ^{+2.97} _{-1.37}	1.45 ^{+1.06} _{-0.61}
N _{H,eq} / 10 ²² cm ⁻²	31.31 ^{+40.34} _{-6.58}	145.81 ^{+47.43} _{-30.20}	483.29 _{-156.60}	101.55 ^{+817.87} _{-67.64}	1000 _{-502.08}
N _{H,inst,num.} (LoS hydrogen column density)					
N _H / 10 ²² cm ⁻²	54.25 ^{+7.54} _{-8.16}	63.52 ^{+3.26} _{-2.41}	91.43 ^{+2.07} _{-5.89}		
N _H ^{Ch.1} / 10 ²² cm ⁻²				62.39 ^{+14.71} _{-12.90}	
N _H ^{Ch.2} / 10 ²² cm ⁻²					74.70 ^{+22.09} _{-16.43}
N _H ^{Ch.3} / 10 ²² cm ⁻²					78.09 ^{+15.24} _{-12.83}
N _H ^{Ch.4} / 10 ²² cm ⁻²					68.88 ^{+11.97} _{-10.35}
N _H ^{Ch.5} / 10 ²² cm ⁻²					76.38 ^{+13.35} _{-11.52}
F _{2-10keV} / 10 ⁻¹² erg s ⁻¹ cm ⁻²	2.57 ^{+0.32} _{-0.74}	2.84 ^{+0.04} _{-0.10}	1.83 ^{+0.12} _{-0.02}	1.79 ^{+0.64} _{-1.34}	1.94 ^{+0.63} _{-1.49}
Statistic					
χ ² /d.o.f.	85/79	86/81	264/236	56/50	201/183
T	0.68σ	0.56σ	1.82σ	0.85σ	1.33σ

p-value for the model: 1.49 × 10⁻³

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